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Revisiting the competitive storage model as a tool for the empirical analysis of commodity price volatility.

Nicolas Legrand

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Reconsidérer le modèle de stockage compétitif comme outil d'analyse empirique de la volatilité des prix des matières premières

Thèse de doctorat de l'Université Paris-Saclay
préparée à AgroParisTech (l'Institut des
sciences et industries du vivant et de
l'environnement)

École doctorale n°581 Agriculture, alimentation, biologie,
environnement et santé (ABIES)
Spécialité de doctorat: Sciences économiques

Thèse présentée et soutenue à Paris, le 21 novembre 2016, par

Nicolas Legrand

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Contents

Remerciements	i
1 Introduction	1
1.1 Motivation	1
1.2 Empirical strategies in macroeconomics	2
1.2.1 Two complementary approaches	2
1.2.2 One and not the place to start	4
1.3 Organization of the dissertation	5
2 Review and Perspectives	8
2.1 Two views of commodity price fluctuations	10
2.2 Empirical validation as justice of the peace	10
2.2.1 Confronting the cobweb models to the data	11
2.2.2 Empirical performance of the competitive storage model	12
2.2.3 The excess co-movement puzzle	26
2.3 The interest rate channel	28
2.3.1 The latent Hotelling's rule	29
2.3.2 The exchange rate pass-through	30
2.3.3 The overshooting theory	33
2.4 The outlook	35
3 Trending Commodity Prices	37
3.1 The model	40
3.1.1 Model equations	40
3.1.2 How can storage generate high serial correlation?	42
3.2 Econometric procedure	43
3.2.1 Trend specifications	44
3.2.2 The likelihood estimator	45
3.3 Estimation results	48
3.3.1 Data	48
3.3.2 Model selection	48
3.3.3 No trend	49
3.3.4 Models with a time trend	54
3.3.5 Model predictions	55
3.4 Conclusion	58
3.A Numerical method	60
3.B Computational details	60

3.C	Small sample properties	61
3.D	Supplementary tables	64
3.E	Supplementary figures	67
4	Bayesian Estimation of the Storage Model using Information on Quantities	68
4.1	The Model	69
4.1.1	Model equations	69
4.1.2	Model solution	72
4.2	Overview of the grains market	73
4.2.1	Data	73
4.2.2	Descriptive statistics	75
4.3	Estimation	77
4.3.1	The likelihood function	78
4.3.2	Prior distribution of the parameters	81
4.3.3	Posterior estimates of the parameters	82
4.4	Conclusion	86
5	The Crowding-Out Effect of Storage on Investment	89
5.1	Preamble	90
5.2	Introduction	97
5.3	Complementary theories: A Literature Review	99
5.3.1	Investment dynamics and constraints	99
5.3.2	The competitive storage model	100
5.3.3	The determinants of futures pricing	102
5.4	Theory and Facts	105
5.4.1	A tale of investment and storage	105
5.4.2	The data	106
5.4.3	Empirical features	108
5.5	Model	114
5.5.1	Model's equations	114
5.5.2	The competitive equilibrium	115
5.5.3	Numerical Solution	116
5.6	Simulation Results	117
5.6.1	Calibration	117
5.6.2	Theoretical insights	118
5.6.3	Discussion	126
5.7	Conclusion	132
6	Conclusion	134
6.1	General Conclusion	134
6.2	Perspectives	136
	Bibliography	146
	Résumé substantiel	i

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CHAPTER 1

INTRODUCTION

1.1 MOTIVATION

In 2013, at the beginning of my research, the commodity prices experienced one of their episodic crises, with crude oil prices lying above the US\$ 100 a barrel and a price of the ton of corn close to US\$ 250. Such rocketing prices have devastating consequences in terms of food security on the poorest population, especially the poorest, and can trigger social unrest and riots. Ironically, although today these same two prices are about twice as low, the situation is no less worrisome for the government of exporting countries, where national income primarily relies on the production of one particular basic product. The current social and political instabilities in Venezuela exemplify the adverse consequences of the recent collapse of the crude oil price. Actually, whether too high or too low, at both the micro or macro levels, commodity prices affect a large spectrum of domestic as well as international economic activities, and thus the issues related to their volatility have always been high on the political agenda.

That said, to take any effective actions, whether designed to smooth the prices fluctuations or to protect itself against them, there is a need to know what are the main causes of these typical instabilities in commodity markets. Among the reasons advanced were the rising demand from emerging economies such as China and India, the biofuels mandates entering in competition with food products, the side-effects of climate change with more frequent droughts and flooding threatening the global supply, the weaker US dollar in response to the monetary policy in the US following the 2008 financial crisis or else the financialization of commodity markets with investors willing to diversify their portfolio and speculating in the financial markets. But there are many others and nearly each explanation call for a specific remedy, if any, not always compatible with one another. Worse still, I had the feeling that the difference of opinions varied with the study's sponsors or the targeted audience, and reflected more personal beliefs dictated by self-economic interests and political biases, rather than true objective arguments grounded in "neutral" science. In fairness to these conflicting views, none of them is completely wrong nor the whole truth and all deserve a careful examination.

In this respect, not really convinced by the explanation brought so far and, in face of the lack of consensus around issues where the stakes are yet so high, I decided to undertake research and attempt to modestly add to our common knowledge of the behavior of commodity prices. With hindsight, I must confess that I better

understand the reasons why it is so complicated to draw decisive conclusions about the main factors driving the world prices dynamics. Nonetheless, this is not to say that nothing can be done for attempting to improve our understanding of the workings of international markets of basic goods. Given my scientific education, I naturally chose to tackle the topic on a quantitative front which usually involves statistical techniques. Unlike the qualitative approaches, any empirical analyses cannot but rely on a model designed to represent and explore the observed data in a disciplined fashion. The competitive storage model pioneered by Gustafson (1958) is one such analytical device when it comes to study the aggregate fluctuations of storable commodity prices. At the heart of the framework is the storage theory stipulating that the ability to store primary products is an essential determinant of the observed price variations. This thesis is dedicated to evaluate and improve the empirical relevance of the storage theory in confronting the competitive storage model to the observed data.

Before delving into the details of the inner working of the storage model, first I would like first to evoke the variety of statistical tools available, of methods used to be developed in empirical macroeconomics to provide quantitative answers to the essential concerns related to, among others, the determinants of the economic growth and unemployment, the effects of monetary and fiscal policies, and the way they relate with one another. This aims at getting the big picture of the lines of economic research followed in the present work.

1.2 EMPIRICAL STRATEGIES IN MACROECONOMICS

Global commodity prices being nothing but macroeconomic variables, their study rests on the reservoir of macroeconometrics techniques set up to isolate regularities, to interpret and identify salient patterns in every sample of observed data, as well as to uncover correlations and even causalities across variables. As most of the statistical procedures applied thereafter are borrowed from this toolkit, I will depict a brief summary of the shared traits between all these econometrics methods along with their main strengths and weaknesses.

1.2.1 TWO COMPLEMENTARY APPROACHES

As demonstrated at length in the survey of Labys (2006, Ch. 1) in the case of commodity prices, there exists a multitude of econometrics techniques for analyzing a times series whether at the short, medium or long-run frequencies. They can nevertheless be divided into two major categories known as the structural and “atheoretical” estimations strategies, whether they incorporate restrictions derived from the economic theory.

A GRADIENT OF ECONOMIC THEORY A first way of studying the variations of macroeconomic variables is to focus on the aggregated relationships. In this spirit, the models takes the form of regression equations in which endogenous variables gathered on the left-hand side are explained by a set of exogenous variables appearing on the right-hand side. The links between the variables can possibly be assumed non-linear to accommodate more complex dynamics, while the relative explanatory power of each variable is eventually assessed using standard statistical tests of significance. But in the end, the logic is still to “let the data speak”

and reveals both the nature and the significance of the relationships as well as dependencies between the variables of interest. This ad-hoc characterization of the macroeconomic behavior is a quite flexible and robust way of summarizing the properties of the data. The thing is that the results are hardly interpretable without a minimum of economic theory. Put crudely, to pass from observed correlations to conclusions about causality relationships often requires to incorporate some theoretical assumptions.

This is where the alternative structural strategy takes on its full meaning. More precisely, the gist of the methodology is to combine the data with a set of theoretical restrictions mostly derived from the microeconomic principles including the specification of production and consumption functions, market equilibrium conditions (e.g., market clearing, accounting identities), the agents' behavior, namely the way dynamic decisions are made. Embedding additional information borrowed from the economic theory should in principle guarantee the model internal consistency, and enable a clear and hopefully direct economic interpretation of the values of the estimated parameters. Nonetheless, if the modeling relies on inadequate assumptions the model's fit is worse and the whole theoretical structure can well be rejected by the data. Actually, there is no such thing as a divide between both approaches since there exists a continuum of models depending on the degree of economic constraints integrated in the estimation procedure. In addition, more often than not the reduced-form versions of structural models prove useful to assess the relevance of a theory in formally testing the validity of the restrictions the latter imposed on the data (Deaton and Laroque, 1992).

THE CHANGE OF PARADIGM The aforementioned distinction between the modeling approaches was insignificant until the end of the 1970's since, at that time, the empirical macroeconomics mostly relied on the structural econometric models (SEMs) which consisted in a mixture of both structural and ad-hoc equations relating aggregated economic variables and estimated independently of one another. Models of this type in the case of international commodity markets can be found in Labys (1973). However, not only the SEMs given their large size—e.g., often several tens of equations—were cumbersome and relatively sluggish, struggling for example to accommodate structural breaks in the economic environment, but above all they did not survive both the Lucas (1976) and Sims (1980) critiques. The latter, in turn, marked the start of a new era in macroeconometrics.

The Lucas (1976) critique has to do with the lack of internal consistency resulting from the juxtaposition of unrelated equations as is the case in the SEMs, and the fact that the reduced-form relationships include parameters likely to change with the various government policies and thus deliver invalid conditional forecasts, needed when it comes to compare the macroeconomic impacts of alternative monetary and fiscal policies. Therefore, according to Lucas a model should only contain structural equations with deep parameters invariant to the policy regime. Completed with Sargent (1976)'s econometric work on the power of rational expectations, this call for internal consistency and microfounded models—i.e., derived from the intertemporal optimizing behavior of agents—gave birth to the Dynamic Stochastic General Equilibrium models (DSGEs).¹ Unlike the SEMs, the DSGEs models are of smaller size, rest on a sound theoretical

¹ See Smets and Wouters (2007) for a standard DSGE model in the modern macroeconometrics literature.

basis squared by microeconomic principles and, above all, are now estimated as a whole system of equations thereby preserving the internal consistency of the structure.

From Sims' standpoint, the major empirical failure of the SEMs' approach was twofold: (i) the estimation equation by equation which does not allow for interrelationships across variables even though, especially in macroeconomics, the causalities might well be reciprocal, and (ii) regarding the structural equations, the assumed character exogenous or endogenous of the different variables and, more broadly, the constraints imposed by the economic theory might well be at odds with the data, thereby crippling the quality of the model's predictions. In other words, Sims (1980) places greater emphasis on the external consistency of the modeling and thus suggests instead a flexible econometric strategy, known as Vector Autoregressive models (VARs), in which variables are regressed on their own past values along with those of the related variables embedded in the model. Having said this, estimation of VARs requires identification restrictions which can either belong to the shocks ordering or to the economic theory then leading to the Structural Vector Autoregressive models (SVARs). Studying the propagation of an oil price shock and quantifying its macroeconomic impacts as is done in Kilian (2008), is one illustration of the SVARs models' use in the empirical literature of commodity prices.²

In summary, the modern macroeconometrics relies on two streams of strategies, the choice between both of them resulting from a trade-off between the targeted level of internal and external coherence, interpretability of the results and model's fitting performance. That said, as illustrated with the SVARs models, the boundary between both new generations of models remains porous.

1.2.2 ONE AND NOT THE PLACE TO START

The following dissertation explores the commodity price volatility using the competitive storage model with rational expectations as an analytical tool. In substance, it is a basic supply and demand dynamic equilibrium model of the world commodity market in which storage plays a key role. According to the storage theory, the market demand not only consists in a demand for immediate consumption, but also in a speculative demand from forward-looking and rational storers buying in expectations of profits despite the carrying costs incurred. To complete the set of assumptions, the production is subject to random shocks while the market clears in every period. Specified like this, the core system of equations structuring the storage model is fully microfounded thereby insuring internal consistency and thus immunity to the Lucas critique. In addition, as shown in Cafiero et al. (2011b), even in its crudest form, the canonical storage model proves able to replicate many typical aspects observed in the commodity price series including nonlinearities, autocorrelation, cluster of volatility and asymmetries in the distribution.

All in all, the rather clear microfoundedness combined with the demonstrated satisfying empirical performances make the competitive storage model with rational expectations a good candidate to start thinking about global commodity price volatility. What is more, although it is only a partial equilibrium model of the global commodity markets, the rational expectations storage model shares many features with

² Refer also to (Kilian, 2009, Inoue and Kilian, 2013, Kilian and Murphy, 2014, Baumeister and Hamilton, 2015) for more about the use of SVARs models in the context of commodity prices.

the DSGE models and thus the empirical studies of price instabilities in world commodity markets pursued in this thesis sit in this branch of the macroeconometrics literature. Recalling that research advances in empirical macroeconomics have always resulted from the combinations of theories with facts, I will build upon the existing body of work dedicated to assess the quantitative merits of the storage theory and, taking the storage model to the real data, attempt to improve its explanatory power while maintaining its internal consistency.

From this perspective, I will voluntarily omit, or at best only evoke, the purely statistical approaches essentially based on the VARs models. This is not to say that I think they are useless, quite the contrary in fact. Indeed, in many respects these theory-free models directly focused on the aggregated relationships between the macroeconomic variables of interest and which do not bother with the microfoundations' issues, prove to be highly complementary to the structural empirical studies to which this thesis conforms. Among their main appeal are the often better predictive abilities, the demonstrated greater robustness to the almost inevitable misspecifications and, even more importantly maybe, their suitability to handle in a quantitative manner the variety of macroeconomic drivers. More precisely, the ad-hoc relationships can *(i)* shed light to some empirical flaws in the modeling such as important observed dynamics not yet explained by the model but which deserved careful considerations, and even *(ii)* be used as temporary model's repairs to capture a particular phenomenon in the data so as to increase the model's external consistency the time needed to develop the adequate microfoundations accounting for the phenomenon in question. For all these reasons these two pillars of macroeconometrics are definitively not substitute and should work hand-in-hand rather than being opposed as it happens sometimes. In this spirit, the VAR techniques can deliver very valuable insights for a comprehensive knowledge of the main drivers governing the behavior of commodity prices and has its entire place in the empirical analyzes of the commodity price volatility along with the related discussions. Still, they are well beyond the primary scope of this thesis and thus will not be further examined.

1.3 ORGANIZATION OF THE DISSERTATION

This thesis falls in four main chapters. The first one carries on the Cafiero and Wright (2006)'s textbook chapter and surveys the empirical strategies designed to take the storage model to the data. It ends by setting the stage of the rest of the dissertation in suggesting avenues of model's extensions to increase its explanatory power, some of which are then followed by the three other chapters. Based on the model's empirical failures pointed out in the survey, the subsequent two aim at estimating richer storage model specifications likely to improve the fitting performance of the model. The last one is more theoretical and, taking the example of the crude oil market, analyzes the implications in terms of price dynamics resulting from the negative interactions between investment and storage. It includes a short and self-contained preamble, written for a non-academic audience, which attempts to offer a narrative of the wild swings in crude oil prices, highlighting the paramount importance of returning to the supply and demand fundamentals when it comes to try to understand the dynamics of price in the crude oil market. This justifies the modeling approach adopted thereafter in the rest of the chapter, namely an extension of the storage model on the supply-side.

CHAPTER 2: A REVIEW OF THE EMPIRICAL PERFORMANCE OF THE STORAGE MODEL This chapter aims at setting the scene of this thesis. It presents both the history and the state-of-the-art of the empirical approach of the modeling of the world commodity price volatility, in placing the storage model at the heart of the analysis while outlining the key milestones. Specifically, I try to offer somebody unfamiliar with the related literature a gist of the modeling issues at stakes from both a retrospective and speculative view point. I remain focused on the empirical techniques designed to assess the merits of the storage theory without trying to be exhaustive, and thereby leaving aside the purely statistical approaches, weakly linked to the storage model and well beyond the scope of the present dissertation. I conclude by suggesting a research agenda at all times frames for overcoming the current empirical flaws and hopefully improving the storage model explanatory power. The subsequent three chapters then deal with one of each of the noted pitfalls in attempting to provide remedies.

CHAPTER 3: ESTIMATING THE STORAGE MODEL WITH TRENDING PRICES The chapter, co-authored with Christophe Gouel and to be published in the Journal of Applied Econometrics, presents a method to estimate jointly the parameters of a standard commodity storage model and the parameters characterizing the trend in commodity prices. Introduced in the DSGE literature by Canova (2014), this procedure allows the influence of a possible trend to be removed without restricting the model specification, and allows model and trend selection based on statistical criteria. The trend is modeled deterministically using linear or cubic spline functions of time. The results show that storage models with trend are always preferred to models without trend. They yield more plausible estimates of the structural parameters, with storage costs and demand elasticities that are more consistent with the literature. They imply occasional stockouts, whereas without trend the estimated models predict no stockouts over the sample period for most commodities. Moreover, accounting for a trend in the estimation imply price moments closer to those observed in commodity prices. Our results support the empirical relevance of the speculative storage model, and show that storage model estimations should not neglect the possibility of long-run price trends.

CHAPTER 4: BAYESIAN ESTIMATION OF THE STORAGE MODEL USING PRICES AND QUANTITIES This chapter, written in collaboration with Christophe Gouel, presents a new strategy to estimate the rational expectations storage model. The main innovations are twofold. First, it uses information on prices and quantities – consumption and production – in contrast to previous approaches which use only prices. This additional information allows us to estimate a model with elastic supply, and to identify parameters such as supply and demand elasticities, which are left unidentified when using prices alone. Second, contrary to the previous chapter, the estimation relies on the Bayesian methods, popularized in the literature on the estimation of DSGE models, but so far never used to recover the parameter estimates of the storage model. The primary reason for this choice is that, as is often the case in the estimation of dynamic models, the likelihood is flat into certain areas and/or exhibit many local maxima. In this context, the classical inference approach has trouble finding the global maximum of the likelihood and, as shown in chapter 3, usually requires an initial grid-search routine to locate a candidate maximum along with the cumbersome implementation of sophisticated algorithms like simulated annealing. It is even more challenging as the number of parameters

to be estimated increases, not to mention the computation of the corresponding standard errors or confidence intervals. As long as inference is relying on prices alone, given the small number of parameters that can be freely identified (three at the most), maximizing the likelihood function is not that big a deal. But now with the increase in the dimensionality of the likelihood function (e.g., up to four times), the superiority of the Bayesian techniques appears even more obvious. The Bayesian inference is finally carried out on a market representing the caloric aggregate of the four basic staples – maize, rice, soybeans, and wheat – from 1961 to 2006. The results show that to be consistent with the observed volatility of consumption, production, and price, elasticities have to be in the lower ranges of the elasticities in the literature, a result consistent with recent instrumental variable estimations on the same sample (Roberts and Schlenker, 2013).

CHAPTER 5: THE CROWDING-OUT EFFECT OF STORAGE ON INVESTMENT This chapter opens with a short story of the recent collapse of the most scrutinized crude oil price. Although self-contained and written in a non-technical fashion, it lays out the main features a model should encapsulate to be able to deliver consistent explanation of the observed behavior of crude prices. On top of the list are sticking to the dynamics of the market fundamentals: supply, demand and inventories.

Apart from the opening preamble, the rest of the chapter has been written in collaboration with Assia Elgouacem. It aims at connecting and building upon three strands of the finance and economics literature so as to feature the essential structural forces driving the commodity price in the world market. In particular it hones in on the interaction between storage and investment by showing that the presence of storage brings forth features in the investment and commodity price dynamics that cannot be accounted for when focusing only on investment. Even more interestingly, exploiting the positive relationship between the levels of inventories and the forward price volatility, we find that storage has a crowding-out effect on investment. The crude oil market will be used as a guideline illustration since it embodies, fairly well, this crowding-out phenomenon as well as the occurrence of booms and busts cycles characterizing the prices behavior of most commodities. Ideally, we would estimate the model's deep parameters as has been done in the previous chapters. In face of the computational challenge involved, as in Routledge et al. (2000) and in Carlson et al. (2007) we contend with a calibration-simulation exercise to explore the empirical relevance of the new framework. The results shed light on (i) the importance of introducing storage in an irreversible investment model to generate the price and investment patterns observed in the data, (ii) the key role of the storage arbitrage condition not only in dictating the impact of the irreversibility constraint on the timing of investment, but also in causing a crowding-out effect of storage on investment, and (iii) the close relationship between the market fundamentals and the term structure of forward curves given that the behavior of investment and storage are better reflected in the slope of the forward curve rather than in the levels of spot and futures prices which are mainly governed by global business cycles.

CHAPTER 2

THE COMPETITIVE STORAGE MODEL ON THE EMPIRICAL FRONT: REVIEW AND PERSPECTIVES

Commodity prices are known to experience wild swings hurting producers along with consumers and thus have always been high on the political agenda. The thing is that there is a host of effective causes behind such a sharp volatility and not all of them required government intervention. As different determinants entail different cures, policy guidance in this respect, and let alone on the quantitative front, cannot but relies on a sound model featuring not only the economics mechanisms underlying the formation of commodity prices, but also the key drivers governing the observed dynamics and the way external shocks propagate into the system. It has to be both empirically relevant so as to account for the bulk of the observed patterns in the data, and transparent in the sense of allowing a clear understanding of the interdependence between the variables involved along with a description of the effects of a given policy. Simply put, there is a trade-off between model complexity and readability, internal and external consistency putting more weight on one or the other depending on the prime target of the policy implemented.

One such candidate when it comes to think about prices instability in world commodity markets is the competitive storage model with rational expectations, whose foundations have been first laid out in Gustafson (1958). In essence it is a mere supply and demand dynamic equilibrium model of the commodity market with the peculiarity of placing storers at the center of the stage. This speculative demand for storage, by absorbing and spreading the exogenous disturbances to the market, plays a key mediating role in the implied dynamics of prices. This is not to say that the storage theory is the only way of thinking about commodity price volatility and stabilization policies.¹ Yet, it has become the cornerstone of empirical studies dealing with the prices fluctuations in the global markets of primary products, and several derived versions started flourishing in the dedicated literature (Wright and Williams, 1982, Williams and Wright, 1991, Deaton and Laroque, 1992) depending on the topics for which it was supposed to provide answers.

This chapter aims at summarizing the state-of-the-art of the empirical approach of the modeling of the world commodity price volatility in placing the storage model at the heart of the analysis. Specifically, I will try to offer somebody unfamiliar with this literature a gist of the modeling issues at stake from both a

¹ The traditional opposite view is to consider that prices fluctuations are endogenous and originate from the agents' forecasting errors as posited by the cobweb theorem (Ezekiel, 1938).

retrospective and speculative view point. The dedicated literature being large, I will focus on the empirical techniques designed to assess the merits of the storage theory without trying to be exhaustive, and thereby leaving aside the purely statistical approaches, weakly linked to the storage model and well beyond the scope of the present dissertation.² Indeed, the objective here is only to set the scene of this thesis in staying consistent with the upcoming chapters.

As said earlier, the usefulness of any economic model should be evaluated in light of its performance with respect to both the assigned goals of internal and external consistency. From this perspective, the achievements of the storage model and the associated theory are fairly mixed. On the one hand, in many respects its success regarding the first criterion is hardly disputable: the model is both parsimonious and theoretically grounded with crystal clear mechanics. On the other hand, the external consistency of the storage has been challenged in the early structural estimations published in Deaton and Laroque (1996). At that time the empirical approach developed for a full test of the storage theory against the observed price data was as innovative as the conclusions disappointing. The version of the model tested failed to match the typical high levels of serial correlation observed in the real price data.³ This may have cast a chill in the entire research community working in this field. It is only a decade later that Cafiero and Wright (2006) pointed out in the estimation procedure several pitfalls of various nature—e.g., empirical, theoretical and numerical—and which, once settled, might well improve its explanatory power. Since then, and with the benefit of a further round of mathematical and computational advances, these same authors have addressed most of the previously identified models' failures, and especially the lack of induced persistence in prices. This in turn contribute to restate in part the empirical relevance of the storage theory. That said, the autocorrelation is not the only aspect in the behavior of commodity prices that the storage model struggles to match. Chief among them maybe is the excessive correlations across commodity and other asset prices alike, also known as the “excess of co-movements” puzzle (Pindyck and Rotemberg, 1990).

In this survey I will attempt to carry on the work of Cafiero and Wright (2006) and it is thus built in a similar fashion. Section 2.1 briefly reviews the two classical ways—e.g., endogenous or exogenous—to think about price instabilities in commodity markets. Section 2.2 starts by presenting the various econometrics techniques designed to put these two theories into tests against price data. The data poorly supports the endogenous explanation which naturally leads to favor the storage theory upon the cobweb alternative. Acknowledging the apparent superiority of the storage theory, I keep on studying the variety of empirical strategies employed to take the storage model to the data, shedding light on the key developments achieved so far and pointing out the dimensions in which it does not perform well. Section 2.3 discusses the possibility of improving the model fit with the introduction of macroeconomic effects through the interest channel. In the final section I summarize the main results and suggest a feasible research agenda covering different time horizons and embedding potential solutions for overcoming the noted obstacles and improve the model empirical performance.

² These times-series techniques are studied at length in the Labys (2006)'s textbook.

³ Recall that the transfer of inventories from one period to the next is the unique source of persistence in prices, provided that the shocks to the system are assumed i.i.d. following a normal distribution.

2.1 TWO VIEWS OF COMMODITY PRICE FLUCTUATIONS

In the theoretical literature of commodity price dynamics, there are two competing explanations to account for the price variations.⁴ The first approach follows the cobweb theorem stated by Ezekiel (1938) according to which the instability of prices stems from the combination of a lag between the supply and demand decisions with expectations failures. Depending of the relative slopes of supply and demand curves, disturbances in yields may lead the dynamics of prices on explosive paths. To address Buchanan (1939)'s criticism of internal contradiction and more generally to deliver a more realistic and complex price behavior, the traditional linear cobweb model has been extended through the introduction of adjustment costs, risk aversion, non-linear curves, and heterogeneous agents with either rational or backward-looking expectations. But in the end, the cobweb logic still consists in considering the origin of prices instability as internal to the market mechanisms.

On the other hand, the rival theory assumes the primary source of price fluctuations of being exogenous in a scheme where agents rationally make decisions eventually subjected to unexpected supply and/or demand disturbances. The storage model sits in this tradition. Gustafson (1958) provides the numerical tools to solve a version of the model without supply reaction but with a non-negativity constraint on storage. Few years later, Muth (1961) lays out the rational expectations framework of the competitive storage model where actual output fluctuates around a steady planned production, and allowing negative inventories shows how the additional demand from speculative storers affects the overall price behavior on the market. By precluding the existence of a closed-form solution, the binding constraint on storage complicates the model resolution but, more interestingly, induces non-linearities in the fluctuations of prices depending on the levels of stocks. Thorough studies of the storage models, its interactions with trade and its final implications on the prices dynamics then have been pursued by Wright and Williams (1982, 1984), and summarized in Williams and Wright (1991). In an effort to reach a more realistic modeling, further extensions to account for intra-seasonal shocks have been achieved by Lowry et al. (1987), Williams and Wright (1991, Ch. 8), Chambers and Bailey (1996), Ng and Ruge-Murcia (2000), and Osborne (2004) among others.

In sum, whether the expectations are assumed to be naive, backward-looking, adaptive, or rational the resulting dynamics of prices follow one of the two endogenous or exogenous modeling strategies. Although none of them is the whole truth, since both conflicting explanations lead to radically different conclusions regarding the appropriateness of policy interventions there is a need to decide among them.

2.2 EMPIRICAL VALIDATION AS JUSTICE OF THE PEACE

The opposition between both theories lies in the way the agents are assumed to form their expectations. The thing is that it is difficult to test hypotheses on the formation of expectations, as discussed in Nerlove and Bessler (2001). This is why Prescott (1977)'s view has been retained in most of the subsequent attempts to empirically validate the models rooted in either theories. In substance, the logic consists in confronting the models to the observed data and, in turn, deduce the consistency of the underlying theory. In other words,

⁴ A more complete survey of this debate and the associated policy implications can be found in Gouel (2012).

what is assessed is the ability of a model to closely replicate the main stylized facts of a given price series, the only observable considered in all the statistical analyses thus far.⁵ Before delving into the empirical assessment of the two classes of models, it worth noting that one of the chief characteristic of the price of storable commodities, namely the occurrence of rare but severe spikes interrupting long periods of low and stable prices, calls for the use of non-linear dynamic models.

2.2.1 CONFRONTING THE COBWEB MODELS TO THE DATA

The main appeal of the endogenous and non-linear dynamic models is their ability to generate complex and even chaotic price fluctuations. However, in view of the poor robustness of the available inference methods, and more broadly the lack of suitable mathematical tools (Barnett et al., 1995, 2001) to estimate chaotic models, the few econometric works in that field focus on (i) the estimation of reduced-form models, (ii) tests for the presence of chaos in the data, and (iii) qualitative assessments of the correspondence between time series delivered by the model and the main observed patterns of storable commodity prices. According to authors such as Deaton and Laroque (1992), Deaton (1999), or Cashin and McDermott (2002), these key features are high positive autocorrelation, strong volatility, positive skewness, and excess kurtosis.

In this regard, the backward-looking expectations models fail in this exercise since years of scarcity and high prices are seen to last for years to come, which triggers increase in the planned production and lead to fall in prices. Still, more optimistic results can be obtained by the adaptively rational equilibrium model of Brock and Hommes (1997) where both backward-looking and rational expectations are considered. These heterogeneous agent models induce the typical observed long periods of low and stable prices interrupted by booms and bust episodes. Westerhoff and Reitz (2005) undertake a formal estimation of such a model in which the behavior of prices is dictated by the interactions between fundamental and technical traders, the latter having a potential destabilizing effect on prices by triggering self-fulfilling bubbles depending on how far the market deviates from its long-run equilibrium value. Using monthly data of the US corn price, they specify a smooth transition autoregressive generalized ARCH (STAR-GARCH) model which fits well the time-varying impacts of both types of trading strategies. Lastly, regarding the main traction of the cobweb type models which is their ability to create chaotic dynamics in prices, then again the rare studies attempting to test for the presence of chaos in times series failed (Chatrath et al., 2002, Adrangi and Chatrath, 2003).

In summary, it is extremely difficult to conduct econometrics test of the cobweb theory. Overall, if the few existing empirical analyses tend to confirm the non-linear dynamics of price series, they fail to prove that this non-linearity is caused by chaos. In light of this lack of empirical evidences combined with the fuzzy, if any, internal consistency, the view of endogenously driven price dynamics seems to be neither the best nor the most fruitful way to start thinking about commodity price instability in global markets. This is even more true once you recall the fact that the model fits the data better if it incorporates some agents with rational expectations (Westerhoff and Reitz, 2005). This is yet another proof calling for favoring instead the alternative modeling strategy based on the storage theory. The latter in assuming a representative

⁵ The primary reasons for this are the reliability and availability of prices over sufficient long period of time.

rational agent with forward-looking expectations might well deliver a story of commodity price volatility more consistent with the data. This means assessing its empirical merits.

2.2.2 EMPIRICAL PERFORMANCE OF THE COMPETITIVE STORAGE MODEL

Most of the empirical research on the storage model rests on the rational expectations competitive storage model with a non-negativity constraint on inventories, justified on the ground that one cannot store what has not grown yet. The standard form is a partial equilibrium model of the international commodity market in which (i) production is annual and follows a normal i.i.d process, (ii) the demand for consumption is linear, and (iii) prices are mediated by the speculative demand of storers. Following the common strategy of buying low and selling high, the storage activity transfers units of production from years of abundance to years of scarcity, thus smoothing prices and creating the positive autocorrelation. The storage mechanism also implies asymmetries in the price distribution since the additional speculative demand prevents dramatic collapses in prices without being able to avoid price to rocket if stocks are empty. The non-negativity constraint on stocks depicts two regimes for the price process whether inventories are held, that is whenever speculators expect the future selling prices high enough to cover the interest and storage charges incurred to carry inventories next period. Put in equation, the storage arbitrage condition gives us

$$\beta (1 - \delta) E_t P_{t+1} - P_t - k \leq 0, = 0 \text{ if } S_t > 0, \quad (2.1)$$

where $\beta = 1/(1+r)$ is the discount factor which is assumed to be fixed, $\delta \geq 0$ is the depreciation rate of inventories, $k \geq 0$ is the constant per-unit physical cost of storage, P_t is the price, and E_t is the expectation operator conditional on period t information. The model is closed by two other equations. The first one is the market clearing condition stating that every period supply equals total demand:

$$A_t = S_t + D(P_t), \quad (2.2)$$

where A_t is the availability at time t . The second one describes the evolution of the state variable A_t over time, written as the sum of the past inventories and the stochastic production ε_t :

$$A_t \equiv (1 - \delta) S_{t-1} + \varepsilon_t. \quad (2.3)$$

The attempts to test the storage theory in bringing the storage model to the data followed the two common reduced-form and structural empirical approaches.

LIMITED-INFORMATION ESTIMATION TECHNIQUES

A first class of econometric methods relies on picking a set of restrictions imposed by the economic theory of storage and then looking in the data to see if they do manifest actually. For instance, Deaton and Laroque (1992) provide a generalized method of moments (GMM) procedure to estimate the competitive storage

model with inelastic supply and without storage costs.⁶ Resting on the rational expectations assumption materialized in the Euler equation (2.1), they show the existence of a constant threshold price P^* above which storage is no longer profitable. As a result they define an autoregressive process for the equilibrium price function in the form

$$E_t P_{t+1} = \gamma[\min(P_t, P^*) + k], \quad (2.4)$$

with $\gamma = 1/\beta(1 - \delta)$. Hence, the price regime implied by the model is either a stationary process with mean P^* or an autoregressive one with coefficient γ whenever the actual price falls below the threshold P^* . The first moment condition (2.4) written as $u_t = P_t - \gamma[\min(P_{t-1}, P^*) + k]$ allows to derive the following GMM criterion $u'W(WW')^{-1}W'u$ given a matrix W of instrumental variables known at time $t - 1$ and earlier, and thus uncorrelated with the dependent variable P_t provided the hypothesis of rational expectations does hold effectively. Relying on the annual prices of thirteen primary products, they estimate γ and P^* using past prices as instruments and come to mixed conclusions. Interestingly, the prices simulations implied by the calibrated model display most of the essential patterns observed in the actual price series such as the alternation of booms and busts periods, the heteroskedasticity, the positive skewness as well as the fatter right tail. Furthermore, the high values of the estimated cut-off price P^* entails that between 77 to 99% of the time is spent in the regime of active storage, thereby fostering the positive autocorrelation induced by the model. The chief concern noted by the authors is that the simple storage mechanism does not capture most of the serial time dependency since, with values in the range from 0.21 to 0.48, the first-order autocorrelation coefficients of simulated prices never reach half of the true ones. In an attempt to check the validity of the inference procedure they perform autocorrelation tests on residuals assuming that, if the storage model fails to match the actual high degrees of serial correlation, the unexplained autocorrelation should be found in the residuals u_t . However, both the overidentification and the Durbin-Watson tests conducted on the residuals lead to reject the hypothesis of serially correlated residuals, and thus to conclude that no excess serial correlation seems to be left unaccounted for by the autoregression equation (2.4). This tends to qualify the pessimistic conclusion drawn by the authors.

In the same spirit of using reduced-form empirical methods to verify the storage theory, Ng (1996) exploits the implied switching regime of the price dynamics around P^* by fitting the data with a Self-Exciting Threshold Autoregressive model (SETAR) (Tong and Lim, 1980). Interestingly, such a set-up allows to identify which aspect of the storage theory is rejected by the data, a question for which the GMM procedure is silent. Basically, the approach relies on the fact that the price process must exhibit two different stochastic properties depending on whether it lies above or below the cut-off. More precisely, once exceeding the threshold P^* , the price is only given by the inverse demand function, so that the price evolves according to the supply process assumed normally and identically distributed. As previously noted, when inventories are carried over the price follows a first-order autoregressive process and the conditional moments lose their Gaussian nature. For instance, the conditional variance of prices becomes heteroskedastic since the volatility

⁶ The GMM technique introduced by Hansen and Singleton (1982) consists in minimizing the distance between the equation residuals implied by the model and the variables known at time t .

is increasing with the price level as fewer stocks are available to buffer a production shortage.⁷ Using the quasi-maximum likelihood estimator and exactly the same dataset that Deaton and Laroque (1992), she estimates a SETAR(r,d,c,q) model of the form

$$\begin{aligned} P_t &= a_1 + \rho_1 P_{t-1} + e_{1t} \text{ if } S_t > 0, \\ P_t &= a_2 + \rho_2 P_{t-1} + e_{2t} \text{ otherwise,} \end{aligned} \tag{2.5}$$

where the threshold value c is P^* , the number of thresholds r is equal to one along with both the delay parameter d and the order of the autoregression q are equal equal to one as dictated by the theory which also imposes the testable restrictions $\rho_1 > 0$ and $\rho_2 = 0$. Another assumption, albeit not implied by the storage theory, which can be tested from (2.5) is the market efficiency condition given by $a_1 + \rho_1 P^* = a_2 + \rho_2 P^*$.⁸ From the estimation results obtained without imposing the market efficiency condition, she concludes that the whole of conditional mean prices and all but tea, cocoa and rice variances are lower when storage is active, as predicted by the theory. In addition, although most commodity prices show the expected significant persistence in the stockholding regime (e.g., $\rho_1 > 0$), the latter time-dependency remains also significant in the stockout situation (e.g., $\rho_2 \neq 0$), something in clear contradiction with the underlying theory.⁹ In fact, only four out of the thirteen commodity price series provide a full support to the theory. Notwithstanding, and in line with Deaton and Laroque (1992), the author also finds a low frequency of stockouts episodes and underlines the fact that this tends to lower not only the precision in the identification of the parameters of the second autoregression in (2.5), but also the robustness of the standard significance test for the null $\rho_2 = 0$, since it is based on a very limited number of observations which indeed are falling into the stockout regime. Acknowledging this, she infers that when stocks are empty prices are autocorrelated if the absolute value of ρ_2 is substantially greater than zero. All in all, the speculative storage theory cannot be rejected on the sole basis of a statistically significant autoregressive coefficient ρ_2 .

In subsequent work, Beck (2001) completes the empirical analysis by conducting statistical tests for the significance of volatility clustering in the distribution of commodity prices. This also is a key characteristic implied by the speculative storage activity which, by reallocating production across time, creates a channel for the transmission of the price volatility over time.¹⁰ In statistical terms, this means that the price variance should be time-dependent. From an econometric standpoint, the author relies on the generalized autoregressive conditionally heteroskedastic-type models ((G)ARCH(p,q)) to capture the potential time-varying volatility clustering manifested in the residuals of the autoregressive models estimated on commodity prices. The

⁷ The author overlooks the heteroskedasticity issue in noticing that it only affects the efficiency property of a given estimator which, otherwise, stays consistent.

⁸ This relationship is not satisfied for cocoa, rice, tea and tin.

⁹ Imposing the market efficiency restriction does not change the overall conclusion since patterns of serial correlation in prices are also found in both regimes.

¹⁰ Note that this link is either broken when there is a stockout or irrelevant if the commodity is not storable.

general expression of the estimated model is

$$\begin{aligned} P_t &= \alpha + \beta t + \sum_{i=1}^p \rho_{i-1} P_{t-i} + e_t^p, \\ &= \alpha + \beta t + \sum_{i=1}^p \rho_{i-1} P_{t-i} + e_t^d - e_t^s, \end{aligned} \quad (2.6)$$

where the error term e_t^p is the combination of a demand and a supply shock assumed i.i.d. with zero means and variances respectively denoted $\sigma_{\varepsilon^d}^2$ and $\sigma_{\varepsilon^s}^2$, and drawn from a stationary distribution.¹¹ Though both of the external shocks are homoskedastic, she shows that the resulting price variance $\sigma_{\varepsilon^p}^2$ is not constant and depends on its lagged values.¹² It comes $e_t^p = \eta_t \sqrt{h_t}$, where η_t is a white noise and h_t is the expected price variance conditional on past values e_{t-i}^p . In a first step, h_t is assumed to follow an autoregressive moving average ((ARMA(p, q)) process such that:

$$h_t = a_0 + \sum_{j=1}^p a_j \sigma_{\varepsilon_{t-j}^p}^2 + \sum_{k=1}^q b_k h_{t-k}. \quad (2.7)$$

Another testable prediction of the theory is the response of prices to external supply and/or demand shocks that should vary whether or not the non-negativity constraint on inventories is binding. Indeed, high prices are expected to be more volatile as little or no inherited inventories can be used to smooth price changes. Thus, times of high (low) price volatility should be associated with positive (negative) shocks to the price level. The exponential-GARCH model (EGARCH) can characterize this phenomenon and is obtained by rewriting (2.7) as follows:

$$\ln(h_t) = a_0 + \sum_{i=1}^p a_{1i} \left(\frac{e_{t-i}}{\sqrt{h_{t-i}}} \right) + \sum_{i=1}^p a_{2i} \left(\left| \frac{e_{t-i}}{\sqrt{h_{t-i}}} \right| - \mathbb{E} \left| \frac{e_{t-i}}{\sqrt{h_{t-i}}} \right| \right) + \sum_{j=1}^q b_j \ln(h_{t-j}) + u_t, \quad (2.8)$$

where the a_{1i} and a_{2i} parameters account for the asymmetry and the ARCH process respectively. Assuming a first-order ARCH process, a positive value of a_{11} associated with a positive (negative) shock to the price level e_{t-1}^p raises (reduces) the expected price variance h_t .

The final specification estimated in the article is the GARCH in mean (GARCH-M) model to check if in addition of being rational, speculators are also risks averse so that the expected variance has an explanatory power. The GARCH-M provides an explicit link between both the conditional mean and variance of the price and is derived from a simple extension of (2.6) which becomes

$$P_t = \alpha + \beta t + \sum_{i=1}^p \rho_{i-1} P_{t-i} + \theta_1 \sqrt{h_t} + \theta_2 (P_{t-1} \sqrt{h_t}) + e_t^p. \quad (2.9)$$

¹¹ See the paper's appendix for details about the decomposition of e_t^p in both the demand and supply components.

¹² In absence of the storage mechanism, the expected variance is constant as it is only function of the variance of external shocks assumed constant.

Theoretically, if the assumption of risk-averse storers were to hold, θ_1 should be positive given that the more volatile the expected price the lower the amount stored which induces not only a higher price level next period but also a weaker serial correlation ($\theta_2 < 0$).

Although the order of the GARCH terms p and q can be pinned down by the theory as in Ng (1996), here the author chooses the number of lags p according to the Schwartz-Bayesian criteria and checks for the presence in the residuals of serial correlation up to the fourth-order by computing Lagrange multiplier statistics. The results lead her to chose $p = q = 1$, in line with the timing of production decisions assumed in the basic model. Interestingly, using the annual prices of twenty storable and non-storable commodity prices, she finds a significant ARCH(1) process only in the behavior of the former category as predicted by the theory. However, there is no clear distinction between the two types of commodities when it comes to testing for the explanatory power of the conditional variance of prices. Indeed, a significant skewness can be found in the behavior of prices of some storable but also non-storable commodities suggesting that such asymmetry is not entirely created by the zero lower bound constraint on stocks, and that other forces might come into play. Finally, consistent with the assumption of risk-neutral storers made in the standard storage model, the estimation results taken from (2.9) indicate that the forecasting power of the expected variance of prices is not significant.

Although indirect, another proof in favor of the speculative theory of storage is provided by Roberts and Schlenker (2013) whose instrumental variable approach crucially relies on the validity of the speculative storage theory. Indeed, working with the prices of grains, they develop an identification strategy in which past yield shocks has an effect on the levels of inventories carried over and in turn on the futures prices through the storage mechanism. Assuming that weather and demand shocks are uncorrelated, past production disturbances can thus be used to separately identify supply and demand elasticities. The approach and the data used in this article have widely inspired the subsequent Chapter 4.

INSIGHTFUL FUTURES PRICES In another vein, the finance literature also focuses on some of the expected effects of storage in the behavior of futures prices and forward curves. Ng and Pirrong (1994) exploits the long-term equilibrium relationship between the forward and spot prices to derive a variety of testable consequences of the storage theory well detailed and documented in Williams and Wright (1991). They are all about the correlations between spot price volatility, inventories, and spreads between the forward and the spot prices. Recalling that if agents are risk-neutral the forward price is equal to the expected spot price, from the arbitrage condition (2.1) they compute the spread minus the storage and interest costs such that

$$Z_t = \beta F_{t,T} - P_t - k, \quad (2.10)$$

with $F_{t,T}$ the forward (or futures) price as of time t expiring at $T > t$.¹³ The theory of storage states that the lag spread Z_{t-1} will have an explanatory power. The intuition behind that belief is that if supply and demand conditions are the prominent drivers of the commodity price dynamics, a substantial amount of variation

¹³ Under the risk-neutrality and constant interest rates assumptions the distinction between the futures and forward prices is irrelevant (Williams and Wright, 1991). Thus, the two terms will be used interchangeably in the rest of the thesis.

might be explained by the past values of the adjusted spread Z_{t-1} given that the wider the adjusted spread in absolute value, the lower the level of inventories carried over and the more susceptible to shocks the markets.¹⁴ It is indeed the lagged spread value which summarizes the information as of time $t - 1$ (e.g., prior to the shock) and thus that matters when forecasting the variations of spot and futures prices. Turning to the specification of the estimated model, they express the conditional means of the logarithm of spot and futures prices as an error-correction model with time-varying means, variances and covariances of the form

$$\Delta \ln S_t = \alpha_S + \sum_{i=1}^5 \beta_{i,S} \Delta \ln S_{t-i} + \sum_{i=1}^5 \gamma_{i,F} \Delta \ln F_{t-i} + \mu_S Z_{t-1} + \varepsilon_{S,t}, \quad (2.11)$$

and

$$\Delta \ln F_t = \alpha_F + \sum_{i=1}^5 \beta_{i,F} \Delta \ln F_{t-i} + \sum_{i=1}^5 \gamma_{i,S} \Delta \ln S_{t-i} + \mu_F Z_{t-1} + \varepsilon_{F,t}, \quad (2.12)$$

where the commodity is denoted by i , the error terms ε_S and ε_F are assumed to obey a GARCH(1,1) process augmented by the adjusted term spread (e.g., an augmented bivariate GARCH(1,1) model). Hence, the conditional covariance $\sigma_{S,F,t}$ and variances $h_{S,t}$ and $h_{F,t}$ of the spot and futures prices are written as follows:

$$h_{S,t} = \omega_S + \delta_1 h_{S,t-1} + \delta_2 \varepsilon_{S,t-1}^2 + \delta_3 Z_{t-1}^2, \quad (2.13)$$

$$h_{F,t} = \omega_F + \phi_1 h_{F,t-1} + \phi_2 \varepsilon_{F,t-1}^2 + \phi_3 Z_{t-1}^2, \quad (2.14)$$

$$\sigma_{S,F,t} = \rho \sqrt{h_{F,t} h_{S,t}} + \theta Z_{t-1}^2. \quad (2.15)$$

Overlooked in previous studies, the equation (2.15) provides an explicit link between the spread and the covariances of the spot and forward prices and is an important innovation from the authors. Indeed, according to the storage theory the cointegration relationship between the spot and forward prices loosens with a reduction in the amount stockpiled associated with a widening lag adjusted spread (i.e., $\theta < 0$).¹⁵ At full carry, Z_{t-1} is zero and $\rho \approx 1$ as the spot and futures prices are nearly perfectly correlated.

The system of equations (2.11)–(2.15) is estimated with the daily and three-month forward prices of four of the major industrial metals in addition to silver, a precious metal which might behave differently because of its safe-heaven status going hand-in-hand with large amount hoarded and thus a very small and stable spread. They also use the warehousing fees delivered by the London Metal Exchange, Ltd., as a proxy for the physical costs of carry k . Together, the results reported are very encouraging and confirm the predictions of the theory in many respects. Not only both spot and to a lesser extent forward-return volatilities significantly vary with the square of the adjusted spread (Z_{t-1}^2) (e.g., $\delta_3 > \phi_3 > 0$) but (i) Z_{t-1}^2 is inversely related to the correlations between spot and forward returns, (ii) the forward price elasticity defined as $e_t = \Delta \ln F_t / \Delta \ln S_t = \sigma_{S,F,t} / h_{S,t}$ falls with inventory drawdowns while approaching one at full carry, (iii) together the lagged-squared spreads account for between 50% to 70% and between 50% to 60%

¹⁴ In the empirical part the authors prefer the squared spread values instead of the absolute values specification since it offers a better fit without changing the qualitative results.

¹⁵ The link is even broken if the commodity is stocked out.

of the innovations in industrial metal spot-and-forward-return variances respectively, and unsurprisingly, (iv) statistically insignificant parameter estimates are found in the case of silver prices.

Working with the price of crude oil, Routledge et al. (2000) explore the implications of the storage mechanism in the behavior of the term structure of forward prices. In the basic set-up prices are driven by transitory demand shocks following a Markov process with two—high and low—states. After studying and illustrating the many consequences linked to the introduction of the storage arbitrage and the lower bound on inventories the authors turn to the data to see in which dimensions such a one factor model offers the best and the worst fit. Particular attention is paid to the slope of the forward curve whether increasing—known as contango—or decreasing—known as backwardation—with respect to the contract horizon. Intuitively, low incoming storage has less depressing effect on futures prices and so is associated with higher and more volatile spot and near term forward contracts. The reason for this is that such a backwardated market is more vulnerable to a positive demand shock causing a price peak and a stockout.¹⁶ The model is calibrated with the NYMEX crude oil daily futures prices. First, they fix to low values the constant decay and interest rates borrowing from the estimates reported by Deaton and Laroque (1992), and then select the values of the other parameters so as to match the mean and standard deviation of prices with and without conditioning on the shape of the forward curve a month prior. If the model can closely match the unconditional volatility, it fails to account for the conditional moments. One reason for this stems from a too little and not sufficiently volatile amount of stocks accumulated in backwardation. It turns out that the spot price is primarily driven by the transitory shock process, which is unable to generate a long-run volatility matching the observed conditional variations. The authors fix this issue by adding in the model a permanent demand shock assumed log-normally distributed. The idea is that inventories and transitory shocks only shape the front-end of the forward curves while the permanent component has the long-lasting effect which pins down the substantial volatility of futures observed in the longer horizon. The augmented model delivers a much better fit to the data and especially when forward prices are backwardated. Together, the very promising empirical results obtained from the literature of finance suggest that, in the competitive storage model with rational expectations, the forward-looking behavior of agents appears to be particularly suited to govern, at least in the short-run, the moves of forward prices. As a result, further empirical works can make the most of the substantial amount of valuable information taken from the futures prices.

A MIXED EMPIRICAL SUPPORT Together the empirical studies based on reduced-form versions of the competitive storage model come to mixed conclusions. That said, the rejection by the data of some aspects of the core theory of storage does not mean the latter is irrelevant for explaining the price fluctuations on the spot and futures commodity markets and some of the critiques deserve comments. First, it must be highlighted that to verify the validity of the storage theory most of the empirical strategies exploit the regime-switching behavior of the prices implied by the non-negativity constraint on stocks. But at the same time, for the most part the estimated threshold price P^* is such that stockouts are very infrequent, which means that only the few

¹⁶ Questions related to the shape of forward curves and the embedded information about the market fundamentals are further discussed in chapter 5.

observations located above P^* can serve to identify and test for the significance of the parameters in equations characterizing the stockout regime. Therefore, the evidences against the theory might well be due to the lack of power of the statistical tests employed rather than the failure of the theory in itself. This is even more true given the strong support to the theory provided by the finance literature where the greater amount of available data allow much more powerful testing procedures. Moreover, for some commodities the distinction drawn between those assumed storable which, in theory, should exhibit time-varying clusters of volatility and positive skewness and the other non-storable which should not is rather subjective, not obvious, and possibly questionable. Above all, the limited success of the tests clearly indicates that the speculative stockholding mechanism must not be the only driver of the price dynamics. For instance, the positive skewness can well be due to a government intervention defending a target floor price, to international commodity agreements as studied by Gilbert (1987, 1996) or else to the mechanical price rebound effect of a cut in the production part which became unsustainable below a certain price level. As there is an element of truth to all of them, this calls for working with a more elaborated storage model to determine which aspects of the core theory are the least supported by the data and in which directions models extensions should be done.

The point with such limited information estimation techniques, is that it left many key parameters unidentified, which precludes comparisons between the distribution of price series generated by the estimated model and the actual ones. A solution is thus to rely on the structural econometrics methods, a point to which we will turn now.

STRUCTURAL ESTIMATION TECHNIQUES

Structural estimation approaches push even further the reconciliation exercise between theory and observations by taking the structural model to the data directly, thereby providing a full characterization of the observed price series. The idea is to use the economic theory as a complement to the lack of data as stated in Varian (1989). Those empirical strategies are often less robust than their non-structural counterparts which is the common trade-off to be made between robustness and full identification of the parameters governing the behavior of prices. More specifically, they come at the cost of (i) taking a stand on the functional form of both the demand and storage cost functions, (ii) fixing some of the parameters that cannot be identified when inference is drawn from prices alone, and (iii) solving for the intractable price policy function needed to build the information-theoretic estimators.¹⁷ Worse still, the latter numerical resolution has to be done for every set of parameters in the maximization routine rendering the whole estimation procedure really computationally demanding.

THE METHODOLOGICAL BREAKTHROUGH All these challenges have been fixed in path-breaking papers of Deaton and Laroque (1995, 1996) aiming at dealing with the price autocorrelation puzzle raised in their

¹⁷ There is no closed-form solution for the price policy function which instead has to be numerically approximated. Gustafson (1958) pioneered the numerical techniques which then have been developed and grounded in the literature by Wright and Williams (1984), Williams and Wright (1991) before being thoroughly reviewed and even completed in Gouel (2013a). Lastly, in all the resolution methods the distribution of the stochastic process has to be approximated to get a problem of finite dimension.

previous article (Deaton and Laroque, 1992). Specifically, they assume a downward sloping linear demand for consumption $D(P) = (P - a)/b$, a physical storage cost proportional to the quantities in store and captured by the decay rate δ ,—i.e., $k = 0$ in equation (2.1)—a fixed interest rate $r = 5\%$ and an i.i.d. normally distributed supply process ε with mean μ and variance σ^2 . Moreover, given that the estimation relies on prices only, they demonstrate that it is not possible to uncover separately the demand parameters from those of the supply process. Hence, they assumed $\mu = 0$ and $\sigma^2 = 1$ so that ε is unit normal. Having laid out the general assumptions, they develop a structural estimation strategy based on the pseudo-maximum (log)-likelihood (PML), which falls in the class of the information-theoretic estimators.¹⁸ Here are the main elements.

First is to solve for the price policy function $\mathcal{P}(A; \theta)$ given the availability level A and the set of structural parameters stacked in $\theta \equiv (r, \delta, a, b)$. As needed in the numerical resolution, ε is approximated by a Gaussian quadrature with 10 equiprobable nodes.¹⁹ Then, recalling the time-dependency between prices induced by the storage channel and, still working with the thirteen price series taken from the World Bank dataset, they compute the first two conditional moments of P^{obs} , respectively denoted $M(P_t^{\text{obs}}; \theta)$ and $S(P_t^{\text{obs}}; \theta)$, entering the PML function and written as:

$$\begin{aligned} M(P_t^{\text{obs}}; \theta) &= E(P_{t+1}^{\text{obs}} | P_t^{\text{obs}}; \theta), \\ &= \sum_{n=1}^{N=10} \{\varepsilon_{t+1}^n + (1 - \delta) [\mathcal{P}^{-1}(P_t^{\text{obs}}; \theta) - D^{-1}(\mathcal{P}(A_t; \theta))]\} Pr(\varepsilon_{t+1}^n), \end{aligned} \quad (2.16)$$

and

$$\begin{aligned} S(P_t^{\text{obs}}; \theta) &= V(P_{t+1}^{\text{obs}} | P_t^{\text{obs}}; \theta), \\ &= \sum_{n=1}^{N=10} \{\varepsilon_{t+1}^n + (1 - \delta) [\mathcal{P}^{-1}(P_t^{\text{obs}}; \theta) - D^{-1}(\mathcal{P}(A_t; \theta))]\}^2 Pr(\varepsilon_{t+1}^n) - M(P_t^{\text{obs}})^2. \end{aligned} \quad (2.17)$$

where ε^n and $Pr(\varepsilon^n) = 0.1$ respectively stand for the nodes and their associated probabilities of the supply process discretization. $M(P_t^{\text{obs}}; \theta)$ and $S(P_t^{\text{obs}}; \theta)$ can finally be combined to form the PML($\theta; P_{1:T}^{\text{obs}}$) estimator:

$$\begin{aligned} \text{PML}(\theta; P_{1:T}^{\text{obs}}) &= -\frac{1}{2} \left(\left((T-1) \ln 2\pi - \sum_{t=1}^{T-1} \ln S(P_t^{\text{obs}}; \theta) \right) \right) - \\ &\quad \frac{1}{2} \left(\left(\sum_{t=1}^{T-1} \frac{(P_{t+1}^{\text{obs}} - M(P_t^{\text{obs}}; \theta))^2}{S(P_t^{\text{obs}}; \theta)} \right) \right). \end{aligned} \quad (2.18)$$

At the heart of the estimation procedure is the ability to recover the observed availability A^{obs} directly from P^{obs} by inverting the monotonously decreasing price policy function \mathcal{P} so that $A^{\text{obs}} = \mathcal{P}^{-1}(P_t^{\text{obs}})$. This imposed to solve for \mathcal{P} for each change in the value of θ . Hence, to uncover the parameters included in θ ,

¹⁸ Contrary to the full information maximum likelihood method, the PML abstracts from the third to higher moments of the price distribution, while keeping the consistency properties (Gourieroux et al., 1984). Put differently, unlike supply shocks, prices observations are not assumed normally distributed.

¹⁹ In their papers Deaton and Laroque propose a fixed-point algorithm which is, provided that the supply is assumed inelastic, not only very robust but also very fast. That is why it quickly became the standard method applied in most of the subsequent articles dealing with the structural estimations of the storage model.

the PML optimization routine needs to nest an inner numerical algorithm for the model resolution which, as mentioned above, makes the whole procedure computationally cumbersome.

The estimation results have been as disappointing as the approach truly innovative and inspiring since, then again, the model fails to induce more than half of the autocorrelation levels measured in the true data, regardless of the commodity under study. Put it another way, the transmission of shocks through the inventory channel accounts for only a small part of the story of commodity price variations on a market driven by i.i.d. fluctuations in production. Even more discouraging perhaps is the finding that a basic linear autoregressive model (AR(1)) does offer a better fit. Going ahead and borrowing from Chambers and Bailey (1996), the authors relax the assumption of an i.i.d. unit normal harvest shocks for one in which supply disturbances followed a mere AR(1) process, denoted z_t , thereby introducing an additional source of persistence in the model dynamics.²⁰ Looking beyond the theoretical plausibility of such a hypothesis, for instance in the case of annual crops like grains, in spite of this richer modeling, the conclusions remain widely pessimistic as stated by the authors themselves: “we find these results almost as disappointing as those for the storage model with i.i.d. harvests”. Indeed, the higher levels of serial correlations obtained are almost entirely resulting from the estimated value of ρ . All in all, the model cannot match the high degrees of serial correlation observed in the actual price data regardless of the assumed degree of persistence in the distribution of the supply innovations.

Still, with this methodology Deaton and Laroque definitely paved the way for future structural estimation of the competitive storage model. Moreover, as discussed above, in the same way as the lack of power of a statistical test can spuriously lead to reject the hypothesis of significant storage effects, the apparent autocorrelation failure does not necessarily mean rejecting the storage theory per se. As noted in Cafiero and Wright (2006), it rather has to do with the wrongness of part of the assumptions needed to be laid out: the functional form of the storage cost or linear demand functions (linear, convex, constant-elasticity), the absence of both supply reaction (production costs, capital dynamics) and demand shocks, the nature of the innovations (e.g., size, distribution, independence) and the fixed interest rate value among others.

Besides, such a sensitivity to the model hypotheses is even confirmed by the more optimistic results obtained from another stream of literature, initiated by Kaldor (1939) and Working (1949), and resting on the convenience yield hypothesis. The latter is seen as the flow of services accruing to the stockholders and is justified on the ground of timely deliveries and avoided costs either through a disruption in the manufacturing process or thanks to the trading advantage the owner of a commodity enjoys if the price spikes-up.²¹ The convenience yield prevents the occurrence of stockout situations which allows a much better fit of the measured autocorrelation (Miranda and Rui, 1999).

²⁰ The AR(1) process is written as $z_{t+1} = \rho z_t + \varepsilon_{t+1}$ with ρ the autocorrelation coefficient and ε a white noise with zero mean and unit variance. It is approximated by a Markov chain limited to the 10 nodes values of ε and in which the associated transition probabilities are calculated so as to match a predetermined ρ . Note also that z_t comes as a second state variable in the system which makes the estimation trickier as proved in the associated technical paper (Deaton and Laroque, 1995).

²¹ Technically, it is obtained by modeling the storage cost as a marginal log-linear function of the amount stored which becomes infinitely negative as the levels of inventories tend to zero. P^* being infinite the constraint is never binding. Another appeal of this approach is to easily permit the computation of the Maximum Likelihood estimator.

However, sticking to the assumption of the non-negativity constraint on inventories, Cafiero and Wright (2006) point to the direction of several theoretical and technical improvements to deal with this empirical failure.

TECHNICAL ACHIEVEMENTS Building upon the Deaton and Laroque (1996)'s PML, Cafiero et al. (2011b) demonstrate that a model with a constant marginal cost of storage which is solved with higher accuracy fits the behavior of prices better. Considering the carrying costs proportional to the amount stored is problematic since it makes stockholding increasingly expensive with prices. This in turn decreases the incentive to store which is the single source of time dependency of prices in the model. As a result, the authors suggest to set the decay rate of inventories δ to zero and estimate a constant marginal storage cost k instead. Also crucial is the precision in the numerical approximation of the price policy function given that a substantial part of inference relies on the accurate location of the kink at the cut-off price P^* above which there are no carryovers. Specifically, recalling that the lower P^* the more time in the stockout region and the less serial correlation generated by the model, an underestimation of P^* entails a reduction in the model ability to induce high levels of autocorrelation in prices.²²

Michaelides and Ng (2000) compare the asymptotic properties of the PML with three simulated estimators: the simulated methods of moments (Darrell Duffie, 1993), the efficient method of moments (Gallant and Tauchen, 1996) and the indirect inference estimator (Gourieroux et al., 1993). Developed in the 90's, these computationally intensive procedures of estimation aimed at providing alternative estimators able to uncover structural parameters of models for which there are no closed-form solutions. Through a series of Monte-Carlo experiments, the authors show that what the PML makes up on efficiency and precision in the sense of a smaller root mean squared error, it loses through larger estimation biases which are not decreasing with the sample size. More precisely, it leads to overstate the decay rate δ but also to an underestimation of the demand elasticity, the combination of the two translating into too frequent periods of zero stocks, reducing accordingly the ability of the model to generate autocorrelation in prices. For instance, with an annual deterioration rate of 16.9%, the estimation results for cotton imply that inventories are held only half of the time over the 1900–1987 considered sample interval, something clearly implausible.

With this in mind, Cafiero et al. (2015) come up with a full information maximum likelihood estimator (MLE) with better small sample performance properties and which, applied to the price of sugar, delivers a much more optimistic view of the empirical consistency of the storage model. Although more promising the results, trying to match the whole autocorrelation observed in the prices come at the cost of overstating the role of storage in the formation of prices. Hence, as noted in Cafiero and Wright (2006) and further explained in the next chapter, it might be the case that part of the serial correlation in commodity prices cannot be accounted for by the standard storage model.

The resolution of these numerical and specification issues, in yielding much more positive conclusions regarding the model ability to generate sufficient persistence in prices, decisively help to rekindle interests

²² According to the authors a number of points on the approximation grid in the range between 500 to 1000 appears to be sufficient as compared to the 20 to 45 points depending on the commodities used by Deaton and Laroque (1996).

in the competitive storage model and the underlying theory. Having said this, as will be shown in the next chapter, the higher autocorrelation levels can be obtained solely with very low values of demand elasticity and storage costs k . As a result, over the whole data sample spanning from 1900 to 1987 the estimated number of stockouts is very small if not zero. This is somewhat problematic given that the main appeal of the storage model is precisely its faculty of delivering two regimes of prices depending whether stocks are carried over. Together these results hint at exploring elsewhere than in the model specification and to look at the data themselves as also suggested in Cafiero and Wright (2006). The underlying logic is simply that part of the serial correlations in prices might have nothing to do with the storage theory and the associated transfer of inventories, or even more broadly to any kind of economic mechanism. It is just an artifact stemming from the way the series have been constructed and deflated. Thus, trying to fit this aspect of the price data is likely to come at the expense of the reliability of the whole estimation procedure. Better still, in such an empirical endeavor to test for the storage model consistency, issues related to the data are at least as important as those regarding the model specification itself.

EMPIRICAL REFINEMENTS Guerra et al. (2015) address the potential problem of spurious time dependencies due to the construction of yearly price series. Indeed, the data used thus far are a calendar averages of monthly prices, thereby mixing spot prices from two consecutive production cycles. Working with the MLE of Cafiero et al. (2015) on the price of corn over the period 1949–2012, they test for eight averaging methods to construct annual price indexes, and find to really sizeable effects across the studied samples. For instance, one of the key parameter estimates, namely the elasticity of demand for consumption, can vary by more than a factor of two if the annual index consists in a daily average over the November month rather than over the calendar year. On the whole they find that the best fit is obtained when using an annual value built as the daily average over the single month of December as in Roberts and Schlenker (2013).

The second major concern is actually very standard in econometrics as it revolves around the non-stationarity of the data.²³ Specifically, the commodity prices are likely to exhibit long-run trends. An illustration in the case of maize is given in figure 2.1. A long-run downward sloping trend is quite visible. Another point to note is the difference in magnitudes between the very wild short-run variations in prices with respect to the slow decreasing trend. In other words, the volatility supersedes the long-run trend, if any, along with all the movements of lower frequencies in general. The key challenge is thus to disentangle both components whether it is simply for testing data stationarity or when inferring parameter values. Going beyond this preliminary crude visual inspection with formal unit root tests, I follow the strategy presented in Ghoshray (2011) and conduct the Lee and Strazicich (2003) test which allow for shifts in the trend parameters under both the null and the alternative, so that the rejection of the null hypothesis necessarily implies trend stationarity. The results are reported in table 2.1.

As documented in the table, at a significance level of 10% or below, nine out of the thirteen commodities under study are found to be trend stationary with one or two structural breaks. These findings slightly differ from those reported by Ghoshray (2011) who runs the test on the same WB dataset but deflated by the

²³ I will contend with a short summary of the various stakes given that the next chapter is entirely dedicated to the related issues.

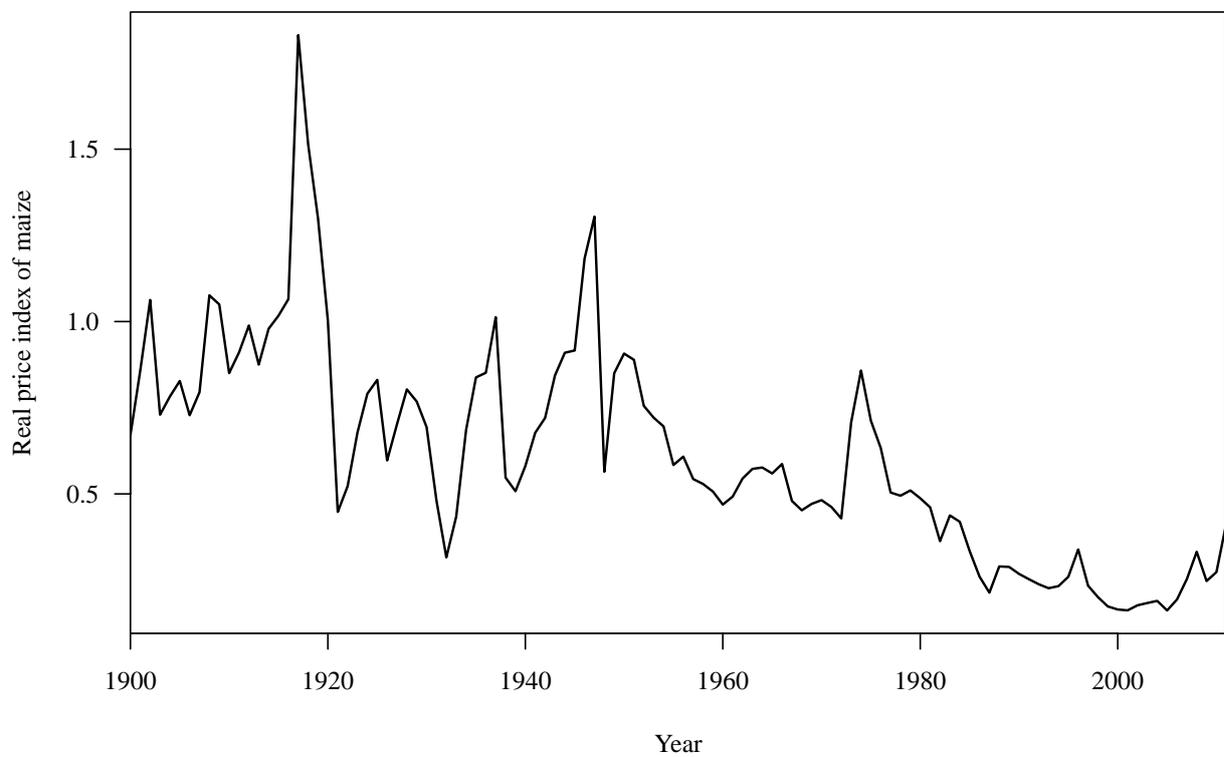


Figure 2.1. Annual real annual price index of maize (1900–2011). Source: World Bank Development Prospects Groups.

Notes: The data consist in the same series as initially used in Deaton and Laroque (1992) but consistently extended to 2011. Real indexes are obtained by normalizing the nominal prices with respect to the 1977–79 mean price before being deflated by the nominal price indexes by the US Consumer Price Index (CPI).

Table 2.1. Lee-Strazicich unit root test with structural breaks in intercept and slope

Commodity	k	TB1	TB2	t-stat
Banana	1	1941	1996	−6.994***
Cocoa	2	1946	–	−3.055
Coffee	2	1945	1987	−4.353
Copper	1	1917	–	−4.578**
Cotton	1	1928	1950	−7.228***
Jute	3	1927	1947	−5.648**
Maize	1	1916	1936	−5.497*
Palmoil	1	1983	–	−5.018**
Rice	7	1933	1982	−5.588*
Sugar	5	1919	1974	−5.412*
Tea	2	1934	1964	−5.114
Tin	11	1972	1988	−5.093
Wheat	3	1925	–	−5.394***

Note: ***, **, and * denote significance of the test at the 1%, 5%, and 10% levels respectively. k is the same lag length used by (Ghoshray, 2011, Table 3) when available or using the general-to-specific method as suggested in Lee and Strazicich (2003). TB1 and TB2 are the first and, if any, second break dates.

Manufactures Unit Value index (MUV) and on a shorter sample (e.g., 1900–2003), both elements likely to affect the results of the unit root tests. More precisely, the null of a unit root with breaks is rejected for jute and sugar but not for tin and tea while banana, and maize display a trend stationary process with two instead of one breaks. Furthermore, in line with the relative measures of the prevalence of a trend Ghoshray (2011, Table 6), the four commodities (coffee, cocoa, tea and tin) for which the price series are not trend stationary with breaks, are also those exhibiting trendless behavior for at least 50% of the sample. For the remaining nine, the author finds evidence for the presence of trend segments. Finally, it should be noticed that results vary across the commodities, (i) confirming the fact that there is actually a host of reasons that can be put forward to explain the presence of the trends and (ii) strengthening the relevance of working on an individual commodity basis rather than an index, and more so as the list of commodities includes both renewable with non-renewable commodities.

In light of these results, if most commodities are found to be trend stationary, it is by segments divided by infrequent shifts. With this in mind, in the upcoming chapter is provided a method to estimate jointly the structural parameters along with those of the trend. Introduced by Canova (2014), the hybrid method of trend and cycle decomposition of macroseries has the appeal of removing the influence of a trend but without restricting the model specification, while allowing different trend specifications to be tested and compared so that one can select the set-up which best fits the data. On the whole, accounting for a trend in the estimation procedure has a non-negligible impact on the demand elasticity and storage cost estimated values, both higher and closer to those published elsewhere in the literature (for e.g., in Roberts and Schlenker (2013)). This implies the occurrence of rare stockouts episodes in which the prices spike, thereby bolstering even more the empirical relevance of the competitive storage model.

THE COMPELLING EXOGENOUS EXPLANATION

All in all, no matter which type of econometric technique is employed (e.g., reduced-form or structural), the storage theory is favored by the data. Indeed, albeit pitfalls, more evidences is found for an exogenous source of prices fluctuations with a model in which the production/consumption decisions of rational agents with forward-looking expectations are subjected to random shifts. Of course, in view of the stark imbalance between both literature, it is tempting to evoke the “streetlight effect” in arguing that if the rational expectations model is favored it is mainly, if not only, for pure mathematical convenience, the research effort being ultimately allocated in the direction of least resistance. That would be forgetting a final but rather decisive observed fact which strongly opposed an endogenous story of the commodity prices dynamics: the stability gains belonging to more integrated markets and trade increase as documented among other in Jacks et al. (2011). Studying the long-run—e.g., more than three centuries—consequences of falling transportation costs and trade barriers on the price volatility of a variety of primary products taken individually, they unambiguously find smoother prices fluctuations during more trade-friendly periods and regardless of the frequency of the data chosen. Unlike the speculative storage model with rational expectations, the cobweb theory does not predict such a trade stabilization effect on prices.

In summary, it is safe to say that the storable property of many primary products is a key feature that should not be overlooked to understand the formation of commodity prices on the world market. However, although the speculative activity of stockholders generates a dynamics of prices consistent with the main stylized facts observed in the data, further extensions of the simple annual theoretical model are still needed to portray a more comprehensive picture of the behavior of commodity prices. The latest numerical and empirical developments definitely help improve the model fit, and more particularly the autocorrelation, thereby mitigating the initial deceptive conclusions of Deaton and Laroque (1996). The thing is that the elevated degrees of serial correlations in prices is not the sole puzzling phenomenon for which a coherent theory is missing. Chief among them is the excessive co-movements.

2.2.3 THE EXCESS CO-MOVEMENT PUZZLE

The expression comes from Pindyck and Rotemberg (1990) who show that commodity prices exhibit excessive covariations, even after having controlled for the main classical common macroeconomic drivers of the dynamics in the global commodity market.

The key in their approach is to consider not only the direct effects of these macroeconomic factors but also those indirect affecting the expected supply and demand conditions. The storage theory sits at the heart of the empirical strategy. Specifically, rearranging equation (2.1) they express, for a commodity i , the interest rate as a function of the expected and spot prices along with the carrying cost:

$$r_t = \frac{[E_t P_{i,t+1} - C_{i,t} - P_{i,t}]}{P_{i,t}}, \quad (2.19)$$

where $C_{i,t}$ is the period t cost of carry of the commodity including the constant physical storage cost k less the capitalized flow of its marginal convenience yield, which is a function of the level of inventories S as well

as current and past values of the macroeconomic variables which directly affect the market conditions and so the price. After some algebra starting from equation (2.19) they relate the change in the commodity price to the set of current and past values of macroeconomic variables and possibly to past price variations through the two following regression equations:

$$\Delta p_{i,t} = \sum_{k=0}^K \alpha_{i,k} \Delta x_{t-k} + \sum_{k=0}^K \beta_{i,k} \Delta z_{t-k} + \varepsilon_{i,t}, \quad (2.20)$$

$$\Delta p_{i,t} = \sum_{k=0}^K \alpha_{i,k} \Delta x_{t-k} + \sum_{k=0}^K \beta_{i,k} \Delta z_{t-k} + \rho_i \Delta p_{i,t-1} + \varepsilon_{i,t}, \quad (2.21)$$

where the vector x included the current and past values (up to the lag K) of the index of industrial production, the CPI, the nominal interest rate on the 3-month Treasury bills, an equally-weighted index of the dollar value of the German marks, Japanese Yen, and the British pounds and z embeds the money supply and the S & P common stock index, while ε is the error term assumed normally distributed and serially uncorrelated in (2.20) but not in (2.21).

Finally, under the null of absence of excess co-movements across commodities, $E(\varepsilon_{i,t} \varepsilon_{j,t}) = 0 \forall i \neq j$, that is after having controlled for the past, current and expected effects of the primary common macrodeterminants, there should not remain any systematic and predictable correlations in the residuals. Put simply, under the null any correlations in the error structure are assumed insignificant and purely fortuitous. They estimate the equations (2.20) and (2.21) by Ordinary Least Squares (OLS) working with the 1960–1985 monthly, quarterly and annual series of the US cash price of seven commodities—crude oil, gold, lumber, copper, cocoa, cotton and wheat—and test for the excess co-movements hypothesis using the likelihood ratio statistic. For all commodities and at all frequency, they reject the null of no excessive co-movements across commodities. In an attempt to assess the magnitudes of the marginal explanatory power of this excess of co-movements they look at the R^2 values of the OLS regressions and find that a large share—e.g., up to one half in the case of cotton—of the variances in commodity price changes is actually explained by these excessive contemporaneous variations.

Before finding to a definitive refutation of the canonical speculative storage model the authors deem it appropriate to qualify somewhat the extent of their findings on the ground of three weaknesses. The first one is purely statistical and rests on the normality assumption of the regressions residuals, likely to be violated by the well documented fat-right tails exhibited in the commodity prices fluctuations. Thus, this threatens the validity of the procedure and in the end might lead to a spurious rejection of the null hypothesis. In any event, tackling such a technical issue is of poor help given the final objective of improving the empirical relevance of the standard storage model. Like the authors I will not pursue further down this road. The second weakness has to do with one of the authors' assumption stating that none of these commodities can be seen as an important input for production of the others, thereby washing out the possibility of cointegration relationships among them. Admittedly, given the macroeconomic importance of the oil price, which for instance represents a substantial share of agricultural production costs, whether directly (fuel) or indirectly (chemical inputs such

as fertilizers), it is hard to deny its influence on the other primary products, and maybe even more today in view of the growing importance of biofuels in the global energy mix.²⁴ Still, among the set of commodities included in the analysis, crude oil price is the only one with such a macroeconomic status and it would be dubious if, by itself, it can account for the lion's share of the significant excessive co-movements measured in the data. Finally, the last caveat is really common in econometrics since, reminding that correlation is not causation, one cannot rule out the possibility that one or several omitted variables ultimately govern the observed covariances between the commodity prices. Then again, the variety of factors embedded in the x and z vectors covered a fairly broad spectrum of the macroeconomic environment, so that it is not worth the effort to embark into the quest for such prominent omitted variables able to overturn the authors' conclusions. Not to mention the many associated sensitivity analyses confirming the robustness of the core results.

In summary, on the one hand none of the above three shortcomings, even pulled all together, seems to be in a position to relegate such a puzzling phenomenon as a spurious finding or else a simple artifact of the data not to be taken seriously. All the more since the commodities are not the only class of assets whose prices tend to exhibit excessive co-movements as suggested in Pindyck and Rotemberg (1993) in the case of stocks returns and, more broadly, by the phenomenon of contagion in financial markets described and analyzed in detailed in Kaminsky et al. (2003). On the other hand, as with the no less enigmatic autocorrelation discussed above, acknowledging the presence of excessive co-movements across commodity prices does not mean completely throwing out the microfoundations of the speculative storage model and the associated rational expectations hypothesis. For instance, Veldkamp (2006) shows that if the acquisition of information is costly, excessive correlations across the earnings of unrelated stocks can well arise as a rational outcome.

In any case, what cannot be disputed is that attempting to solve these puzzles clearly call for extending the storage model so as to include some market frictions and widen the scope of the structural explanations of the behavior of commodity prices. As studied in the next section, given the current estimated specification of the storage model, the interest rate could be the key variable for taking into account these macroeconomic spillovers.

2.3 THE INTEREST RATE CHANNEL

So far, in all the empirical studies the competitive storage model consists in a single non-linear Euler equation in which the interest rate enters as a simple discount factor assumed exogenous and fixed. The latter hypothesis, in leading the modeling to abstract totally from the global economic environment, might well be another misspecification of the model hampering its empirical performance. Indeed, dealing with the macroeconomic forces driving the dynamics of commodity prices requires consideration of the general equilibrium effects. Put differently, the commodity market cannot be isolated from the other markets such as the forward, money and stock markets. To study the relationships across these different markets, it is safe to say that particular attention has to be paid to the interest rate. According to Frankel (2014), there four main channels through which, say, a higher interest rate might affect and lower commodity prices:

²⁴ See the recent textbook of de Gorter et al. (2015) for more on this burning issue.

1. a selling of inventories in response to the more costly storage activity;
2. an incentive to raise current production following the logic of the Hotelling's principle;
3. a change in the flow of portfolio investment from the basic products into the Treasury bills;
4. an appreciation of the domestic currency leading to a decrease in the dollar denominated commodities on the world market.

Each of these explanations are backed by theoretical developments which gave birth to specific strands of literature. If there is certainly an element of truth to all of them, some are better supported by the data. Furthermore, it is hard to deny the likely existence of close connections between them. For example, the portfolio shift out of the commodity sector goes hand-in-hand with the domestic currency appreciation. Therefore, all the econometric challenge lies in teasing-out the own contribution of each channel into the overall variations of commodity prices. Apart from the rather intuitive and direct storage cost canal which has already received extensive consideration, I will attempt to pick, discuss and assess both the theoretical and empirical relevance of some of the economic mechanisms underlying the indirect effects of the interest rate embodied by the other three channels. In the end, the aim is to build upon the competitive storage model by painting a rough and rapid overview of some of the key macroeconomic linkages which possibly could help to remedy both the autocorrelation and excess co-movements puzzles. Hopefully, doing this will improve the explanatory power of the model, while keeping the storage theory at the center of the stage.

2.3.1 THE LATENT HOTELLING'S RULE

On the supply front, reckoning that until now only the mere inelastic version of the storage model has been brought to the data, the "Hotelling's rule" stating that the marginal value of an exhaustible resource should grow at the rate of interest, is an appealing extension of the model albeit only meaningful for nonrenewable resources. The point is that it thus far has been deeply rejected by the observed data (Krautkraemer, 1998). One reason for this is that a higher interest rate is also associated with an increase in the capital cost, reducing the rate of extraction and so the supply which, in turn, causes the price to rise. In the end it is unclear whether an increase in the rate of interest eventually leads to raise or decrease the commodity price. In fact, everything depends upon the "in situ" value—e.g., the difference between the price and the marginal extraction cost—of the resource which is itself inversely related to the amount of reserves underground. This is why a more fruitful extension perhaps would be to incorporate, in the basic storage framework, the effects of the dynamics of investment and capital accumulation known to be particularly costly in capital intensive industries. The last chapter of this thesis precisely deals with the interactions between investment and storage, and demonstrates that the addition of such supply constraints in the system has material consequences on the price behavior implied by the model. Nevertheless, as speculated in Hamilton (2009), the Hotelling's notion of scarcity rent raising at the rate of interest might well become more relevant in the years to come with the depletion of the resource.

In the meantime, in light of the many possible explanations for the current empirical failure of the Hotelling's principle, I will not enter further into the details of why the prices of exhaustible resources have tended to deviate from the optimal price path which would have emerged if the theory were to hold.²⁵ Instead, it is fair to assume that, so far, this channel has not been essential in the behavior of commodity prices and better insights could be gained by investigating the exchange rate and monetary policy channels.

2.3.2 THE EXCHANGE RATE PASS-THROUGH

To begin with, I would like to provide a brief historical background explaining the growing importance of the macroeconomic environment in the dynamics of commodity prices. In the wake of the break down of the Bretton Woods monetary system and the resulting liberalization of capital and monetary markets, monetary policy, interest rate and exchange rate have found themselves bound by the Mundell-Fleming trilemma. Since then, interest and exchange rates are intrinsically linked within a political debate in international macroeconomics fully polarized around the three corners of such an inconsistent trinity. Let me quickly illustrate the way the mechanics operate with a country pegging its currency to the US dollar and not imposing any capital controls. If, say, the US Federal Reserve raises its policy interest rate, the central bank of the country which currency is pegged to the US dollar lost its autonomy and has to follow. Otherwise, the resulting negative interest rates differential will entail a capital outflow towards the higher returns offered in the US and, in turn, the local currency depreciation which eventually would break the peg with the US dollar.

A LARGE BODY OF DEDICATED LITERATURE To illuminate the various monetary, fiscal and trade policy discussions, a huge literature emerged to assess the pass-through of exchange rates into commodity prices, the consequences in terms of exports/imports volumes and, more broadly, the interdependence between the financial (e.g., stocks, bonds, exchange rates), the money and commodity markets. Specifically, most of the work in this field aims at testing the empirical validity of related theories such as the Law of One Price (LOP), the Purchasing Power Parity (PPP), the Uncovered Interest Parity (UIP) or the rational expectations present-value model. At first is the seminal contribution of Ridler and Yandle (1972) who depict a single-commodity analytical framework to understand the effects of exchange rates variations on the price of an individual primary product. This work have then been followed by studies included Schuh (1974), Chambers and Just (1979, 1982) and Jabara and Schwartz (1987) mainly focused on the agricultural products. Finally, the field of investigation spread to other commodities and sectors with contributions from Gilbert (1989), Cashin and McDermott (2002) and Engel and West (2005) among others.

The overall conclusions drawn are mixed. If to very rare exceptions they all agree to sizable effects of monetary policy and exchange rates on commodity prices, this is absolutely not the case when it comes to assess the relative magnitudes of these impacts, in particular in terms of estimated elasticities. Moreover, most of the time the model's predictions are rejected. In fact, the main reasons for these empirical failures are

²⁵ Krautkraemer (1998) provides an extensive and thorough overview of these factors which basically have to do not only with violations from the efficient market hypotheses among which are imperfect competition, incomplete markets, externalities, but also with the discovery of new deposits, the technological progress and the lack of data availability which makes any empirical analyses even more complicated.

very similar to those leading to reject the storage theory and underlined earlier: the wild fluctuations in both the observed exchange rate and commodity prices render really challenging any attempts to clearly uncover the causalities between the variables so as to obtain precise estimates in such an unstable environment.

A good summary is provided in Chen et al. (2010) who attempt to address these major empirical caveats of endogeneity and stationarity in relying on the concept of “commodity currency” exchange rates.²⁶ More precisely, concentrating on five small commodity-exporting countries—i.e., Australia, Canada, Chile, New-Zealand and South-Africa—with floating exchange rates regimes, they embark in an in-depth empirical analysis of the dynamic relationships between global commodity prices and exchange rates. They circumvent the endogeneity problem inherent to all macroeconometric studies in working with a country-specific world commodity price index whose dynamics can be reasonably assumed exogenous to those of the exchange rates of such small open-economies.²⁷ Regarding the stationarity concern related to possible structural shifts in parameter values, it is alleviated in implementing the Granger causality test developed by Rossi (2005) which, in allowing for structural breaks in the series, has proved to be robust to time-varying parameters. In the end, they uncover a significant causal relationship, both in-sample and out-of-sample, running from the exchange rates to the world commodity prices. Interestingly too is the finding that exchanges rates are better in forecasting world commodity prices than the random walk with or without drift as well as the first-order autoregressive specification which have been tested for comparison. According to the authors, this forecasting power of exchanges rates can be explained by the very forward-looking nature of these variables which encompass more information about the future macroeconomic conditions than what could be brought by the others factors—e.g., output, monetary aggregate, stock market indexes—commonly introduced in the times series regressions. Finally, they complement their analysis with a battery of robustness checks. For instance, in obtaining similar results with the British pound instead of the US dollar, they show that the causality uncovered is not a “dollar effect” consequence of two variables originally priced in US dollars.

All in all, the results of this study bring yet an additional evidence not only of the great influence of the exchange rates on the behavior of global commodity prices, but also of their wide informative content about the macroeconomic environment. There can be no doubt that it is a really good candidate for raising the explanatory power of the commodity storage model. In my view, and from a purely speculative standpoint, there are actually two avenues for incorporating the exchanges rates dynamics in the structural estimation of the competitive storage model: one is exogenous while the other is endogenous.

THE DEMAND SHOCK APPROACH In this first empirical strategy, the idea consists in considering that the monetary policy and all factors affecting the exchange rate are determined outside the commodity market model so that it can enter the model with a reduced-form specification such as a basic AR(1). Another way of saying that is to assume that the exchange rate is simply a sort of “manna from heaven” aggregating the information about the macroeconomic environment and shifting the equilibrium price implied by the model, like a long-lived demand shock in some sense.

²⁶ The concept refers to the free-floating currencies of countries whose export revenues heavily depend on commodity exports.

²⁷ They test for potential endogeneity with an Hausmann Test. The null of exogeneity is accepted at the standard statistical levels.

For this to be done, imagine a perpetual net-exporting country of a given commodity, say Saudi-Arabia with crude oil, selling its product to another in perpetual deficit, say the rest of the world. Under this assumption the supply shocks do not impact the trade direction. As a result, everything goes as if both countries equally shared the risk inherent to the uncertainty in the realized production, since any supply disruption only affects the global amount on hand A , the unique state variable governing the commodity price. Add to this one-way trade and perfectly risk-sharing situation the fact that, to save on trade expenses a net-importing country never stores, and the storage and trade model described in Williams and Wright (1991, Ch. 9) collapses into its standard version with a single country. Then, provided zero tariffs barriers and borrowing from Chen et al. (2010) the concept of commodity currencies, there is a case for translating the producer commodity price in the US dollars denominated international price according to the following relationship:

$$P_t = \frac{(\tilde{P}_t - \theta)}{\tau_t} \quad (2.22)$$

where θ is the trade cost expressed in the domestic currency (the Saudi Arabian Riyal in the above example), P and \tilde{P} stand for the US dollar international and domestic prices respectively, while τ is the exchange rate defined as the US dollar price of the domestic currency.

However, this “ad-hoc” statistical approach, although quite fast and easy to implement given that it only adds one exogenous state variable (τ) to the system, does not seem able to resolve the excessive correlations puzzle. Indeed, introducing an autocorrelated exchange rate variable is nothing but having an additional persistent shock exactly like Deaton and Laroque (1996), but on the demand side this time. Simply put, modeled this way the exchange rate enters the model in a similar fashion as a negative persistent supply shock, with admittedly a more universal and convincing economic justification than its autocorrelated supply shocks counterpart, but still identical in nature. Thus, there are good reasons to expect the estimation results to be as discouraging as those published in Deaton and Laroque (1996), namely that the model will manage to fit the serial correlation in prices but at the expense of attributing all the persistence to the autocorrelation coefficient of the exchange rate. Further, since the measured excessive covariations in commodity prices typically refers to those detected once having controlled for the exchange rates fluctuations, it does not provide an answer at all to the excess of co-movements phenomenon.

In summary, if the unique objective is to improve the fitting performance of the storage model, then such a model’s repair seems enough to yield satisfactory results notably in terms of induced serial correlations in prices. Otherwise, to actually tackle the excess of covariances puzzle, there is a need for a richer storage model specification allowing for cross-price elasticity effects between commodities and all kinds of interconnections, feedbacks along with other linkages existing among the main macroeconomic variables of interests. The latter only, in conveying the variety of international shocks within the structural system of equations, hopefully can lead the model to deliver nontrivial patterns in the behavior of commodity prices, that is going beyond the predictions based on the fundamentals alone.²⁸ Therefore, to extend and deepen the

²⁸ In this spirit, the Pavlova and Rigobon (2007)’s model, albeit developed in a continuous time context, is very instructive about the potentiality of generating assets prices co-movements similar to those observed through the inclusion of an additional terms of trade channel in an otherwise standard international asset pricing set-up.

understanding of the structural mechanisms at stakes and the directions in which the causality are running, there is no alternative but to augment the storage model system of equations with an additional theoretical monetary-based characterization, even very crude, which features the determination of the exchange rate. One such theoretical framework is the model of Frankel (1986) which formalizes the theory behind the overshooting phenomenon, a point to which I will turn now.

2.3.3 THE OVERSHOOTING THEORY

A typical illustration of what is meant by “non-trivial” patterns in the behavior of commodity prices is certainly the overshooting concept. The core logic is completely analogous to the one embedded in the famous overshooting model originally proposed by Dornbusch (1976) for the exchange rates. It has then been imported in the field of commodity prices by Frankel and Hardouvelis (1985) and Frankel (1986) as a way to feature the interdependence between the financial, money and commodity markets so as to study the influences of the monetary policy on the dynamics of commodity prices. The key underlying assumption is that, in response to a shift in the money supply, commodity prices adjust more rapidly than prices of manufactured goods as has been empirically demonstrated in Bordo (1980). Reminding the storage arbitrage condition on the expected rate of return of commodities prevailing in the commodity market, the higher interest rate entails a fall in spot prices. However, given the stickiness of the other prices, the commodity spot price will overshoot its expected long run equilibrium level where the general price level—e.g., consisting in both the prices of primary and manufactured goods—has fully adjusted to the change in the money supply. In other words, commodity prices will decline by more than proportionately to the drop in the money supply so as to be sufficiently undervalued to offset the higher real interest rate. Hence, the expected increase in commodity price covers the rise of the real rate of interest and induces market participants to hold inventories.

In a attempt to quantify the short-run effects subsequent to a monetary shock, Frankel (1986) combines a money demand equation with an expectation-augmented Philips curve and the storage trade-off condition, to derive the following relationship (keeping Frankel’s notations):

$$\Delta p_c = \frac{1 + \lambda \theta}{1 - \alpha + \lambda \theta} \Delta m + \lambda \frac{1 + \lambda \theta}{1 - \alpha + \lambda \theta} \Delta \mu; \quad (2.23)$$

where m is the log of money supply, p_c^e and p_m denote the logarithm of the expected commodity and manufactured prices respectively, λ is the semi-elasticity of money demand with respect to the interest rate, θ stands for the speed of adjustment in manufactured good markets, and μ is the secular expected rate of inflation. Since the coefficient of Δm is greater than one, the commodity prices will tend to overreact following a variation in the supply of money. The latter degree of overshooting is inversely related to the value of θ : the higher θ , the less the commodity spot price overshoots its long term value.²⁹

From an empirical standpoint, the literature seeking to test the overshooting theory applied in the context of commodity prices is much thinner than the one focused on the exchange rates and, as far as I know, all of

²⁹ In the limit of an infinite θ , both commodity and manufactured goods prices instantly converged to their long-term values, the coefficient of Δm tends to unity and there is no overshooting.

them are reduced-form approaches. One of them is offered by Browne and Cronin (2010).³⁰ Specifically, using US data they apply the maximum likelihood cointegration procedure developed in Johansen (1988) to test for the presence of the long-run dynamic relationships money, commodity and consumer prices as posited by the theory. Embedding in a four vector autoregressive (VAR) framework with six lags, the money stock measured by the M2 aggregate, a measure of the real GDP, the CPI, and an index of commodity prices (three different indexes are tested), they implement the Johansen's trace statistic test and uncover, at either 5% or 10% levels of significance depending on the commodity price index considered, two significant cointegrating vectors between the money stock and both the consumer and commodity price indexes.³¹ Using the estimated cointegrating relationships, the empirical analysis is finally supplemented by Impulse Response Functions (IRFs) plots of the variables included in the system following a money supply shock. On the whole, the adjustments profiles side with the theory, with the commodity price index overshooting its long-term equilibrium level while the CPI does not. Together these results are encouraging and shed light on the empirical relevance of the overshooting theory. Still, as mentioned by the authors themselves, their findings in support of the overshooting theory have been obtained through a reduced form model, and thus cannot be given any structural interpretation. All that can be said is that the predictions derived from the theory are not at odds with the observed data.

To conclude, the overshooting theory is really attractive as it seems able to provide a theoretical explanation to both the autocorrelation and the excess co-movements puzzles, while staying consistent with the rational expectations foundations of the canonical storage model. At this juncture, the only fly in the ointment comes from the always tricky stage of bridging the theoretical model to the data. Hence, it should come as no surprise if, in spite of three decades of existence, there is an overall lack of empirical studies and particularly of structural econometric works attempting to test the validity of the overshooting theory. Part of the reason has to do with the so called "curse of dimensionality". Indeed, as appealing and relevant as it looks like, the integration of such monetary and macroeconomic effects within the core system of equations of the storage model inevitably leads to an increase in the number of state variables. The thing is that, as demonstrated in Gouel (2013a), the competitive storage model is too nonlinear to be solved with the perturbations methods and the more numerical intensive projection techniques have to be employed instead.³² Add to that the estimator optimization step and you get the perfect recipe for an explosion in the computational time needed to complete the whole structural estimation procedure. All in all, addressing all these numerical and empirical challenges is worth pursuing but very time-consuming. It turns that in the near future one has to content with ad-hoc repairs to the competitive storage model which help improve the model fit even though less microfounded.³³ That said, the overshooting story is fairly close to be incorporated in the storage model structure as it provides a rational explanation to the puzzling persistence and excessive

³⁰ See also Saghaian et al. (2002) and Ching-chong et al. (2005) in the case of agriculture prices.

³¹ The VAR is estimated assuming neither intercepts nor trends in the cointegrating vectors while the lag length has been chosen according to the Akaike information criteria.

³² They are even more computationally burdensome if you recall that the grid of approximation has to be fine enough for the price policy function approximated with a satisfactory level of precision (Cafiero et al., 2011b).

³³ The alternative would be relaxing the non-negativity constraint on inventories following the convenience yield tradition.

covariances in observed prices, with both a long established theoretical bedrock and a solid body of empirical evidences.

2.4 THE OUTLOOK

In this chapter I surveyed a variety of theoretical along with empirical developments designed to provide a structure to the analysis of commodity price volatility in the world market. This literature review helps to isolate some key features to be considered for a sound understanding and prediction of the observed fluctuations of prices which would prove to be helpful for informing the policy debate.

In this respect the commodity storage model with rational expectations deserves particular interest. In its basic version, it consists in a single intertemporal storage Euler equation derived from the optimizing behavior of speculators. Such very transparent microfoundations is not its unique asset compared to the opposed way of modeling the behavior of commodity prices and embodied in the cobweb-type models. Indeed, when it comes to assess their respective quantitative merits, on the whole the literature is more supportive of a price behavior driven by the market fundamentals affected by unexpected and exogenous shocks. From the external consistency standpoint, the superiority of the storage model has even been bolstered over the past decade following the many important contributions achieved to address the autocorrelation puzzle along with the other model's empirical failures highlighted in Cafiero and Wright (2006). That said, as the short-run volatility can also result of market exuberance, panics and irrationality, the cobweb-type models and the complex price dynamics they can generate are still worth of existence, even though not at the center of the political debate since, ultimately, the price reverts back to the reality dictated by the fundamentals of supply, demand and inventories.

This is why the storage model is a good place to start thinking about commodity price volatility in offering a common and mere core structure around which to build and organize policy discussions. In some sense, it should be the architecture in which the relevant findings from the various fields of finance and economics are eventually integrated, so as to improve its explanatory power and, hopefully, attempt to provide answers to some of the current puzzling phenomenon included the persistence and the excess of co-movements in prices.

Still, to this point, it has to be noted that, so far, all the structural estimations of the storage model rest on price information alone, which highly limit the number of parameters that can be freely identified. This is the main reason why reasoning from a price change is of poor help when it comes to go further in the empirical analysis with richer storage model specifications. Therefore, it is paramount in futures inference of the storage model to draw information from both data on prices and quantities, above all now that they begin to be available over a sufficiently long period of time.³⁴ It is only thereafter that it will be possible to draw reliable conclusions about the relative empirical merits of the storage theory. Moreover, confronting the storage model with observed data on both prices and quantities will allow to assess in which dimensions the model does and does not perform well.

³⁴ Chapter 3 precisely tackles the challenges inherent to the structural estimations of the storage model using information on prices and quantities.

In summary, and in a pure speculative manner, a promising and realistic research agenda covering all times frames could go like this:

ECLECTIC STORAGE MODELS in the short-run in the absence of sound theoretical microfoundations to rely on and/or in waiting for the computational advances needed to cope with the current numerical issues, especially those related to the curse of dimensionality discussed above. Put differently, the objective is to improve the overall model fitting performance by embedding reduced form specification within the structural estimation procedure to capture aspects of the data that have nothing to do with the storage theory. One such example is the treatment of the long-run trends in commodity prices and is precisely the topic of the next chapter.

MACROECONOMIC STORAGE MODELS in the medium-run to gradually incorporate macroeconomic forces in a structural fashion for instance through the interest rate channel. The goal here is, without loosing any explanatory power, to strengthen the internal consistency of the model by attempting to have as much as possible theoretically grounded relationships across the variables in the framework. In this respect, ideally the interdependence between the monetary policy and the commodity prices is endogenously derived in an overshooting-type model, instead of intervening as a mere persistent demand shock imitating the broader macroeconomic environment encapsulated in the exchange rate.

FINANCIALIZED STORAGE MODELS in the long-run to generate even richer patterns of co-movements among commodity and assets prices. The idea is to acknowledge for spillovers effects stemming from the financial markets flowing into the physical commodity markets, and eventually have a story for potential speculative bubbles, self-fulfilling prophecies and other irrational behaviors of this kind. From this perspective, the burgeoning literature on the integration of financial frictions within stochastic dynamic equilibrium models like the competitive storage model is promising and worth of consideration. Having said this, to avoid ending with a black-box model, it might be wiser to develop different versions of the storage model suitable for applications under a variety of circumstances.

CHAPTER 3

ESTIMATING THE COMPETITIVE STORAGE MODEL WITH TRENDING COMMODITY PRICES

Gustafson's (1958) commodity storage model is fundamental for explaining the annual behavior of commodity prices. It features forward-looking speculators that maximize profit by stockpiling a commodity based on the difference between the expected price and the current price. The source of volatility in the commodity storage model is the occurrence of unexpected supply shocks. The model has proven capable of reproducing many features of commodity prices such as sharp spikes, volatility clustering, positive skewness, and excess kurtosis (Deaton and Laroque, 1992). However, in early estimations of this model, Deaton and Laroque (1992, 1996) show that it could not explain the high degree of serial correlation observed in the price series. This finding was challenged. Cafiero et al. (2011b) show that using a finer grid to approximate the policy function and a different model specification, the storage model is able to generate the observed serial correlation for seven of the twelve commodities analyzed in Deaton and Laroque (1996). Since Cafiero et al. (2011b), several papers provide positive evidence for the role of storage arbitrage in price behavior (Bobenrieth et al., 2013, 2014, Cafiero et al., 2015, Guerra et al., 2015). However, if the model is estimated on untransformed real price indexes (as in Cafiero et al., 2011b), discretionary stocks are always strictly positive (i.e., there are no "stockouts") for most commodities over the sample interval. This result casts doubt on the appropriateness of using for estimation a nonlinear model with two regimes (with and without stocks) if, over long samples and for most commodities, the estimations imply that only one regime is active.

The absence of predicted stockouts in the sample indicates a possible model misspecification. This misspecification may arise from the attempt to fit with the storage model a serial correlation that is artificially high, due to a possible non-stationarity in the price series. Commodity prices are unlikely to be stationary over long periods. Starting with the work by Prebisch (1950) and Singer (1950), a large literature has been devoted to characterizing the nature of this non-stationarity: whether trends are stochastic or deterministic, the existence of long-run cycles, or secular decline of commodity prices relative to those of manufactures (e.g., Grilli and Yang, 1988, Cashin and McDermott, 2002, Ghoshray, 2011, Harvey et al., 2010). As illustrated in figure 3.1, the nature of the trends (or their absence) tends to be specific to each commodity

(e.g., mostly trendless behavior after a decreasing interval for copper, hump-shape behavior for cotton, monotonically decreasing for rice). Removing the trends using an Hodrick-Prescott filter reduces the one-year autocorrelation in commodity prices by one-third from about 0.85 to 0.5 (see table 3.11 in the appendix). We show in the next section that to generate with the storage model an autocorrelation in prices as high as 0.85 requires extreme parameter values, corresponding to very low storage costs along with very inelastic demand thereby implying extremely rare stockouts, while a smaller autocorrelation is compatible with more plausible parameters and occasional stockouts. Low storage costs are needed to match a high autocorrelation because they ensure there are always stocks to connect one period to the next. So estimating the storage model, which features prices converging to a stationary distribution, with untransformed prices (as in Deaton and Laroque, 1992, 1996, Cafiero et al., 2011b) is likely to lead to biased parameter estimates if prices are non-stationary. The present chapter assesses the role of potential non-stationary price series in estimations of the storage model, and proposes an approach that statistically accounts for a trend in the price series.

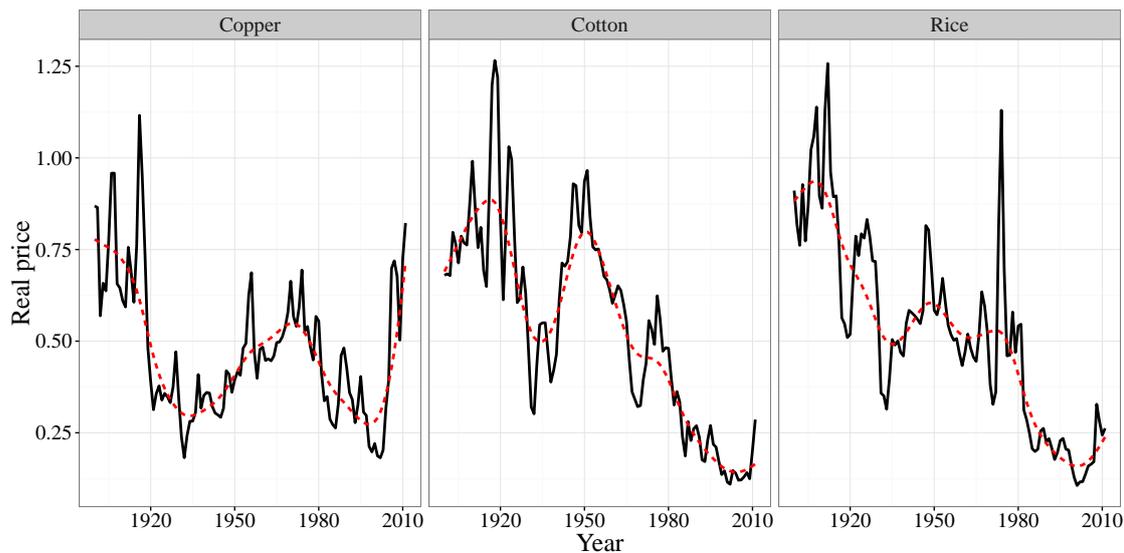


Figure 3.1. Real prices and Hodrick-Prescott trend (smoothing parameter 400)

How to estimate dynamic stochastic rational expectations models that are defined to be stationary around a steady state using non-stationary data is a very important question in the related literature on the estimation of DSGE models. In a recent paper, Canova (2014) summarizes the various strategies used in this literature. Most apply also to the storage model. Most DSGE models are estimated on transformed data in two steps. First, a statistical filter (linear detrending, first-order differencing, Hodrick-Prescott or band-pass filters) is applied to the raw data, then the structural model is estimated using the transformed data. This approach is convenient but is known to involve problems. The business cycle facts will depend on the choice of filter which is arbitrary (Harvey and Jaeger, 1993, Canova, 1998), due to lack of formal tests to select the most appropriate trend specification. For the storage model, the two-step approach is applied in Cafiero et al. (2011a), Bobenrieth et al. (2013), and Guerra et al. (2015) where prices are detrended ex-ante using a log-linear trend.

Another approach involves the construction of a model that includes transitory and permanent shocks, the latter aimed at capturing non-cyclical fluctuations. The model is made stationary by scaling the variables by the permanent shocks, and is fitted to the raw data. This approach has the appeal of theoretical consistency but introduces the risk of misspecification. Because it is not possible to make every model stationary for all possible specifications of permanent shocks, the model design and the nature of the shocks may be driven more by computational than economic motives. This approach is applied in Zeng (2012) and Bobenrieth et al. (2014) with storage models in which storers internalize the downward trend in commodity prices and adjust their behavior accordingly, and in Dvir and Rogoff (2014) where quantities are non-stationary, but not prices. However, to obtain stationary equations while accounting for a trend in prices, various restrictions must be satisfied: the trend must be multiplicative and the logarithm of the trend is restricted to take the form of a random walk with drift; the demand function has to be isoelastic, but not linear as commonly adopted for numerical simplicity; and storage costs must either be zero or have the same trend as prices.

Canova (2014) proposes an alternative method to estimate DSGE models using raw data.¹ In this approach, the econometrician defines a statistical model which is a combination of a DSGE and a reduced-form model; the reduced-form is aimed at capturing the component in the data that the structural model is unable to explain. This statistical model can be estimated using raw data, which leads to joint estimation of the structural and reduced-form parameters. Interestingly, this one-step approach allows to select the most likely trend specification based on a statistical criterion for model selection. Furthermore, it presents the benefit of not restricting the trend and model specifications, but at the cost of the agents neglecting the trends in their decisions.

The choice between the approaches amounts to a trade-off between theory and empirics. If the conditions under which a storage model can be made stationary are too restrictive with respect to the prevailing trends, it may not be possible to properly capture them in the model. The most severe restriction for a storage model with trending prices is probably that the trend has to be the exponential of a random walk with drift, possibly collapsing to a simple linear trend if the random walk step has zero length. It is unlikely to be satisfied for most commodities. In the literature on long-run trends in commodity prices, a consensus has emerged (Kellard and Wohar, 2006, Balagtas and Holt, 2009, Harvey et al., 2010, Ghoshray, 2011, Cuddington and Nülle, 2014, Yamada and Yoon, 2014): (i) one can exclude a positive upward trend for commodity prices, (ii) there is no general support for the Prebisch-Singer hypothesis of a secular deterioration with respect to manufactured goods for all commodities, with most commodity prices actually better characterized by discontinuous, deterministic, and non-monotonic long-term trends, possibly negative over some intervals, and (iii) the remaining commodity prices displaying a unit root, possibly with breaks. In sum, if most commodities are found to be trend stationary, it is by segments divided by infrequent shifts. Since a random walk with drift would not be a satisfactory trend specification for most commodities, we adopt Canova's approach by jointly estimating a storage model and a reduced-form trend that describes the non-cyclical component of price. Our approach implies that the storers neglect the existence of a trend in prices and arbitrate prices only on the basis of their cyclical component. This issue is likely to be of second order

¹ See also Ferroni (2011) for an application.

compared to the gains from making the prices more stationary (as confirmed in Zeng, 2012, who finds little differences in estimations on small sample whether storers account for trend or not).

The estimation procedure starts from the Maximum Likelihood estimator proposed for the storage model by Cafiero et al. (2015), and which was proved to have better small sample properties than Deaton and Laroque's (1996) Pseudo-Maximum Likelihood estimator. We extend the Maximum Likelihood estimator to account for a potential trend in prices and to exploit the information available from the first observation. This leads to the development of a new simulated unconditional Maximum Likelihood estimator. Following the finding that most commodity prices are best characterized as trend stationary with breaks, we consider only deterministic trend specifications. This assumption simplifies the analysis by allowing the likelihood to be expressed analytically,² at the cost of being inadequate for the commodity prices best characterized as difference stationary. As well as the case without trend, we consider a multiplicative trend, in which the logarithm of the trend can be linear as in Cafiero et al. (2011a), Bobenrieth et al. (2013, 2014), and Guerra et al. (2015), or represented by a restricted cubic spline as in Roberts and Schlenker (2013). We believe that by using for the trend a restricted cubic spline with up to four knots we are able to capture in a tractable way the deterministic trends with breaks identified in the literature. For the thirteen storable commodities considered in Deaton and Laroque (1992), there is a model with trend which presents a lower Akaike information criterion than the model without trend. Our estimates for the preferred models more closely replicate the key features of the data and allow for the occurrence of stockouts in line with the observed two-regime structure of long periods of stable prices interrupted by isolated spike episodes.

The remainder of the chapter is organized as follows. Section 3.1 describes the competitive storage model discussed and estimated in Deaton and Laroque (1992, 1996) and Cafiero et al. (2011b). Section 3.2 presents the econometric procedure used to estimate the storage model with multiplicative deterministic trend, and describes how the unconditional maximum likelihood estimator is constructed. Section 3.3 presents the empirical results, and section 4.4 concludes.

3.1 THE MODEL

3.1.1 MODEL EQUATIONS

We adopt the standard competitive storage model with no supply response, constant marginal storage cost, and no stock deterioration in line with Cafiero et al. (2011b). The exogenous supply is modeled by i.i.d. random production shocks ε_t following a normal distribution with mean μ and standard deviation σ truncated at five standard deviations. The demand for commodities consists of a demand for current consumption C_t associated with the inverse demand function $D^{-1}(C_t) = a + bC_t$, which is assumed to be linear with fixed parameters a and $b < 0$, and a speculative demand from competitive risk-neutral storers. Storers carry over $S_t \geq 0$ units of the commodity into the next period whenever they expect a positive return to storage over the

² Stochastic trends would require a non-linear state-space approach and the use of particle filters (Fernández-Villaverde and Rubio-Ramírez, 2007), a promising but challenging approach for a model as non-linear as the storage model.

interest and physical storage costs, and otherwise sell their past inventories. Assuming rational expectations and taking account of the non-negativity constraint on storage yields the following arbitrage condition:

$$\beta E_t P_{t+1} - P_t - k \leq 0, = 0 \text{ if } S_t > 0, \quad (3.1)$$

where $\beta = 1/(1+r)$ is the discount factor which is assumed to be fixed, $k \geq 0$ is the constant per unit physical cost of storage, P_t is the price, and E_t is the expectation operator conditional on period t information. In equilibrium, supply equals total demand such that

$$A_t = S_t + D(P_t), \quad (3.2)$$

where the amount on hand A_t at time t is the sum of the past inventories and the stochastic production ε_t written as

$$A_t \equiv S_{t-1} + \varepsilon_t, \quad (3.3)$$

with $A_t \in \mathbb{A} \equiv [-5\sigma, \infty)$.

Combined with the market clearing condition, the arbitrage condition (3.1) leads to two regimes in the price dynamics:

$$P_t = \max [\beta E_t P_{t+1} - k, D^{-1}(A_t)]. \quad (3.4)$$

The first regime holds when speculators stockpile expecting the future price to cover the purchasing and full carrying costs. The second regime defines the stockout situation with empty inventories, where the market price is determined only by the final demand for consumption and the amount on hand in the market.

For this problem, a stationary rational expectations equilibrium is a price function $\mathcal{P} : \mathbb{A} \rightarrow \mathbb{R}$ which describes price as a function of contemporaneous availability. From equation (3.4), this price function satisfies for all A_t

$$\mathcal{P}(A_t) = \max [\beta E_t \mathcal{P}(S_t + \varepsilon_{t+1}) - k, D^{-1}(A_t)], \quad (3.5)$$

where, from (3.2), S_t is given by

$$S_t = A_t - D(\mathcal{P}(A_t)). \quad (3.6)$$

Building on Deaton and Laroque (1992), Cafiero et al. (2011b) prove that for this model there is a unique stationary rational expectations equilibrium \mathcal{P} in the class of continuous strictly decreasing functions.³ If we define $P^* \equiv \beta E \mathcal{P}(\varepsilon) - k$, the cutoff price for no storage, the price function has the following properties:

$$\mathcal{P}(A) = D^{-1}(A), \text{ for } A \leq D(P^*), \quad (3.7)$$

$$\mathcal{P}(A) > D^{-1}(A), \text{ for } A > D(P^*). \quad (3.8)$$

³ Cafiero et al. (2015) extend the proof to a model with free disposal and with a production support that may be unbounded. Free disposal has the advantage to prevent the realization of negative equilibrium prices, but increases significantly the time required to solve the model numerically preventing us from implementing it in this study.

So P^* , which depends on the price function, defines the threshold between the two regimes. Prices above P^* are too high to make storage profitable, while for prices below P^* some stocks are carried over.

There is no closed-form solution for the equilibrium price function, which has to be approximated numerically. The numerical method follows the fixed-point approach proposed by Deaton and Laroque (1992) and is described in section 3.A of the appendix.

3.1.2 HOW CAN STORAGE GENERATE HIGH SERIAL CORRELATION?

The debate over the empirical relevance of the storage model revolves around its ability to generate the high serial correlation observed in the data. Here, we explore the combination of parameters that allows the model to generate high serial correlation. Our storage model has six parameters, $\{a, b, k, r, \mu, \sigma\}$. In the remainder of this chapter, we follow Deaton and Laroque (1996) and Cafiero et al. (2015) by fixing r at 5%. Deaton and Laroque (1996, Proposition 1) prove that it is not possible to identify separately the demand function and the distribution of supply shocks. So in this section, we set the mean and standard deviation of the harvest at 1 and 0.05.⁴ The mean price over the model asymptotic distribution is set to 1, which implies $a + b = 1$. Two degrees of freedom remain: storage cost and demand elasticity. We vary them to see how this affects the serial correlation. Given our assumptions, k can be interpreted as the ratio of storage costs with respect to the mean price, and the demand elasticity calculated at the mean price is simply equal to $1/b$.

To analyze the effect of storage cost on serial correlation, we set demand elasticity at -0.05 , corresponding to Roberts and Schlenker's (2013) best estimate of the elasticity of a caloric aggregate of the major crops. We vary storage costs between 0 and 20 percent of the mean price, and for every value of storage cost we solve and simulate the model. We calculate the first-order autocorrelation for 100,000 series of 100 periods on the asymptotic distribution. As noted by Cafiero et al. (2011b), simulating the storage model generates time series with very volatile moments when the series length is around the number of observable annual prices (close to one hundred years). Therefore, it is not sufficient to compare the serial correlation of observable price to the average simulated first-order autocorrelation, we need also to compare it to the quantiles of the distribution of simulated first-order autocorrelation. The left panel of figure 3.2 displays the 5th, 50th, and 95th percentiles of the distribution of simulated first-order autocorrelation when we vary the storage cost. Serial correlation is a monotonically decreasing function of storage cost. This can be explained by the fact that the storage model displays two regimes. In one regime, there are positive stocks and prices are serially correlated. In the other, stocks are zero and prices are not serially correlated. The more time that is spent in the stockout regime, the lower will be the overall serial correlation generated by the model. Decreasing the storage cost makes storage more profitable, increases stock levels, thereby decreasing the likelihood of a stockout and increasing the serial correlation. With this calibration, even for a zero storage cost, the median first-order autocorrelation is well below the very high correlation observed in the price series (above 0.82 for all commodities except sugar). Even the 95th percentile is below 0.8.

⁴ A coefficient of variation of 5% for supply shocks is close to what is observed for the commodities considered in this work (see table 3.13 in the appendix).

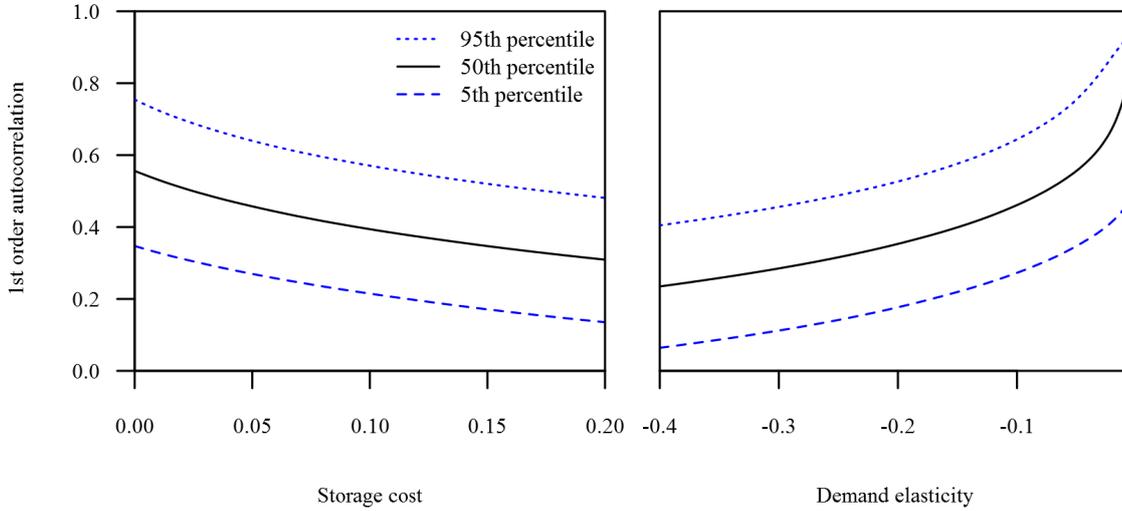


Figure 3.2. First-order autocorrelation implied by the storage model over 100 periods for several values of storage cost (with demand elasticity set at -0.05) and demand elasticity (with storage cost set at 0)

This failure of the storage model to induce sufficient serial correlation in prices calls for a parameterization that is even more favorable to storage. This can be achieved by rotating the slope of the demand function around its mean. Indeed, in absence of inventories to buffer against short supply, the price adjustments are dictated only by the final demand for consumption. So the more inelastic the demand, the steeper the variations in prices and the greater the incentive to store. We set the storage cost at its zero lower bound and vary the demand elasticity between -0.4 and -0.005 (right panel of figure 3.2). Only for a very inelastic demand curve is the median of simulated first-order autocorrelation close to 0.8. The 95th percentile can be compatible with a first-order autocorrelation of 0.8 for a demand elasticity above -0.037 .

In the storage model with i.i.d. supply shocks, stockpiling is the sole source of time-dependency in prices, so only a model parameterization in which storage arbitrage is often active can generate high serial correlations. The model can generate high serial correlation only by decreasing the occurrence of stockouts which requires a parameterization of very low storage cost and very inelastic demand. So in the estimations that follow, we should expect that a storage model able to replicate the characteristics of the raw price series will be characterized by low storage costs and inelastic demand functions. Even with this combination, high first-order autocorrelation is achieved only by the high percentiles of the asymptotic distribution.

3.2 ECONOMETRIC PROCEDURE

In this section, following Canova (2014), we propose an econometric procedure to estimate the storage model and the trend in prices jointly. The idea behind this procedure is to capture in the trend the component of prices that cannot be accounted for by the storage model, in particular the non-cyclical fluctuations. As a result, the storage model has to account only for cyclical fluctuations in the observed data. We assume that observed prices, P_t^{obs} , can be decomposed into a multiplicative trend $\exp[\Gamma(t, \theta^\Gamma)]$ and a cyclical component

denoted P_t^{sto} to be explained by the storage model:

$$P_t^{\text{obs}} = e^{\Gamma(t, \theta^\Gamma)} P_t^{\text{sto}}. \quad (3.9)$$

The vector of the parameters to be estimated θ can be split into two groups: the trend parameters θ^Γ , and the structural parameters of the storage model, θ^{sto} . In addition to the baseline case where any trend is ignored we consider three deterministic time trend specifications. In none of the trend specifications do we introduce an intercept because it would not be possible to identify separately the intercept of the trend from the intercept of the inverse demand function since both would be determined by the mean level of observed prices.

3.2.1 TREND SPECIFICATIONS

NO TREND Our benchmark situation is where observed prices are assumed to be without trend. In this case, $\Gamma(t, \theta^\Gamma) = 0$, $P_t^{\text{obs}} = P_t^{\text{sto}}$, and θ^Γ is empty.

LINEAR TREND Here we assume the trend is a deterministic linear time trend:

$$\Gamma(t, \theta^\Gamma) = g_1 t. \quad (3.10)$$

In this case $\theta^\Gamma = \{g_1\}$. For numerical stability, the time variable, t , is taken to vary between -1 and 1 .

RESTRICTED CUBIC SPLINES While the linear trend allows us to capture the overall long-run trend, it may not capture all the non-cyclical fluctuations that the storage model is unable to explain. It is often considered that trends in commodity prices might be non-constant (a feature captured, e.g., in Arezki et al., 2014, by a piecewise linear trend with structural breaks). For a more flexible trend than in the linear case, we use restricted cubic splines. Cubic splines are piecewise cubic polynomials with continuous first and second derivatives. “Restricted” splines are splines that are constrained to be linear beyond the boundary knots which avoids a poor behavior in the tails, a feature common to polynomial trends. A restricted cubic spline with three knots has two parameters. With four knots, it has three parameters. So restricted cubic splines with three and four knots have the same degrees of freedom as quadratic and cubic polynomials but tend to be slightly more flexible. A spline with two knots would be the same as the linear trend above. Restricted cubic splines with three to five knots are also used in Roberts and Schlenker (2013) to capture trends in prices and quantities of agricultural commodities.

When represented by restricted cubic splines, the trend is expressed as

$$\Gamma(t, \theta^\Gamma) = \sum_{i=1}^I g_i B_i(t), \quad (3.11)$$

where I and $B_i(\cdot)$ are the degree of freedom and the basis functions of the spline,⁵ and g_i are the trend parameters to be estimated. The $B_i(\cdot)$ are functions of the knots, but once the knots are fixed the trend is linear in its parameters. Following the heuristics proposed in Harrell (2001), the knots for the cubic spline with three knots are located at the 10th, 50th, and 90th quantiles of the covariate, which correspond in our 1900–2011 sample to the years 1911, 1956, and 2000. The spline with four knots uses as knots the 5th, 35th, 65th, and 95th quantiles (1905, 1939, 1970, and 2006).

Since the knots are fixed before the estimation, only the slope parameters have to be estimated: $\theta^\Gamma = \{g_i\}_{i=1}^I$.

3.2.2 THE LIKELIHOOD ESTIMATOR

Given that the price function \mathcal{P} is strictly decreasing (Cafiero et al., 2011b), we can invert it to obtain the amount on hand from the price. Using the inverse of the price function, the cyclical component of prices, P^{sto} , follows a first-order Markov process with the transition equation defined by equations (3.3) and (3.6) as

$$P_t^{\text{sto}} = \mathcal{P}(\mathcal{P}^{-1}(P_{t-1}^{\text{sto}}) - D(P_{t-1}^{\text{sto}}) + \varepsilon_t). \quad (3.12)$$

It is possible to link P_t^{sto} to observed prices, P_t^{obs} , using equation (3.9). So, given the price function \mathcal{P} , equations (3.9) and (4.4) define a mapping from the supply shocks ε_t to P_t^{obs} , conditional on P_{t-1}^{obs} and t .

Given a set of model parameters θ and a sample of observed prices of length T , noted $P_{1:T}^{\text{obs}} \equiv \{P_1^{\text{obs}}, \dots, P_T^{\text{obs}}\}$, and using the Markov structure of the problem, the likelihood function can be expressed as

$$L(\theta; P_{1:T}^{\text{obs}}) = f(P_1^{\text{obs}}; \theta) \prod_{t=2}^T f(P_t^{\text{obs}} | P_{t-1}^{\text{obs}}; \theta). \quad (3.13)$$

Using the mapping between observables and shocks, Miranda and Rui (1999) and Cafiero et al. (2015) obtain the conditional density $f(P_t^{\text{obs}} | P_{t-1}^{\text{obs}}; \theta)$ from the variable transformation method. Identification of the parameters of the demand function requires the parameters of the distribution of shocks to be set to arbitrary values. From here, the distribution of ε is assumed to be the unit normal distribution truncated at five standard deviations, with probability density function $f_\varepsilon(\varepsilon) = \phi(\varepsilon) / [\Phi(5) - \Phi(-5)]$ for $\varepsilon \in [-5, 5]$ and $f_\varepsilon(\varepsilon) = 0$ otherwise. We can write the conditional density of P_t^{obs} as:

$$f(P_t^{\text{obs}} | P_{t-1}^{\text{obs}}; \theta) = f_\varepsilon(\varepsilon_t) |J_t|, \quad (3.14)$$

where $|J_t|$ is the determinant of the Jacobian of the mapping $P_t^{\text{obs}} \mapsto \varepsilon_t$.

⁵ For numerical stability, the splines are expressed in B-spline form and their basis matrices come from the command `ns` in the R package `splines`.

Based on equations (3.9) and (4.4), this mapping is

$$\begin{aligned}\varepsilon_t &= \mathcal{P}^{-1}(P_t^{\text{sto}}) - [\mathcal{P}^{-1}(P_{t-1}^{\text{sto}}) - D(P_{t-1}^{\text{sto}})], \\ &= \mathcal{P}^{-1}(e^{-\Gamma(t, \theta^\Gamma)} P_t^{\text{obs}}) - [\mathcal{P}^{-1}(e^{-\Gamma(t-1, \theta^\Gamma)} P_{t-1}^{\text{obs}}) - D(e^{-\Gamma(t-1, \theta^\Gamma)} P_{t-1}^{\text{obs}})],\end{aligned}\quad (3.15)$$

which gives the expression of J_t :

$$J_t = e^{-\Gamma(t, \theta^\Gamma)} \mathcal{P}^{-1'}(e^{-\Gamma(t, \theta^\Gamma)} P_t^{\text{obs}}). \quad (3.16)$$

The probability of any element of $P_{1:T}^{\text{sto}}$ being equal to P^* is zero, so the derivative of \mathcal{P}^{-1} exists almost everywhere.

In this study we extend the Conditional Maximum Likelihood Estimator pioneered by Cafiero et al. (2015) to its unconditional counterpart. The aim is to use all the available information from the first observation by accounting for the marginal density $f(P_1^{\text{obs}}; \theta)$ in equation (3.13). The marginal density $f(P_1^{\text{obs}}; \theta)$ can be expressed as the following integral over the steady-state distribution:

$$f(P_1^{\text{obs}}; \theta) = \int_{P_0} f(P_1^{\text{obs}} | P_0; \theta) f(P_0; \theta) dP_0. \quad (3.17)$$

This integral is intractable, because there is no closed-form solution for the steady-state distribution of the storage model. However, we can draw from the distribution with density $f(P_0; \theta)$, which is the unconditional probability density function of price in the storage model. Therefore, we can use Monte Carlo integration to estimate $f(P_1^{\text{obs}}; \theta)$ by simulating the model on the stationary distribution:

$$f(P_1^{\text{obs}}; \theta) \approx M^{-1} \sum_{m=1}^M f(P_1^{\text{obs}} | P_0^{(m)}; \theta), \quad (3.18)$$

where $m = \{1, \dots, M\}$ indexes random draws from the unconditional price distribution. We set the number of draws M to 1,000,000 and obtain them by simulating 10,000 trajectories starting from the steady state for 120 periods and discarding the first 20 periods as burn-in periods. The random production shocks that generate the price simulations are drawn at the beginning of the estimation procedure and remain fixed throughout. Because of this simulation step, the Unconditional Maximum Likelihood Estimator falls within the class of simulated estimators.

As is well known in time-series econometrics (Hamilton, 1994, Ch. 5), if the sample size is sufficiently large the contribution of the first observation to the likelihood is negligible, while it is often much more complex to calculate the unconditional likelihood than the conditional likelihood. In the case of the storage model, it is true that the simulations necessary to calculate the marginal density make the likelihood evaluation much more costly. In Monte Carlo experiments designed following Michaelides and Ng (2000) and Cafiero et al. (2015), the unconditional likelihood performs only marginally better than the conditional likelihood.⁶ However, when using an actual sample, the unconditional likelihood has benefits which in our view outweigh

⁶ Results available in section 3.C of the appendix.

its costs. For observed prices the conditional likelihood presents many local optima. The unconditional likelihood helps to select an optimum with an unconditional price distribution not too far from the price sample which may not be the case for a conditional likelihood. Indeed, in order to fit the high serial correlation of the data, the Conditional Maximum Likelihood Estimator often leads to parameter estimates for which the availabilities corresponding to observed prices (calculated using \mathcal{P}^{-1}) are set at very high levels which would correspond to very high stock levels. Observing large stock levels may have a high probability conditional on having large stocks in the previous period, but the unconditional probability of such a situation is very low. So, the Unconditional Maximum Likelihood Estimator helps to filter out some of these situations.

Based on all the previous elements, we can write the log-likelihood as

$$\begin{aligned} \log L(\theta; P_{1:T}^{\text{obs}}) = & -\frac{T}{2} \log 2\pi - T \log [\Phi(5) - \Phi(-5)] + \sum_{t=1}^T \left[-\Gamma(t, \theta^\Gamma) + \log \left| \mathcal{P}^{-1} \left(e^{-\Gamma(t, \theta^\Gamma)} P_t^{\text{obs}} \right) \right| \right] \\ & - \sum_{t=2}^T (1_{|\varepsilon_t| \leq 5} \cdot \varepsilon_t^2 + 1_{|\varepsilon_t| > 5} \cdot \infty) / 2 + \log \left(M^{-1} \sum_{m=1}^M 1_{|\varepsilon^{(m)}| \leq 5} \cdot \exp \left(-\varepsilon^{(m)2} / 2 \right) \right), \quad (3.19) \end{aligned}$$

where 1 is the indicator function and $\varepsilon^{(m)} = \mathcal{P}^{-1} \left(\exp(-\Gamma(1, \theta^\Gamma)) P_1^{\text{obs}} \right) - S_0^{(m)}$. Given that the interest rate and the parameters of the distribution of production shocks have been fixed, there are three parameters that we need to estimate for the storage model $\theta^{\text{sto}} = \{a, b, k\}$, in addition to the parameters characterizing the trend, θ^Γ , defined above. From a set of parameters θ provided by the optimization algorithm, we calculate the detrended price P^{sto} and solve for the policy function of the storage model $\mathcal{P}(\cdot)$. Using this policy function, we can simulate the model to calculate the marginal probability and evaluate the likelihood for this set of parameters.

Evaluated on the observed prices, the above log-likelihood behaves badly. It displays many local optima. Gradient-based solvers and derivative-free local search methods converge only to local optima which are very sensitive to first guesses. Thus, we need to apply a global search algorithm to increase the likelihood of obtaining a global solution. Following a recent review of derivative-free algorithms (Rios and Sahinidis, 2013), and some tests on our problem, we choose a global solver, the particle swarm pattern search algorithm proposed by Vaz and Vicente (2007), and refine the solution it delivers with a local solver using a sequential quadratic programming approach (Nocedal and Wright, 2006, Ch. 18). Parameters are constrained to remain within bounds (this is required by the global solver). b is constrained to be strictly negative (≤ -0.001) and k to be positive or null. All the other bounds are chosen to be low enough or high enough to avoid them being binding. The particle swarm solver is initialized with 700 vectors of first-guess parameters, a combination of educated guesses, random draws, and vectors of previous solutions (e.g., the estimation without trend serves as a first guess for the linear trend). The tolerance for both optimization solvers is fixed at 10^{-6} .

Once a maximum has been identified, we estimate the asymptotic variance-covariance matrix of the parameters as the inverse of the outer product of the scores. If the highest log-likelihood is obtained with k constrained at its zero lower bound, calculating the variance-covariance matrix using the scores is inappropriate, and other methods such as bootstrap should be used. However, the number of our estimations prevents us from using the bootstrap method. For the estimates with k at zero, we do not report the standard

errors for k but report the standard errors of the other parameters obtained using the inverse of the outer product of the scores by maintaining k at zero.

3.3 ESTIMATION RESULTS

3.3.1 DATA

Our data set is composed of the thirteen commodities analyzed in Deaton and Laroque (1992) (banana, cocoa, coffee, copper, cotton, jute, maize, palm oil, rice, sugar, tea, tin, and wheat). The original price series from Grilli and Yang (1988) is extended by Pfaffenzeller et al. (2007) and cover the period 1900 to 2011. The data were downloaded from Stephan Pfaffenzeller's personal website.⁷ The data are annual price indexes calculated by averaging the monthly price data provided by the World Bank Development Prospects Groups over the calendar year, and normalizing them with respect to the 1977–79 mean price. We deflated the nominal price indexes by the US CPI.

We use only price data to estimate the storage model but we also rely on shorter series of production data to illustrate the consequence of our estimations in terms of demand elasticities. The production data are from the FAOSTAT food balance sheets in the case of the agricultural commodities,⁸ from the British Geological Survey in the case of tin,⁹ and from the 2014 World Copper Factbook of the International Copper Study Group for copper.¹⁰ They cover the period 1961 to 2011. For each commodity, the logarithm of production is detrended by modeling the trend by a restricted cubic spline with five knots (as in Roberts and Schlenker, 2013).¹¹

3.3.2 MODEL SELECTION

Joint estimation of the structural and trend parameters allows us to select the preferred trend specification using model selection criteria. We select the preferred trend specification using the Akaike Information Criterion (AIC). The results are reported in table 3.1 which presents the values for the preferred models in boldface. For the model without trend the AIC is given in level, while for the three models with trend they are given in ratios to the AIC of the model without trend so that a value above unity means a lower AIC than the model without trend. According to the AIC, the model without trend is never retained for any of the commodities. The model with a linear trend is preferred for copper, palm oil, and wheat. The model with a three-knot spline trend (RCS3) is preferred for coffee, cotton, jute, rice, and sugar. The model with a four-knot spline trend (RCS4) is preferred for banana, cocoa, maize, tea, and tin.

For the estimations where storage costs are not constrained on their lower bound we also perform likelihood ratio tests to confirm whether the model without trend is rejected (table 3.12 in appendix). The

⁷ <http://www.stephan-pfaffenzeller.com>

⁸ <http://faostat.fao.org/>

⁹ <http://www.bgs.ac.uk/mineralsuk/statistics/home.html>

¹⁰ <http://www.icsg.org/index.php/statistics/selected-data>

¹¹ The knots are located at 1964, 1975, 1986, 1998, and 2008 as suggested by Harrell (2001).

Table 3.1. Model Selection Using the Akaike Information Criterion

Commodity	No trend	Linear	RCS3	RCS4
Banana	-309.823	1.030	1.069	1.070
Cocoa	-417.014	0.998	1.010	1.025
Coffee	-377.997	0.995	1.005	1.000
Copper	-236.051	1.000	0.993	0.997
Cotton	-231.181	0.992	1.021	1.011
Jute	-184.036	1.015	1.056	1.045
Maize	-159.578	0.998	1.002	1.038
Palm oil	-219.800	1.042	1.040	1.034
Rice	-219.357	1.105	1.114	1.104
Sugar	-93.022	1.189	1.198	1.179
Tea	-275.557	1.011	1.010	1.014
Tin	-406.411	0.996	1.006	1.006
Wheat	-189.445	1.054	1.046	1.054

Notes: For the “No trend” column, the AIC are given in levels while for the other columns they are reported in ratios to the “No trend” column so that a value above unity means a lower AIC than the model without trend. The preferred model for each commodity is in boldface.

model selection is confirmed by the likelihood ratio test: for almost all the selected models with trend the test rejects the null of a model without trend. This is not the case for coffee and copper for which we cannot reject the null at the 5% threshold, in line with values of AIC that barely exceed under the preferred trends the values without trend. In what follows, to maintain the comparability with the commodities for which the same test cannot be done, we retain as preferred models for coffee and copper those with trend selected by the AIC, but when interpreting the results it has to be kept in minds that they do not pass the likelihood ratio test.

3.3.3 NO TREND

The parameter estimates for the model without trend are given in table 3.2. In this setting without stock deterioration, estimates of a in the first column are directly interpretable as the ergodic means of the models. Thus, it would be reasonable to expect a to be not too far from the observed sample means reported in table 3.3, even if the sample mean is not the maximum likelihood estimator of a . However, this is not the case. With the exception of sugar, a is systematically higher than the sample mean, and for some commodities by a large margin. For example, a exceeds the sample mean by 255 percent for banana, 227 for cotton, 122 for rice, or 80 for wheat. This “bias” could be related to the presence of a trend in the observables. A trend would generate a serial correlation higher than expected from storage alone. Estimating the ergodic mean of the model at above the sample mean implies that the sample is located in a region of larger than normal availabilities, and with large availabilities there are important stocks, and prices are more positively correlated than if availabilities are close to normal.

Table 3.2. Parameter Estimates Without Trend

Commodity	a	b	k	$\log L$	P^*	# Stockouts
Banana	1.9078 (0.6159)	-3.8117 (2.3678)	0.0011 (0.0037)	157.9117	3.6291	0
Cocoa	0.1826 (0.0383)	-0.8604 (0.0930)	0.0002 (0.0009)	211.5072	0.6149	0
Coffee	0.2571 (0.0259)	-0.8959 (0.0656)	0.0015 (0.0009)	191.9984	0.6876	0
Copper	0.6339 (0.0540)	-1.1740 (0.1382)	0.0046 (0.0034)	121.0254	1.1461	0
Cotton	1.7832 (0.7019)	-6.1122 (3.9400)	0.0029 (0.0027)	118.5906	4.7461	0
Jute	0.6934 (0.0970)	-1.7440 (0.2308)	0.0050 (0.0049)	95.0180	1.4927	0
Maize	0.7058 (0.0816)	-2.3422 (0.1738)	0.0009 (0.0030)	82.7891	1.8374	0
Palm oil	0.7311 (0.0802)	-1.5067 (0.1708)	0.0097 (0.0046)	112.8999	1.3887	1
Rice	1.1766 (0.3604)	-5.2418 (2.2061)	0 -	112.6784	3.8021	0
Sugar	0.5362 (0.0521)	-1.9907 (0.1123)	0.0050 (0.0026)	49.5109	1.4926	3
Tea	1.0839 (0.4672)	-3.6411 (2.2116)	0 -	140.7786	2.8518	0
Tin	0.3606 (0.0509)	-1.0371 (0.2022)	0.0023 (0.0015)	206.2057	0.8462	0
Wheat	1.0926 (0.1819)	-3.9100 (1.0561)	0 -	97.7225	3.0058	0

Notes: Asymptotic standard errors in parentheses. Column # Stockouts indicates the number of times the observed prices are greater than or equal to the cutoff price for no storage: $\sum_{t=1}^T 1_{P_t^{\text{obs}} \geq P^*}$.

The limited number of stockouts confirms that the estimations localize all the samples in regions with large availability. With the exception of palm oil and sugar for which the respective number of periods without stocks over the sample are 1 and 3, commodity prices are always under their respective cutoff price P^* implying that inventories were carried over the whole 112 years of the sample. This feature is present also in the estimations in Cafiero et al. (2011b), where only sugar displays stockouts. In the model, stockouts occur when prices exceed P^* . Our estimations show that on average over all commodities, P^* exceeds its corresponding sample means by 4.5 times, making stockouts unlikely.

Figure 3.3 illustrates this in the case of wheat. Most observed prices are below the ergodic mean of the model, and all are far from P^* . If we compare the localization of the observed prices to the ergodic distribution of availability, we see that the observations are concentrated to the right of the distribution mode. The observations look more like an extreme sample in which the level of availability, and thus the stock level

Table 3.3. Comparisons of Data Features and Predictions of the Model Without Trend

Commodity	Variable	Mean	One-year a-c	Two-year a-c	Coefficient of variation	Skewness	Excess kurtosis
Banana	Observed moments	0.54	0.95	0.90	0.23	-0.27	-0.77
	Model percentiles	0.00	99.99	99.97	0.09	0.00	0.15
Cocoa	Observed moments	0.17	0.86	0.71	0.60	1.24	1.64
	Model percentiles	44.65	79.86	70.05	23.67	17.34	19.25
Coffee	Observed moments	0.20	0.84	0.68	0.50	1.61	3.89
	Model percentiles	24.01	83.94	76.14	10.45	25.41	28.47
Copper	Observed moments	0.47	0.83	0.64	0.40	0.90	0.56
	Model percentiles	6.22	96.47	87.84	10.72	4.30	3.92
Cotton	Observed moments	0.55	0.94	0.85	0.51	0.20	-0.61
	Model percentiles	0.55	99.74	97.75	16.38	0.19	0.71
Jute	Observed moments	0.52	0.84	0.70	0.44	0.41	-0.23
	Model percentiles	13.15	92.75	89.26	8.31	0.62	1.49
Maize	Observed moments	0.61	0.86	0.73	0.51	0.84	1.22
	Model percentiles	31.96	89.21	84.45	18.51	5.54	13.10
Palm oil	Observed moments	0.46	0.82	0.65	0.60	2.43	11.84
	Model percentiles	2.34	95.05	89.66	48.31	50.03	71.20
Rice	Observed moments	0.53	0.91	0.79	0.50	0.42	-0.39
	Model percentiles	5.81	94.03	87.47	12.04	0.89	1.88
Sugar	Observed moments	0.61	0.70	0.51	0.69	1.62	3.45
	Model percentiles	66.50	48.82	40.01	33.70	25.65	26.31
Tea	Observed moments	0.45	0.90	0.81	0.38	-0.02	-0.80
	Model percentiles	1.63	95.84	95.15	3.18	0.03	0.31
Tin	Observed moments	0.20	0.90	0.78	0.47	1.48	2.84
	Model percentiles	3.87	98.21	95.47	9.35	19.40	20.00
Wheat	Observed moments	0.61	0.91	0.79	0.47	0.82	0.39
	Model percentiles	6.73	96.97	91.36	12.58	5.42	6.80

Note: There are two variables for each commodity: the moments calculated on the observed prices, P^{obs} , and below the percentiles corresponding to these moments calculated from the estimated model using samples of the same size as the data.

are always high, than a typical sample from the distribution.

The small number of stockouts, and localization of the samples in regions with large availabilities question the empirical relevance of the storage model. This model is supposed to alternate between two regimes with relatively stable prices when there are stocks, and spikes during stockouts. If there are no stockouts, price spikes are explained by adverse production shocks only. They do not correspond to a much steeper part of the demand function and should be as likely as price troughs, which is not consistent with the stylized facts. Most commodity prices present a positive skewness (table 3.3) and there are few downward spikes to match the upward spikes (Deaton and Laroque, 1992).

Section 3.1.2 showed that the storage model can generate high serial correlation only with parameterization of very low storage cost and very inelastic demand. We next examine the magnitude of the estimated storage costs and demand elasticities. k/a is the ratio of storage cost to the ergodic mean price, so it is unit-free and directly interpretable. Because we assumed that supply shocks follow a truncated unit normal, it is not possible to recover the demand elasticity only from the demand function. To calculate the demand

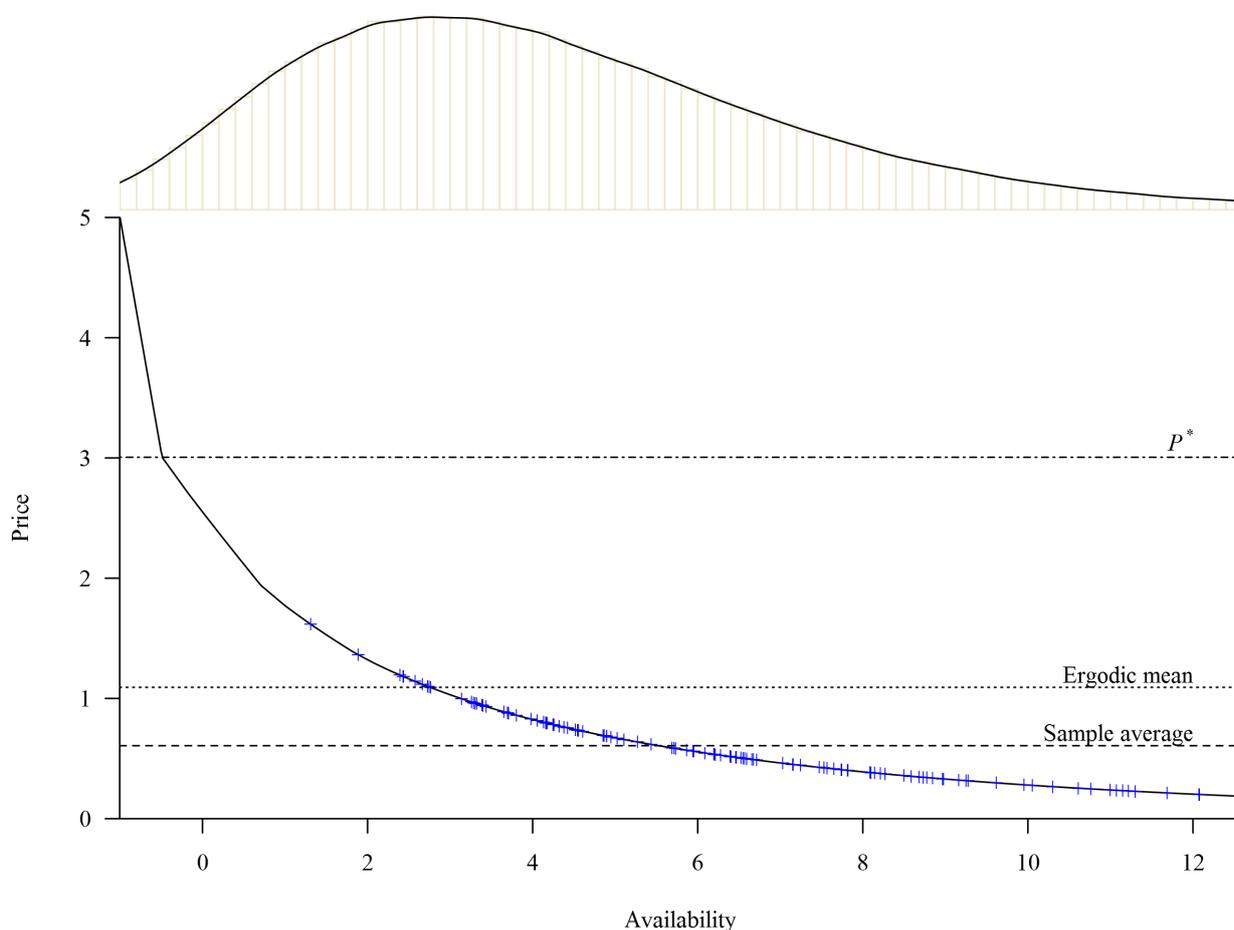


Figure 3.3. Estimated storage model for wheat without trend. Lower panel: price function, $\mathcal{P}(A)$, with observed prices and corresponding availabilities on it noted +. Upper panel: ergodic distribution of availability.

elasticity, we use Deaton and Laroque's (1996) Proposition 1 which shows that re-scaling the distribution of supply shocks to have mean and standard deviation μ and σ while adjusting the inverse demand function to $\tilde{D}^{-1}(C_t) = (a - b\mu/\sigma) + bC_t/\sigma$ does not affect the distribution of prices. Using this adjusted demand function, the demand elasticity evaluated at the model's ergodic mean price is given by $a\sigma/(b\mu)$.¹² The coefficient of variation of the supply shocks, σ/μ , is obtained by calculating the standard deviation of the detrended logarithm of production, and is provided in the appendix.¹³

The estimated storage costs and price elasticities of demand are consistent with the results in section 3.1.2: both are low (table 3.4). The estimated storage costs are below 1 percent of the ergodic price for all

¹² A similar approach is used in Guerra et al. (2015).

¹³ While reformulating the estimates as unit-free parameters is necessary to compare them between trend specifications, the expression as a demand elasticity relies on a literal interpretation of the storage model. In this specification of the storage model, additive demand shocks are equivalent to additive negative supply shocks, and thus the supply shocks in the model should be interpreted as net-supply shocks. If we assume that demand and supply shocks are uncorrelated, the elasticities calculated using only the coefficient of variation of supply will be downward biased. For staple food markets, where price volatility is often believed to be primarily driven by supply shocks the bias may be small, but it may be larger for commodities more subject to demand shocks such as metals.

commodities except palm oil, and are null for three commodities: rice, tea, and wheat. Information on storage costs to which we could compare these estimates are not readily available for all commodities. However, in a study of the grain chain in Middle East and North African countries, World Bank and FAO (2012, figure 2-4) report that the storage cost of wheat in the US was equal to US\$ 24.24 per ton in 2009, which would represent around 10% of the recent price of wheat. So, at least for cereals, the estimates of storage costs appear to be low.

Table 3.4. Estimated Values of Storage Costs and Demand Elasticities

Commodity	Storage costs: $100 \cdot k/a$				Price elasticity of demand: $a\sigma/(b\mu)$			
	No trend	Linear	RCS3	RCS4	No trend	Linear	RCS3	RCS4
Banana	0.06 (0.19)	0 –	0 –	0 –	–0.018 (0.013)	–0.033 (0.004)	–0.029 (0.009)	– 0.029 (0.008)
Cocoa	0.11 (0.51)	0.19 (0.54)	0.05 (0.23)	0.53 (0.63)	–0.015 (0.004)	–0.015 (0.004)	–0.015 (0.010)	– 0.027 (0.009)
Coffee	0.59 (0.35)	0.59 (0.35)	1.41 (1.01)	1.41 (1.07)	–0.022 (0.003)	–0.022 (0.003)	– 0.037 (0.010)	–0.037 (0.010)
Copper	0.72 (0.54)	1.09 (0.67)	0.99 (0.70)	0.07 (0.59)	–0.024 (0.004)	– 0.028 (0.004)	–0.028 (0.005)	–0.019 (0.005)
Cotton	0.16 (0.17)	0.19 (0.43)	0.34 (0.43)	0.34 (0.50)	–0.021 (0.016)	–0.022 (0.038)	– 0.029 (0.015)	–0.029 (0.020)
Jute	0.72 (0.71)	0.42 (0.96)	2.35 (0.91)	2.34 (0.99)	–0.045 (0.009)	–0.045 (0.008)	– 0.104 (0.009)	–0.104 (0.015)
Maize	0.13 (0.43)	1.07 (0.83)	1.34 (0.80)	3.25 (0.75)	–0.018 (0.002)	–0.030 (0.004)	–0.036 (0.005)	– 0.062 (0.005)
Palm oil	1.33 (0.64)	1.20 (0.91)	1.40 (0.88)	1.43 (0.98)	–0.023 (0.004)	– 0.027 (0.004)	–0.028 (0.004)	–0.028 (0.008)
Rice	0 –	0.28 (0.51)	0.30 (0.54)	0.33 (0.55)	–0.006 (0.003)	–0.014 (0.002)	– 0.016 (0.004)	–0.016 (0.005)
Sugar	0.94 (0.49)	2.27 (0.81)	2.43 (1.03)	2.35 (0.99)	–0.010 (0.001)	–0.020 (0.002)	– 0.019 (0.002)	–0.019 (0.003)
Tea	0 –	0.57 (0.36)	0.95 (0.51)	0.89 (0.46)	–0.006 (0.005)	–0.011 (0.002)	–0.014 (0.004)	– 0.014 (0.005)
Tin	0.63 (0.43)	0.26 (0.21)	0 –	0 –	–0.019 (0.005)	–0.015 (0.005)	–0.014 (0.003)	– 0.017 (0.002)
Wheat	0 –	1.11 (0.77)	1.18 (0.80)	0 –	–0.012 (0.004)	– 0.033 (0.005)	–0.034 (0.005)	–0.025 (0.005)

Notes: The preferred model values are in boldface and in parentheses the asymptotic standard errors obtained using the delta method. Storage costs are expressed unit-free as a percentage of the ergodic mean price: a . The price elasticity of demand is evaluated at the ergodic mean price using the coefficient of variation of production (table 3.13 in the appendix).

In the model without trend, our implied price elasticities of consumption are comparable to those derived from other estimations of the storage model (see table 4 in Guerra et al., 2015). If we focus on the cereals, although these elasticities are plausible, in absolute value they appear to be in the low range of the elasticities in the literature (e.g., Seale and Regmi, 2006, Adjemian and Smith, 2012, Roberts and Schlenker, 2013). We would expect smaller elasticities than in most of the literature because most estimation methods do not account for the presence of stocks which tend to create a positive bias. Nevertheless, even Roberts and

Schlenker (2013) who control for the effect of storage using instrumental variables find higher elasticities of demand, between -0.066 and -0.028 for aggregate calories from maize, rice, soybeans and wheat, and even higher values for each commodity individually.

3.3.4 MODELS WITH A TIME TREND

The parameter estimates for the model with a linear trend are given in table 3.5. Since for numerical stability the time variable has been defined over the interval $[-1, 1]$, the trend coefficient g_1 is not directly interpretable. To make it interpretable, we report it also as annual growth rates in column G , where the standard deviation is calculated using the Delta method. For all commodities except tin, the annual growth rate is negative, which is consistent with the Prebisch-Singer hypothesis of a long-run downward trend in commodity prices. If we exclude coffee and tin, the values range from an annual decline of 0.4 percent for copper to 1.94 percent for rice. The significance of many trend coefficients indicates that the model without trend is likely to be misspecified.

For the other trend specifications, since the trend and the structural parameters are not directly interpretable, the complete results are not displayed here. They are provided in the appendix, along with a figure plotting the various trends with real prices. Rather than presenting detailed results, table 3.4 presents the parameters estimates expressed in a way that makes them comparable across trend specifications. The presence of a deterministic time trend in the model estimation can lead to large effects in terms of the key parameter estimates. Storage costs tend to increase when there is a trend, and also price elasticity of demand in absolute value. With the preferred model (in boldface) ten out of the thirteen commodities present higher storage costs than if there is no trend. With the exception of tin, all price elasticities are higher with the preferred model. The differences between the elasticities estimated with the models without trend and with the preferred models with trend are important. The elasticities double in the case of cocoa, coffee, jute, rice, sugar, and tea, and increase three-fold for maize and wheat.

For cereals, the elasticities of the preferred model although still low appear to be more consistent with the literature. Similarly, the increase in storage costs for cereals leads to more plausible parameters which nevertheless are low compared to some published figures.

For sugar, we can compare the parameter estimates to the Conditional Maximum Likelihood estimates of Cafiero et al. (2015). They estimate their model on data from 1921 to 2009, because of a possible structural break between 1920 and 1921. On this subsample, the stationarity of deflated prices is more likely to hold (see figure 3.4 in the appendix) and the first-order autocorrelation at 0.63 is lower than the 0.70 obtained over our extended sample. The purpose of our joint estimation approach is precisely to accommodate for such possible breaks. The preferred model for sugar is the model with a three-knot spline trend. The estimated trend is decreasing at the beginning of the sample and roughly constant after 1930 (figure 3.4 in the appendix). We express the parameters in ratios to make them comparable across specifications. For $100 \cdot k/a$, our estimation is 2.43 (table 3.14 in the appendix) and theirs is 2.23 (Cafiero et al., 2015, Table 3, ML setting $d = 0$). For a/b , our estimation is -0.52 and theirs is -0.49 . The estimations are very close, while they

Table 3.5. Parameter Estimates with a Linear Trend

Commodity	G	g_1	a	b	k	$\log L$	# Stockouts
Banana	-0.0161 (0.0010)	-0.8909 (0.0550)	0.8770 (0.0434)	-0.9756 (0.1114)	0 -	163.4962	0
Cocoa	-0.0058 (0.0034)	-0.3215 (0.1899)	0.2036 (0.0501)	-0.9771 (0.1370)	0.0004 (0.0011)	212.1482	0
Coffee	-0.0000 (0.0022)	-0.0008 (0.1225)	0.2571 (0.0261)	-0.8963 (0.0747)	0.0015 (0.0009)	191.9992	0
Copper	-0.0040 (0.0009)	-0.2218 (0.0505)	0.6227 (0.0515)	-0.9837 (0.1082)	0.0068 (0.0042)	122.0631	0
Cotton	-0.0045 (0.0148)	-0.2476 (0.8197)	1.5846 (1.4137)	-5.3011 (8.1716)	0.0031 (0.0062)	118.6970	0
Jute	-0.0108 (0.0014)	-0.6014 (0.0784)	0.5357 (0.0856)	-1.3389 (0.1182)	0.0023 (0.0051)	97.4204	0
Maize	-0.0097 (0.0012)	-0.5386 (0.0671)	0.6957 (0.0694)	-1.3722 (0.1400)	0.0074 (0.0057)	83.6162	0
Palm oil	-0.0179 (0.0014)	-0.9921 (0.0763)	0.4775 (0.0491)	-0.8150 (0.0743)	0.0057 (0.0043)	118.5360	1
Rice	-0.0194 (0.0020)	-1.0755 (0.1119)	0.6286 (0.0647)	-1.2003 (0.1323)	0.0017 (0.0032)	125.2477	1
Sugar	-0.0107 (0.0005)	-0.5955 (0.0282)	0.5811 (0.0415)	-1.0836 (0.0725)	0.0132 (0.0046)	59.2928	5
Tea	-0.0134 (0.0034)	-0.7430 (0.1904)	0.7637 (0.0623)	-1.4313 (0.2095)	0.0043 (0.0027)	143.2308	0
Tin	0.0143 (0.0046)	0.7932 (0.2552)	0.4341 (0.0709)	-1.5516 (0.4729)	0.0011 (0.0009)	206.4246	0
Wheat	-0.0127 (0.0011)	-0.7033 (0.0600)	0.7133 (0.0531)	-0.9266 (0.1104)	0.0079 (0.0055)	103.8497	1

Notes: Asymptotic standard errors in parentheses. Column G is a transformation into an annual growth rate of the trend parameter g_1 . Column # Stockouts indicates the number of times the cyclical prices are greater than or equal to the cutoff price for no storage: $\sum_{t=1}^T 1_{P_t^{\text{sto}} \geq P^*}$.

are very different if we use our estimation without trend ($100 \cdot k/a = 0.94$ and $a/b = -0.27$). This could indicate that for sugar our strategy succeeds in removing a source of non-stationarity in the original series.

3.3.5 MODEL PREDICTIONS

Since one of the main critiques of the storage model is its inability to reproduce the observed serial correlation, one way to assess our new estimates is to compare the model predictions to the features of the data. For samples of the same length of the observables, a storage model generates moments that are highly volatile, so comparing the ergodic moments and observed moments would be inappropriate. We adopt the approach in Cafiero et al. (2011b): we match the observed moments to their corresponding percentiles in the ergodic distribution of the estimated model. The model predictions are consistent with the data when the percentiles

are neither too low nor too high. We calculate the mean, first- and second-order autocorrelations, coefficient of variation, skewness, and kurtosis for the observations. For the model with trend, the moments are calculated on the cyclical component of prices, P^{sto} , which is the component that the storage model is supposed to explain. We calculate the corresponding percentiles using 1,000,000 series of 112 periods from the asymptotic distribution.

The moments and their localization with respect to simulated percentiles are given in table 3.3 for the model without trend and in table 3.6 for the preferred model with trend. All moments from the observations are located within the implied empirical distribution of the models without and with trend. As already noted by Cafiero et al. (2011b), if the model without trend is solved and estimated with a sufficiently precise grid, it is able to generate first-order autocorrelation similar to the observations for several commodities (table 3.3), but except for sugar the observed autocorrelation corresponds to high model percentiles. The storage model even appears to fail more often to reproduce the skewness and kurtosis, with observed moments which are frequently below the 0.5 and 2.5 percentiles calculated from the estimated model. It should be noted that the banana and tea price series present negative skewness, which makes them nearly impossible to reproduce with a storage model which on average generates positive skewness. When a commodity presents negative excess kurtosis, which is the case of banana, cotton, jute, rice and tea, it seems that the estimated model has difficulty reproducing it. Deaton and Laroque (1992, section 2.1) note that the storage model can produce negative excess kurtosis but only from a calibration with low price volatility and a limited role for storage, which does not correspond to our estimations.

We turn next to the predictions of the preferred model with trend (table 3.6). Compared to the model without trend, several commodities show an improvement in the model predictions with many moments closer to central percentiles. However, the predictions for some commodities – banana, jute, and tea – do not improve. The storage model with the specifications we estimated seems unable to match the moments for these three commodities. Due to the deterministic trend, observed first-order autocorrelation decreases but does not become systematically more consistent with the model predictions, because with estimations of higher storage costs and more elastic demand the capacity of the storage model to generate high serial correlation decreases also. For cocoa and maize, the percentiles corresponding to the observed first-order autocorrelation increase significantly toward higher values indicating a decrease in the ability of the model to reproduce this moment. Regarding the second-order autocorrelation, the skewness, and the excess kurtosis, the preferred detrended models are much more able to fit the observed moments than the models without trend. Similarly, if we exclude banana, jute and tea, and with the exception of 3 moments that are outside of the (2.5, 97.5) percentiles, all other moments are consistent with the predictions of the estimated storage models.

A disturbing feature of the estimations without trend is the very small number (often zero) of implied stockouts. Considering the possibility of a trend increases the number of implied stockouts, which becomes positive for many commodities (table 3.7). However, even if we exclude banana, jute and tea, three commodities – cocoa, copper, and cotton – present zero stockouts.

It is interesting to compare the number of implied stockouts to the probabilities of exceeding a given

Table 3.6. Comparisons of Data Features and Predictions of the Preferred Models

Commodity	Variable	Mean	One-year a-c	Two-year a-c	Coefficient of variation	Skewness	Excess kurtosis
Banana	Observed moments	0.66	0.89	0.81	0.41	1.66	3.25
	Model percentiles	0.00	99.91	99.85	52.12	16.70	14.11
Cocoa	Observed moments	0.43	0.82	0.65	0.61	1.76	3.00
	Model percentiles	41.42	87.37	78.94	43.42	25.63	19.62
Coffee	Observed moments	0.21	0.78	0.59	0.47	1.86	5.97
	Model percentiles	17.51	89.71	79.53	12.28	24.70	34.73
Copper	Observed moments	0.47	0.80	0.58	0.38	0.81	0.32
	Model percentiles	4.15	96.49	85.48	8.47	2.51	2.07
Cotton	Observed moments	0.79	0.66	0.43	0.45	3.38	19.96
	Model percentiles	1.10	50.83	30.57	14.14	78.57	86.69
Jute	Observed moments	0.62	0.69	0.40	0.31	0.62	0.17
	Model percentiles	16.66	94.09	66.04	1.86	0.34	0.32
Maize	Observed moments	0.85	0.69	0.46	0.36	1.47	2.79
	Model percentiles	14.25	97.76	89.60	11.28	13.80	20.66
Palm oil	Observed moments	0.42	0.72	0.47	0.39	0.99	1.38
	Model percentiles	23.12	82.59	57.23	7.25	4.54	5.59
Rice	Observed moments	0.97	0.76	0.46	0.38	2.17	7.07
	Model percentiles	9.98	85.62	48.62	13.20	37.65	43.28
Sugar	Observed moments	0.93	0.62	0.35	0.67	3.00	13.73
	Model percentiles	41.58	61.20	28.82	66.35	79.40	83.03
Tea	Observed moments	0.67	0.91	0.85	0.46	0.46	0.01
	Model percentiles	0.06	99.97	99.97	38.81	0.53	1.24
Tin	Observed moments	0.11	0.80	0.65	0.58	1.63	3.27
	Model percentiles	15.62	71.70	67.45	33.05	26.89	26.53
Wheat	Observed moments	0.57	0.75	0.45	0.31	1.26	2.17
	Model percentiles	4.09	94.87	64.47	2.55	6.11	6.88

Note: There are two variables for each commodity: the moments calculated on the cyclical component of prices, P^{st0} , and below the percentiles corresponding to these moments calculated from the estimated model using samples of the same size as the data.

number of stockouts. The probabilities of stockouts are calculated in the same way as the price moments using 1,000,000 series of 112 periods from the asymptotic distribution. The results for the model without trend and for the preferred model with trend for at least 1, 2, 3, 5, and 10 stockouts are given in table 3.8. Models with trend have much higher probabilities of stockouts than the model without trend. If there is a trend, the storage costs and the price elasticities are higher than without trend which discourages storage and leads to higher probabilities of stockouts. Apart from cocoa, cotton and tin, with the preferred model samples without stockouts are highly unlikely. Even samples with only one stockout are fairly unlikely. The parameterization implied by the estimation of a model with trend is much more favorable to occasional stockouts and so provides a natural explanation for price spikes as periods where stocks are exhausted.

Table 3.7. Number of Implied Stockouts over the Sample Interval

Commodity	No trend	Linear	RCS3	RCS4
Banana	0	0	0	0
Cocoa	0	0	0	0
Coffee	0	0	1	2
Copper	0	0	0	4
Cotton	0	0	0	0
Jute	0	0	4	8
Maize	0	0	3	12
Palm oil	1	1	1	1
Rice	0	1	1	1
Sugar	3	5	8	16
Tea	0	0	0	0
Tin	0	0	0	6
Wheat	0	1	1	0

Notes: The preferred model values in boldface. The number of implied stockouts is calculated as the number of times the cyclical prices are greater than or equal to the cutoff price for no storage: $\sum_{t=1}^T 1_{p_t^{\text{sto}} \geq p^*}$. For the specification without trend, cyclical prices are just observed prices.

Table 3.8. Probabilities of at Least n Stockouts, in Samples of the Same Size as the Data

Commodity	No-trend model					Preferred model				
	$n = 1$	$n = 2$	$n = 3$	$n = 5$	$n = 10$	$n = 1$	$n = 2$	$n = 3$	$n = 5$	$n = 10$
Banana	0.91	0.81	0.70	0.48	0.13	0.98	0.94	0.89	0.73	0.30
Cocoa	0.63	0.47	0.35	0.18	0.02	0.86	0.74	0.62	0.39	0.09
Coffee	0.77	0.63	0.49	0.28	0.05	0.95	0.88	0.79	0.59	0.19
Copper	0.95	0.88	0.79	0.59	0.19	0.98	0.94	0.88	0.72	0.29
Cotton	0.75	0.60	0.47	0.26	0.05	0.87	0.75	0.63	0.41	0.10
Jute	0.88	0.77	0.65	0.43	0.10	1.00	0.99	0.99	0.95	0.68
Maize	0.76	0.61	0.48	0.27	0.05	1.00	1.00	1.00	0.99	0.86
Palm oil	0.95	0.88	0.79	0.59	0.19	0.97	0.92	0.86	0.68	0.26
Rice	0.64	0.49	0.36	0.19	0.02	0.95	0.88	0.79	0.59	0.19
Sugar	0.77	0.63	0.49	0.28	0.05	0.98	0.94	0.88	0.73	0.30
Tea	0.74	0.60	0.46	0.26	0.04	0.98	0.94	0.88	0.73	0.30
Tin	0.84	0.71	0.59	0.36	0.08	0.75	0.60	0.46	0.26	0.04
Wheat	0.72	0.57	0.44	0.24	0.04	0.99	0.97	0.93	0.82	0.41

Notes: The preferred model is chosen according to the AIC of table 3.1. The probabilities are calculated for each model as the proportion of simulated samples where prices are greater than or equal to the cutoff price for no storage at least n times. The calculation is done on 1,000,000 samples of 112 periods from the asymptotic distribution simulated using the estimated model.

3.4 CONCLUSION

Estimating the competitive storage model on untransformed series of commodity prices leads to very low demand elasticities and storage costs, which results in a prediction of very infrequent, and often zero, stockouts over the sample period. These results may stem from the presence of trends in prices, which could

create statistical features difficult to explain by a storage model.

This chapter proposes a strategy inspired by Canova (2014) to estimate jointly the structural parameters of a storage model and the parameters characterizing the non-cyclical component of prices for which the storage model cannot account. For the non-cyclical component of prices, three deterministic time trends with increasing flexibility were tested and compared with the baseline model which ignores the possibility of a trend.

Our results show that storage models with trend are always preferred to models without trend, and the significance of the trend parameters indicates that the model without trend is likely to be misspecified. Accounting for a trend is quantitatively important for estimating the structural parameters. For most commodities, the storage model with a deterministic trend yields more plausible estimates of the structural parameters (e.g., higher storage costs and demand elasticities). It also increases the probability of observing stockouts, and more closely replicates the most salient features of the price data. For most commodities our results support the empirical relevance of the speculative storage model which is in line with the recent findings in Cafiero et al. (2011b, 2015) and prove that the joint estimation approach is a superior procedure to fit the storage model with the data. Future estimations of the storage model should no longer neglect the possibility of long-run trends in prices.

For banana, jute and tea, three of the commodities originally studied in Deaton and Laroque (1992), the storage model with or without a deterministic trend fails to reproduce the main features of the price dynamics. With the trend specifications considered in this chapter, the storage model is rejected as a relevant model to explain the price dynamics of these commodities. However, other specifications could be explored in the future.

This work is a first step toward jointly analyzing short- and long-run aspects of commodity prices. Our focus was to show the importance of accounting for long-run trends when estimating the storage model, so we have purposefully chosen simple deterministic trends that maintain the tractability of the likelihood, but more sophisticated trend specifications could permit the reconciliation of two branches of the literature that have long been separated. Because commodity prices are characterized by “small trends and big variability” (Cashin and McDermott, 2002), without good explanations for the big short-run variability it is challenging to identify the trends. Conversely, neglecting trends, even small ones, creates difficulties to explain the short-run variability. To really integrate these two issues, several challenges will have to be faced. A storage model in which agents account for trends implies theoretical restrictions such as an isoelastic demand function that create numerical difficulties for the solution method. More sophisticated trends specifications such as random walk with drift or log-linear trend with Markov switching slope would prevent a direct calculation of the likelihood and would require the use of filters for non-linear state-space models (see e.g., Fernández-Villaverde and Rubio-Ramírez, 2007, for use of the particle filter to estimate macroeconomic models). Some of the pieces are already provided in Zeng (2012), with a storage model including a structural log-linear trend in prices, and Dvir and Rogoff (2014), with a storage model including a trend for quantities following a random walk with drift, but further elaborations are needed to reach the level of sophistication achieved in the literature on trends (Ghoshray, 2011).

3.A NUMERICAL METHOD

There is no closed-form solution for the equilibrium price function, which has to be approximated numerically. The numerical method follows the fixed-point approach proposed by Deaton and Laroque (1992). The equilibrium price function is approximated with a cubic spline over a grid of equally spaced availability points lying between -2 and 20 . The expectation term in equation (3.5) is replaced by a sum by discretizing the truncated normal distribution of the production shocks ε using a Gaussian quadrature calculated by the method of moments, with $N = 10$ nodes, where the production shocks and their associated probabilities are denoted ε^n and π^n . Then, using that production shocks are i.i.d., and combining (3.5) and (3.6) we have

$$\mathcal{P}(A) = \max \left[\beta \sum_{n=1}^N \pi^n \mathcal{P}(A - D(\mathcal{P}(A)) + \varepsilon^n) - k, D^{-1}(A) \right]. \quad (3.20)$$

The model is solved by iterating on this functional equation. Starting from a first guess for the price function, a price function applied on the right-hand side to all grid points leads by simple arithmetic operations to new values of the price function at the grid points on the left-hand side. The iterations stop when the Euclidean distance between two consecutive price functions at the interpolating nodes falls below a given tolerance threshold which we set to 10 decimal places.

Cafiero et al. (2011b) show that the estimation procedure is very sensitive to the accuracy of the model's numerical solution, which is determined mainly by the number of grid points used to approximate the policy function $\mathcal{P}(A)$. These authors show that Deaton and Laroque (1996) approximate the policy function on a grid that is too sparse to locate accurately the kink at the cutoff price P^* of empty stocks, which partly explains the inability of the storage model to generate the high serial correlation. Using a finer grid of 1,000 nodes, Cafiero et al. (2011b) obtain estimations of the parameters for which the storage model induces higher price autocorrelations. We retain their findings and choose a grid of 1,000 points.

3.B COMPUTATIONAL DETAILS

The results were obtained using MATLAB R2014a on a PC with two quad-core processors Intel Xeon E5345 (2.33 GHz) with 32 GB of RAM running Ubuntu 12.04.5 64 bits. The maximization of the log-likelihood was done using Vaz and Vicente's (2007) free particle swarm pattern search software PSwarm version 2.1¹⁴ and the MATLAB function `fmincon` available in MATLAB Optimization Toolbox. The Monte-Carlo simulations have been performed using MATLAB's default random number generator with the seed set to 1. The Gaussian quadrature was calculated using a MATLAB's function from John Burkardt's website.¹⁵ For a unit normal distribution truncated at five standard deviations, the Gaussian quadrature with 10 nodes has nodes $\varepsilon^n = \{\pm 4.4576, \pm 3.3999, \pm 2.3838, \pm 1.4132, \pm 0.4684\}$ and weights $\pi^n = \{1.9834 \times 10^{-5}, 1.2876 \times 10^{-3}, 2.3048 \times 10^{-2}, 0.14029, 0.33536\}$.

¹⁴ <http://www.mat.uc.pt/~lnv>

¹⁵ http://people.sc.fsu.edu/~jburkardt/m_src/truncated_normal_rule/truncated_normal_rule.html

3.C SMALL SAMPLE PROPERTIES

In this section, we assess using Monte Carlo experiments the small sample properties of the simulated Unconditional Maximum Likelihood estimator (UML) we developed, and compare them to those of the Conditional Maximum Likelihood estimator (CML) proposed in Cafiero et al. (2015). From equation (3.19), the conditional log-likelihood without trend is obtained by removing the terms corresponding to the marginal likelihood:

$$\log L^C(\theta; P_{1:T}^{\text{obs}}) = -\frac{T-1}{2} \log 2\pi - (T-1) \log [\Phi(5) - \Phi(-5)] \\ + \sum_{t=2}^T \log \left| \mathcal{P}^{-1'}(P_t^{\text{obs}}) \right| - \sum_{t=2}^T (1_{|\varepsilon_t| \leq 5} \cdot \varepsilon_t^2 + 1_{|\varepsilon_t| > 5} \cdot \infty) / 2. \quad (3.21)$$

Following Michaelides and Ng (2000) and Cafiero et al. (2015), we conduct four Monte Carlo experiments varying the parameterization and the length of the samples. The first set of parameters are $a = 1$, $b = -1$, and $k = 0.02$, which implies a storage cost of 2% of the mean price and, for supply shocks with a coefficient of variation of 5%, a demand elasticity of -0.05 in the range of the best estimates obtained by Roberts and Schlenker (2013) on a caloric aggregate of major crops, but slightly higher in absolute value than our estimated elasticities. The second parameterization only differs by the value of b , now equal to -2 . This rotation of the slope of the demand function around its mean halves the demand elasticity making this parameterization more favorable to storage, and closer to the values found in the chapter. For each set of parameters, we solve for the equilibrium price function on a grid of 1,000 points, and obtain 3,000 prices series of length $T = 50$ and $T = 100$ from the asymptotic distribution. The price series are obtained by the simulation of 3,000 trajectories starting from the steady-state availability and discarding the first 50 periods as burn-in periods.

The numerical methods follow what was described previously, but differ on two aspects. Firstly, to prevent the availability corresponding to the cutoff price to be below the lower bound of the grid of interpolation points, the lower bound is changed from being -2 to being -5 , the minimum availability. Secondly, since the log-likelihood optimization behaves better on simulated samples, we use a faster optimization algorithm: the generalized pattern search algorithm implemented by the MATLAB function `patternsearch` available in MATLAB Global Optimization Toolbox. The optimization starts from initial values randomly drawn in the range between 80% and 120% of the true values. If the optimization solver fails to converge for one of the two estimators, we discard the corresponding samples for both estimators. The results of valid estimates obtained on common samples are given in table 3.9 and 3.10.

The results of the Monte Carlo experiments are similar to those obtained for the CML in Cafiero et al. (2015). They show that the two maximum likelihood estimators yield precise estimates of the parameters of the model, especially for a and b . The storage cost, k , is less precisely estimated with Root Mean Square Errors (RMSE) always above 26%. For all parameters, the bias is small, most of the RMSE being explained by the standard deviation of the estimations.

Table 3.9. Comparison of Monte Carlo Experiment Results with Parameterization $a = 1$, $b = -1$, and $k = 0.02$

	UML			CML		
	a	b	k	a	b	k
$T = 50$						
Mean	0.9930	-0.9720	0.0193	0.9932	-0.9745	0.0194
Standard deviation	0.0650	0.1297	0.0059	0.0668	0.1344	0.0058
Bias	-0.0070 (0.70%)	0.0280 (2.80%)	-0.0007 (3.40%)	-0.0068 (0.68%)	0.0255 (2.55%)	-0.0006 (3.14%)
RMSE	0.0654 (6.54%)	0.1326 (13.26%)	0.0059 (29.67%)	0.0671 (6.71%)	0.1368 (13.68%)	0.0058 (29.24%)
$T = 100$						
Mean	0.9951	-0.9854	0.0196	0.9944	-0.9875	0.0194
Standard deviation	0.0510	0.1066	0.0053	0.0516	0.1070	0.0052
Bias	-0.0049 (0.49%)	0.0146 (1.46%)	-0.0004 (2.17%)	-0.0056 (0.56%)	0.0125 (1.25%)	-0.0006 (2.75%)
RMSE	0.0512 (5.12%)	0.1076 (10.76%)	0.0053 (26.70%)	0.0519 (5.19%)	0.1077 (10.77%)	0.0053 (26.26%)

Notes: The price samples for which one estimator does not converge are discarded. For $T = 50$, the total number of valid replications is 2,737 for UML and 2,733 for CML. For $T = 100$, it is 2,841 for UML and 2,846 for CML. The table reports the 2,593 and 2,764 valid estimates obtained on common samples for the short and long samples.

Table 3.10. Comparison of Monte Carlo Experiment Results with Parameterization $a = 1$, $b = -2$, and $k = 0.02$

	UML			CML		
	a	b	k	a	b	k
$T = 50$						
Mean	0.9793	-1.9639	0.0194	0.9772	-1.9695	0.0193
Standard deviation	0.1280	0.3202	0.0085	0.1351	0.3250	0.0085
Bias	-0.0207 (2.07%)	0.0361 (1.80%)	-0.0006 (3.14%)	-0.0228 (2.28%)	0.0305 (1.52%)	-0.0007 (3.69%)
RMSE	0.1296 (12.96%)	0.3222 (16.11%)	0.0085 (42.51%)	0.1370 (13.70%)	0.3265 (16.32%)	0.0085 (42.45%)
$T = 100$						
Mean	0.9848	-1.9838	0.0195	0.9825	-1.9860	0.0194
Standard deviation	0.1055	0.2592	0.0074	0.1090	0.2611	0.0076
Bias	-0.0152 (1.52%)	0.0162 (0.81%)	-0.0005 (2.56%)	-0.0175 (1.75%)	0.0140 (0.70%)	-0.0006 (3.14%)
RMSE	0.1065 (10.65%)	0.2597 (12.99%)	0.0074 (36.94%)	0.1104 (11.04%)	0.2615 (13.08%)	0.0076 (38.02%)

Notes: The price samples for which one estimator does not converge are discarded. For $T = 50$, the total number of valid replications is 2,820 for UML and 2,767 for CML. For $T = 100$, it is 2,899 for UML and 2,890 for CML. The table reports the 2,674 and 2,839 valid estimates obtained on common samples for the short and long samples.

For all parameterizations, the estimators perform better when the sample length increases. For the UML, a doubling of the sample length from 50 to 100 observations reduces the RMSE by 17% for both parameterizations. The CML benefits slightly more than the UML from an increase in the sample size. Indeed, they have similar RMSE for the long samples, but the UML performs better on the short samples. Regarding the influence of the parameterization, we observe that the parameterization more favorable to storage yields less precise estimates as all the RMSE of table 3.10 are higher than in table 3.9.

3.D SUPPLEMENTARY TABLES

Table 3.11. Descriptive Statistics of Observed Prices and Detrended Prices after Hodrick-Prescott Filtering with Smoothing Parameter 400

Commodity	Observed prices				Detrended prices			
	One-year a-c	Two-year a-c	Coeff. of variation	Skewness	One-year a-c	Two-year a-c	Coeff. of variation	Skewness
Banana	0.95	0.90	0.23	-0.27	0.51	0.11	0.09	-0.56
Cocoa	0.86	0.71	0.60	1.24	0.56	0.11	0.29	1.33
Coffee	0.84	0.68	0.50	1.61	0.56	0.22	0.28	1.25
Copper	0.83	0.64	0.40	0.90	0.61	0.14	0.22	0.87
Cotton	0.94	0.85	0.51	0.20	0.57	0.06	0.19	0.48
Jute	0.84	0.70	0.44	0.41	0.43	-0.06	0.22	0.83
Maize	0.86	0.73	0.51	0.84	0.48	0.03	0.22	0.96
Palmoil	0.82	0.65	0.60	2.43	0.51	0.07	0.28	2.72
Rice	0.91	0.79	0.50	0.42	0.59	0.09	0.22	1.24
Sugar	0.70	0.51	0.69	1.62	0.42	0.01	0.44	2.96
Tea	0.90	0.81	0.38	-0.02	0.46	0.03	0.15	0.48
Tin	0.90	0.78	0.47	1.48	0.58	0.17	0.21	0.31
Wheat	0.91	0.79	0.47	0.82	0.61	0.12	0.22	1.11

Table 3.12. Likelihood Ratio Test Statistics for the Models for Which k is not at its Lower Bound

Commodity	Linear	RCS3	RCS4
Banana	-	-	-
Cocoa	1.28	8.25**	16.43***
Coffee	0.00	5.87*	5.84
Copper	2.08	2.28	5.25
Cotton	0.21	8.86**	8.56**
Jute	4.80**	14.36***	14.33***
Maize	1.65	4.29	12.14***
Palm oil	11.27***	12.69***	13.47***
Rice	-	-	-
Sugar	19.56***	22.46***	22.67***
Tea	-	-	-
Tin	0.44	-	-
Wheat	-	-	-

Notes: The preferred model values are in boldface. For each ratio the denominator is the log-likelihood of the model without trend. ***, **, and * denote significance of the test at the 1%, 5%, and 10% levels respectively.

Table 3.13. Production Variation, 1961–2011

Commodity	Production CV (%)	Commodity	Production CV (%)
Banana	3.67	Palm oil	4.65
Cocoa	7.13	Rice	2.75
Coffee	7.68	Sugar	3.65
Copper	4.46	Tea	2.07
Cotton	7.20	Tin	5.52
Jute	11.35	Wheat	4.34
Maize	5.84		

Notes: The coefficients of variation (CV) are obtained by calculating the standard deviation of the detrended logarithm of observed production, modeling the trend using a restricted cubic splines with five knots.

Table 3.14. Parameter Estimates with 3-Knot Spline Trend

Commodity	g_1	g_2	a	b	k	$\log L$	# Stockouts
Banana	-0.3323 (0.2804)	-1.2359 (0.2011)	1.3237 (0.2013)	-1.6729 (0.4397)	0 -	170.6770	0
Cocoa	-1.5599 (0.8803)	0.7076 (0.3317)	0.3679 (0.1595)	-1.7978 (0.9285)	0.0002 (0.0008)	215.6308	0
Coffee	0.0925 (0.3314)	-0.6813 (0.1557)	0.2522 (0.0455)	-0.5265 (0.1072)	0.0036 (0.0025)	194.9321	1
Copper	-0.4176 (0.1943)	-0.2464 (0.1424)	0.7348 (0.0789)	-1.1835 (0.1589)	0.0073 (0.0051)	122.1660	0
Cotton	-0.6422 (0.8240)	-2.0878 (0.3217)	1.5367 (0.4016)	-3.7632 (1.6051)	0.0053 (0.0065)	123.0208	0
Jute	-0.3974 (0.0756)	-0.9164 (0.0554)	0.6917 (0.0481)	-0.7573 (0.0401)	0.0163 (0.0062)	102.1980	4
Maize	-0.6588 (0.1101)	-0.8850 (0.0815)	0.9504 (0.0816)	-1.5377 (0.1432)	0.0128 (0.0075)	84.9322	3
Palm oil	-1.7887 (0.1181)	-1.2443 (0.0539)	1.0411 (0.0981)	-1.7009 (0.1865)	0.0146 (0.0091)	119.2428	1
Rice	-1.5405 (0.3035)	-1.4251 (0.1417)	1.2128 (0.1914)	-2.0786 (0.3684)	0.0037 (0.0066)	127.1550	1
Sugar	-1.2627 (0.1028)	-0.2394 (0.1652)	0.9701 (0.0809)	-1.8482 (0.1738)	0.0235 (0.0098)	60.7431	8
Tea	-0.9290 (0.3585)	-1.1775 (0.1357)	1.1089 (0.2085)	-1.6789 (0.4149)	0.0105 (0.0053)	144.1925	0
Tin	1.7957 (0.4707)	-0.7677 (0.2843)	0.1940 (0.0244)	-0.7567 (0.1185)	0 -	209.3322	0
Wheat	-1.2473 (0.1482)	-0.8441 (0.1517)	1.2069 (0.1069)	-1.5449 (0.2021)	0.0143 (0.0096)	104.0772	1

Notes: Asymptotic standard errors in parenthesis. Column # Stockouts indicates the number of times the cyclical prices are greater than or equal to the cutoff price for no storage: $\sum_{t=1}^T 1_{p_t^{\text{sto}} \geq p^*}$.

Table 3.15. Parameter Estimates with 4-Knot Spline Trend

Commodity	g_1	g_2	g_3	a	b	k	$\log L$	# Stockouts
Banana	-0.5940 (0.2995)	-0.2663 (0.3033)	-1.5903 (0.2712)	1.2033 (0.1735)	-1.5061 (0.3602)	0 -	171.7633	0
Cocoa	0.2862 (0.2857)	-2.6193 (0.5337)	0.3417 (0.4282)	0.4498 (0.0981)	-1.1874 (0.2765)	0.0024 (0.0028)	219.7236	0
Coffee	0.1199 (0.1792)	0.0281 (0.3230)	-0.7565 (0.1351)	0.2339 (0.0495)	-0.4885 (0.0898)	0.0033 (0.0024)	194.9185	2
Copper	0.6214 (0.3452)	-0.8595 (0.3155)	-0.2444 (0.1968)	0.7416 (0.1155)	-1.7526 (0.3542)	0.0005 (0.0044)	123.6516	4
Cotton	-0.2545 (0.7621)	-1.1035 (0.8597)	-2.2689 (0.4857)	1.4300 (0.5264)	-3.5214 (2.0232)	0.0049 (0.0069)	122.8690	0
Jute	-0.0613 (0.1039)	-0.6035 (0.1805)	-0.9908 (0.0710)	0.6967 (0.0797)	-0.7614 (0.0715)	0.0163 (0.0066)	102.1845	8
Maize	0.0815 (0.1073)	-1.1899 (0.0887)	-1.1229 (0.0576)	0.9358 (0.0481)	-0.8819 (0.0508)	0.0304 (0.0068)	88.8597	12
Palm oil	-0.9208 (0.1402)	-1.6398 (0.3924)	-1.5053 (0.1190)	0.9971 (0.1744)	-1.6352 (0.3267)	0.0142 (0.0095)	119.6359	1
Rice	-0.8285 (0.2131)	-1.7697 (0.4977)	-1.6808 (0.1837)	1.2815 (0.3139)	-2.2062 (0.5310)	0.0042 (0.0070)	127.1070	1
Sugar	-0.6992 (0.1369)	-1.3979 (0.2635)	-0.3698 (0.2479)	1.1136 (0.1329)	-2.0999 (0.2176)	0.0262 (0.0106)	60.8484	16
Tea	-1.4922 (0.3475)	-0.4250 (0.4818)	-1.8818 (0.2257)	1.1959 (0.2308)	-1.7916 (0.4785)	0.0107 (0.0051)	145.6865	0
Tin	1.7411 (0.5157)	1.1081 (0.2943)	-0.2441 (0.1589)	0.1517 (0.0113)	-0.5043 (0.0414)	0 -	210.3823	6
Wheat	-0.1494 (0.1744)	-1.9057 (0.3087)	-0.9026 (0.1902)	1.3447 (0.1606)	-2.3618 (0.3405)	0 -	105.8230	0

Notes: Asymptotic standard errors in parenthesis. Column # Stockouts indicates the number of times the cyclical prices are greater than or equal to the cutoff price for no storage: $\sum_{t=1}^T 1_{P_t^{\text{sto}} \geq P^*}$.

3.E SUPPLEMENTARY FIGURES

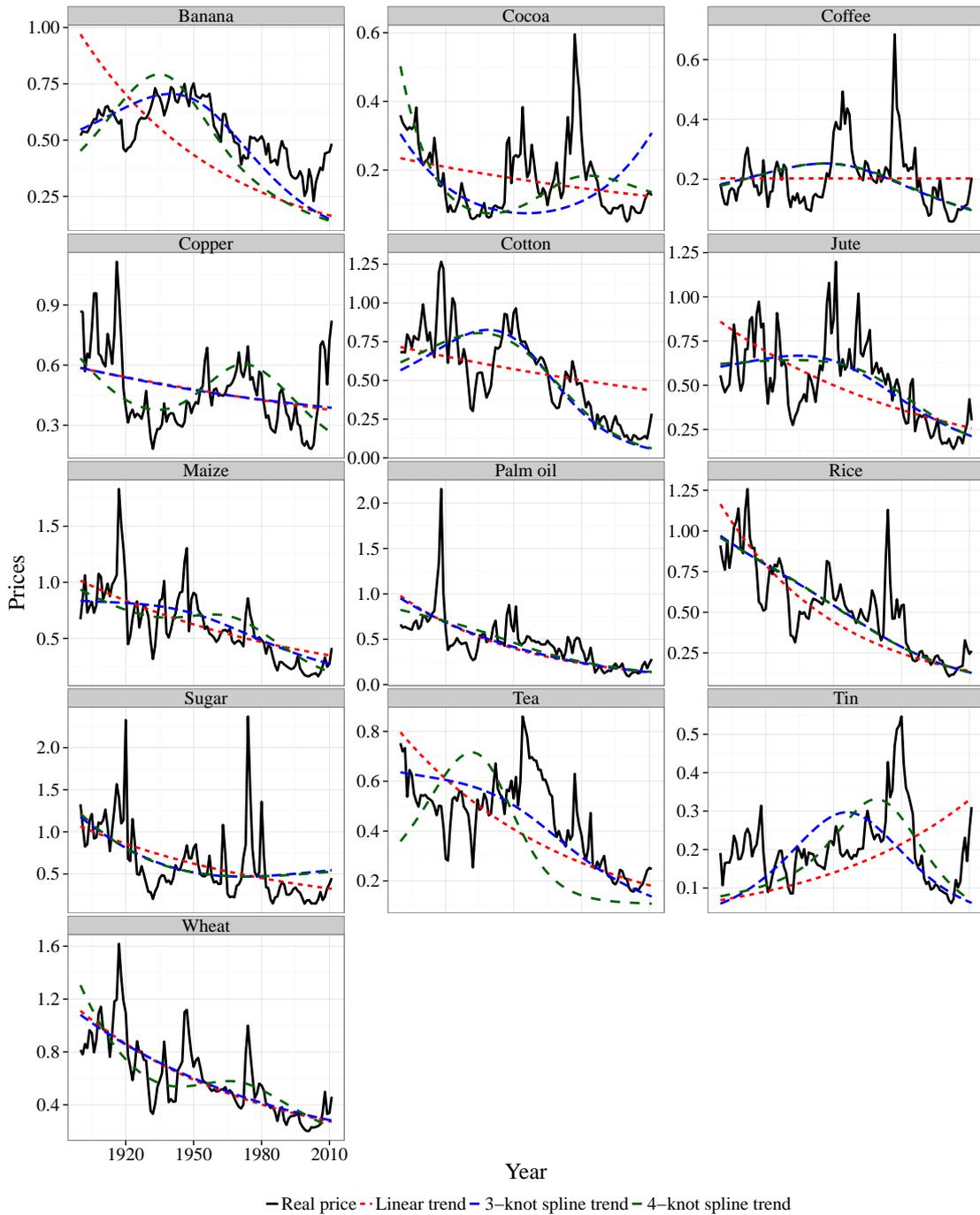


Figure 3.4. Price trends

CHAPTER 4

BAYESIAN ESTIMATION OF THE STORAGE MODEL USING INFORMATION ON QUANTITIES

In research on commodity prices behavior's, the rational expectations storage model of Gustafson (1958) has become the workhorse model for prices formation and commodity market volatility studies. In the model, the dynamics of commodity prices is explained by real shocks to supply and demand influencing the decisions made by optimizing forward-looking agents. Although the theoretical foundations of the storage model are well grounded, its empirical validity continues to be challenged. In pathbreaking papers, Deaton and Laroque (1992, 1996) cast doubt on its relevance because of its inability to generate the observed high levels of autocorrelation in prices. This serial correlation puzzle has been partially solved in part through several refinements to improve the accuracy of the numerical methods (Cafiero et al., 2011b), the development of a Maximum Likelihood estimator (Cafiero et al., 2015), the choice of the data used (Guerra et al., 2015), and management of the trend (Gouel and Legrand, 2016b). However, all these previous estimations are based only on prices information, and ignore the data on quantities, although these would introduce some noise. Another problem with price-only estimations is that many parameters, such as those related to the supply process, are left unidentified. So these estimations have to assume an inelastic supply which is modeled by a unit normal random shock.

In this chapter, we develop a new econometric approach to the storage model estimation that is able to use observables other than prices by borrowing from the recent literature on the estimation of DSGE models. This new approach allows us to estimate a richer storage model than the specifications previously estimated. For example, our storage model features two structural shocks to supply and demand, instead of only one to supply, and includes producers that react to expected price changes. Now that the literature has showed that the storage model is able to fit price dynamics, it is important to assess whether it is able to do so while also accommodating quantities behavior.

In the standard storage model, when observables other than prices are added, the model presents a stochastic singularity. With only one shock in the model, the combination of observables would not be consistent with the theory leading to a likelihood that would be zero with probability one. To avoid this

problem, we follow the literature on the estimation of DSGE models by adding structural and measurement shocks (Fernández-Villaverde, 2010). Adding shocks of measurement errors may have important consequences for the estimation procedure. These additional shocks may make impossible to recover the state of the model from the observables and so to calculate the likelihood analytically. This situation would call for nonlinear filtering techniques, known as particle filtering. In this preliminary version of the study, we focus on cases such that measurement errors do not prevent the observation of the state, which allows us to have likelihood functions that take analytic form. Because of this restriction, we have to assume that prices are always observed without noise so that a one-to-one mapping exists between prices and market availability. Only consumption and production are assumed to be observed with noise. Depending on the number of structural shocks and observed variables used, we estimate a sequence of model specifications allowing us to analyze how information from consumption and production contributes to parameters' identification. Our most simple specification, with prices as the only observables, leads to the same likelihood function as Cafiero et al. (2015). Starting from Cafiero et al. approach, we build more general likelihood functions in order to accommodate the additional observables. As for other rational expectations models, the likelihood functions are challenging to maximize and we estimate the model using Bayesian methods.

Because this is a new approach to estimating the storage model, we carry the estimations on a sample for which we have good benchmark estimations to which our work can be compared: the global markets for calories coming from maize, rice, soybeans, and wheat from 1961 to 2006. Roberts and Schlenker (2013) use the storage model to motivate the choice of instrumental variables for reduced-form estimations of supply and demand on this market for calories. Aggregating staple foods into calories allows to account for about 75% percent of the global food production and to bypass many issues related to the close substitutability in production and consumption of these major crops, such as the risks of mixing own-price with cross-price elasticities. Even if our elasticities tend to be slightly lower, overall our results are consistent with Roberts and Schlenker's results. Our estimations also predict some stockouts over the estimation sample (2 to 5 depending on the specification), consistent with the rare price spikes observed in the sample.

The remainder of the chapter is organized as follows. Section 4.1 describes the storage model and the solution method. Section 4.2 presents our data and some descriptive statistics. Section 4.3 presents the Bayesian estimation strategy, the chosen priors, and the model's posterior. Section 4.4 concludes.

4.1 THE MODEL

4.1.1 MODEL EQUATIONS

Let consider a model of the world market for a storable staple (here the caloric aggregate of maize, rice, soybeans, and wheat). The storage model is based on Wright and Williams (1982) and is a partial equilibrium model featuring profit-maximizing producers, competitive storers with constant marginal storage costs which can transfer the good across time, and a demand function. We extend Wright and Williams' model to make it consistent with a balanced growth path driven by a deterministic increase in demand and a reduction in marginal production costs.

There are a few differences with respect to the storage models used for previous structural estimations (Deaton and Laroque, 1992, 1996, Cafiero et al., 2011b, 2015). First, in our case supply is elastic to prices while previous models tell us nothing about the agricultural producers' reactions to prices: producers are not represented explicitly and production consists only of an exogenous supply shock. Second, we add another structural shock to demand. Most storage models feature only one structural shock, usually a supply shock, which in fact can be interpreted as a net supply shock. When using information on consumption and production for the estimation, it is useful to have structural shocks corresponding to each observable. To avoid making the numerical method more complex, we assume that demand and supply shocks are additive, which allows us to sum shocks, available stocks and planned production, leading to a model with only one state variable.

PRODUCERS A representative producer makes its production decision and pays for inputs one period before bringing its output to the market. The production choice, made in period t , is denoted \tilde{Q}_t . Realized production differ from planned production by an exogenous additive shock, $\tilde{\eta}_{t+1}^Q$, occurring during the growing season (e.g., a weather disturbance). The producer's problem in period t can be written as

$$\max_{\tilde{Q}_t} (1+r)^{-1} E_t P_{t+1} \left(\tilde{Q}_t + \tilde{\eta}_{t+1}^Q \right) - \tilde{\Psi}_t \left(\tilde{Q}_t \right), \quad (4.1)$$

where r is the real interest rate which is assumed to be fixed, E_t is the expectation operator conditional on period t information, P_{t+1} is the price, and $\tilde{\Psi}_t(\cdot)$ is a differentiable and convex production cost function. The solution to this problem is the following first-order condition

$$(1+r)^{-1} E_t P_{t+1} = \tilde{\Psi}'_t \left(\tilde{Q}_t \right). \quad (4.2)$$

At each period, the producer rationally plants up to the point where the expected marginal benefit equals the marginal production cost.

STORERS Competitive storers are risk-neutral. For storing an amount $\tilde{S}_t \geq 0$ from period t until $t+1$ they incur a physical cost of storage proportional to the stored quantities, $k\tilde{S}_t$, and an opportunity cost. Assuming rational expectations and taking account of the non-negativity constraint on storage yield the following arbitrage condition

$$(1+r)^{-1} E_t P_{t+1} - P_t - k \leq 0, = 0 \text{ if } \tilde{S}_t > 0. \quad (4.3)$$

FINAL DEMAND Final demand for the good is the sum of a downward sloping demand function $\tilde{D}_t(P_t)$ and a demand shock denoted $\tilde{\eta}_t^D$.

EQUILIBRIUM The market clears when previous stocks plus production equal final demand plus demand for stocks:

$$\tilde{S}_{t-1} + \tilde{Q}_{t-1} + \tilde{\eta}_t^Q = \tilde{D}_t(P_t) + \tilde{\eta}_t^D + \tilde{S}_t. \quad (4.4)$$

BAYESIAN ESTIMATION OF THE STORAGE MODEL USING INFORMATION ON QUANTITIES

TRENDS AND STEADY-STATE GROWTH Consumption and production of food grow steadily over time because of population increase, income growth, or technological progress. To account for this fact, we allow the demand function, the marginal cost function, and the structural shocks to have deterministic trends. Because of the additivity of the market clearing equation, to obtain steady-state growth requires the adoption of multiplicative trends. Detrended variables are expressed without “tilde” and related to their trending counterparts by the following relations

$$\tilde{D}_t(P_t) = (1 + g)^t D(P_t), \quad (4.5)$$

$$\tilde{\Psi}'(\tilde{Q}_t) = \Psi'(Q_t), \quad (4.6)$$

$$\tilde{\eta}_t^Q = (1 + g)^t \eta_t^Q, \quad (4.7)$$

$$\tilde{\eta}_t^D = (1 + g)^t \eta_t^D, \quad (4.8)$$

where g is the assumed growth rate. Equation (4.6) imposes that the downward trend in marginal production costs perfectly offsets the trend in production, leaving prices stationary. Because of the additive nature of equation (4.3) determining the storage level, to be compatible with a steady-state growth any trend in prices will require marginal storage costs, k , either to be zero or to have the same trend as prices, two restrictions which are unlikely to hold. To avoid imposing these restrictions, we ignore potential trends in prices.¹ This set of trend assumptions induces a common multiplicative trend in all quantities: final consumption, production and stocks. Using the convention $\tilde{S}_t = S_t (1 + g)^t$ and $\tilde{Q}_{t-1} = Q_{t-1} (1 + g)^t$, replacing trending quantities by their detrended counterparts in the market clearing equation leads to

$$\frac{S_{t-1}}{1 + g} + Q_{t-1} + \eta_t^Q = D(P_t) + \eta_t^D + S_t. \quad (4.9)$$

The division of S_{t-1} by $1 + g$ illustrates that, on average, stocks have to increase just to meet the pace of increase in production and demand, so detrended beginning stocks are discounted by $1 + g$ to maintain them at a level comparable to other detrended quantities.

STATIONARY EQUILIBRIUM In equation (4.9), four variables are predetermined: stocks, planned production and the two shocks. They can be summed together in a single state variable, availability net of demand shock A_t :

$$A_t \equiv \frac{S_{t-1}}{1 + g} + Q_{t-1} + \eta_t^Q - \eta_t^D. \quad (4.10)$$

The capacity to combine all predetermined variables in one state variable is crucial to simplify numerical resolution of the model and this simplification is allowed by assuming an additive demand shock.

Equation (4.10) is the model’s stationary transition equation. Applying previous transformations to the

¹ See Dvir and Rogoff (2014) for another storage model with trending quantities but without trending prices.

equilibrium equations leads to the following three stationary equilibrium equations:

$$(1+r)^{-1} E_t P_{t+1} = \Psi'(Q_t), \quad (4.11)$$

$$(1+r)^{-1} E_t P_{t+1} - P_t - k \leq 0, = 0 \text{ if } S_t > 0, \quad (4.12)$$

$$A_t = S_t + D(P_t). \quad (4.13)$$

We assume that the stationary demand function takes the following linear form

$$D(P_t) = \bar{D} \left(1 + \alpha^D \frac{P_t - \bar{P}}{\bar{P}} \right), \quad (4.14)$$

where \bar{D} is the steady-state demand (equal also to steady-state production since stocks are not held at the steady state), $\alpha^D < 0$ is the price elasticity of demand at the steady state, and \bar{P} is the steady-state price. Similarly, the stationary marginal cost function is assumed to be linear:

$$\Psi'(Q_t) = (1+r)^{-1} \bar{P} \left(1 + \frac{1}{\alpha^S} \frac{Q_t - \bar{D}}{\bar{D}} \right), \quad (4.15)$$

where $\alpha^S > 0$ is the supply elasticity at the steady state. Because of the assumed specifications in deviation from the deterministic steady state, these demand and marginal cost functions depend only on parameters that can be directly interpreted, which is important for the prior elicitation of the Bayesian analysis.

η_t^Q and η_t^D , the stationary supply and demand disturbances, are assumed to be serially uncorrelated, independent of each other, and are normally distributed with zero mean and standard deviations σ_{η_Q} and σ_{η_D} .

We also estimate a version of the model with inelastic supply. In this case, equation (4.11) is dropped from the model and planned production is fixed at its steady-state level: $Q_t = \bar{D}$. Except for the demand shock and the growth rate g , this version of the storage model is the same as the one estimated in Deaton and Laroque (1992).

4.1.2 MODEL SOLUTION

Equations (4.10)–(4.13) form a non-linear rational expectations system based on the variables A_t , Q_t , S_t , and P_t driven by the innovations $\eta_t = [\eta_t^Q, \eta_t^D]$. This system does not have a closed form solution and must be solved numerically to allow for a structural estimation. Solution of the rational expectations system takes the form of policy functions which describe control variables as functions of the contemporaneous state variable, net availability:

$$Q_t = \mathcal{Q}(A_t), \quad (4.16)$$

$$S_t = \mathcal{S}(A_t), \quad (4.17)$$

$$P_t = \mathcal{P}(A_t), \quad (4.18)$$

to which the transition equation (4.10) must be added.

Combining equations (4.10) to (4.13), one can see that the policy functions for all A_t have to satisfy:

$$\mathcal{P}(A_t) = \max \left[(1+r)^{-1} E_t \mathcal{P} \left(\mathcal{S}(A_t) + \mathcal{Q}(A_t) + \eta_{t+1}^Q - \eta_{t+1}^D \right) - k, D^{-1}(A_t) \right], \quad (4.19)$$

$$(1+r)^{-1} E_t \mathcal{P} \left(\mathcal{S}(A_t) + \mathcal{Q}(A_t) + \eta_{t+1}^Q - \eta_{t+1}^D \right) = \Psi'(\mathcal{Q}(A_t)). \quad (4.20)$$

Equation (4.19) makes clear the existence of two regimes. The first regime holds when speculators stockpile in the expectation of future prices covering the full carrying costs and the purchasing cost. The second regime defines the stockout situation with empty inventories, where the market price is determined only by the final demand for consumption and the net availability in the market. Let us define P^* as the cutoff price above which there is no storage. This cutoff price is the solution to the following nonlinear equation

$$P^* = (1+r)^{-1} E_t \mathcal{P} \left(\mathcal{Q}(D(P^*)) + \eta_{t+1}^Q - \eta_{t+1}^D \right) - k, \quad (4.21)$$

which depends on the policy functions.

A variety of numerical techniques is available to solve rational expectations storage models and approximate the policy functions (Gouel, 2013a). Previous estimations of the storage model relied on the fixed-point algorithm of Deaton and Laroque (1992). This has the advantage that it is very fast because it requires no rootfinding operation. However, it does not apply to models with elastic supply. The numerical algorithm we implement is the endogenous grid method proposed by Carroll (2006), adapted to the storage model in Gouel (2013a). In the case of a model with inelastic supply, like Deaton and Laroque's algorithm it implies simple arithmetic operations only, but no rootfinding. With elastic supply, it is necessary to solve nonlinear equations, but this algorithm is still much faster than the alternatives. One advantage over the approach in Deaton and Laroque is that the endogenous grid method locates precisely the cutoff point of no storage even with a small number of grid points, whereas the fixed-point algorithm requires a large number of grid points (Cafiero et al., 2011b).

To implement the algorithm, the expectations terms in equations (4.11) and (4.12) are replaced by sums by discretizing the normal distribution of the net supply shocks $\eta^Q - \eta^D$ using a Gauss-Hermite quadrature with 11 nodes. We use a regular grid on storage of 50 nodes spanning the interval $[0, \bar{D}]$, where \bar{D} is fixed at 1, its central value in the estimations below. The algorithm stops when successive policy functions cease to differ by more than a given tolerance threshold, set to 10 decimal places. See Gouel (2013a) for more details on the implementation of the algorithm.

4.2 OVERVIEW OF THE GRAINS MARKET

4.2.1 DATA

The data on world quantities for maize, rice, soybeans and wheat come from the Food and Agriculture Organization statistical database (FAOSTAT). Total demand is obtained by subtracting the variation in inventories from total production. Our sample starts in 1961, the first year available in FAOSTAT. It ends

in 2006 because, after that year, the increasing importance of biofuels, supported strongly by US and EU policies, may have changed the behavior of the food markets (biofuel mandates create an additional inelastic demand for food products, while biofuel demand induced by tax credits may link food and oil markets).² Following the approach proposed by Roberts and Schlenker (2013), the four commodities are aggregated together into calories using the conversion ratios in Williamson and Williamson (1942). Figure 4.1 depicts the patterns of the world production and consumption over the sample period. Although production appears more volatile than consumption, both production and consumption grow at the same steady linear rate over time. We need stationary variables for the estimation. Production and consumption are regressed on the same linear time trend. The residuals are centered on 2006 trend values and normalized to have unitary mean.

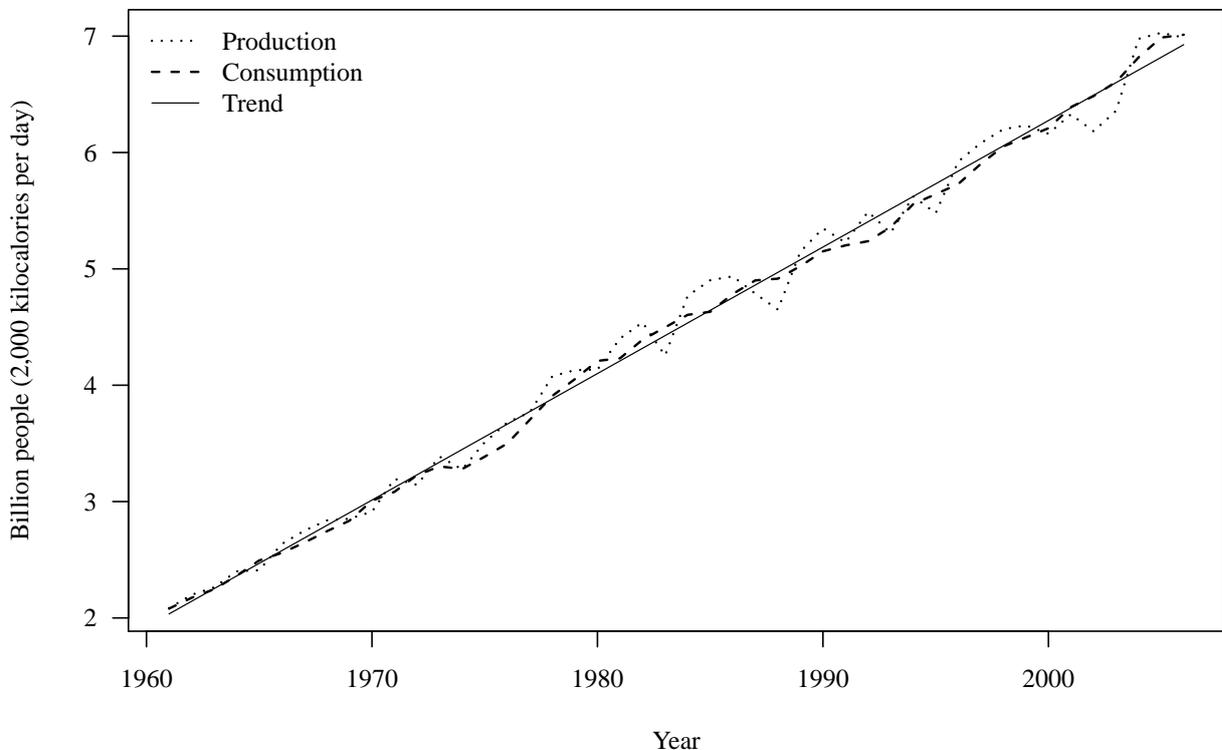


Figure 4.1. World caloric production and consumption, and their trend for 1961–2006. The y-axis is the number of people who hypothetically could be fed on a 2,000 kilocalories per day diet based on consuming only the four commodities.

Regarding prices, a crucial issue is deciding what is the most relevant annual price series to use to estimate of the storage model. The series of prices used in Deaton and Laroque (1992) are formed by averaging prices over the calendar year, which might induce spurious correlations due to mixing together different marketing seasons. Guerra et al. (2015) compare the model fit for a storage model when estimated on different price series for maize and find that the price for the first month following the delivery is what works best. Roberts and Schlenker (2013) adopt the strategy of a single month per year, which is the approach used here. Nominal

² See Wright (2014) and de Gorter et al. (2015) for more.

spot prices are taken from the World Bank pink sheets,³ which provide monthly prices by averaging the daily prices observed during each month. The annual price is the price observed during the month following delivery in the main market (December for maize and wheat, and November for soybeans and rice). The resulting annual price series are deflated by the US CPI and aggregated to a single caloric price index series similar to the calculation for quantities. The deflated price index exhibits a downward trend over the sample period (figure 4.2). To remove the trend, we follow Roberts and Schlenker (2013) and regress log prices over a restricted cubic spline with three knots which offers enough flexibility to account for small movements in the trend.⁴

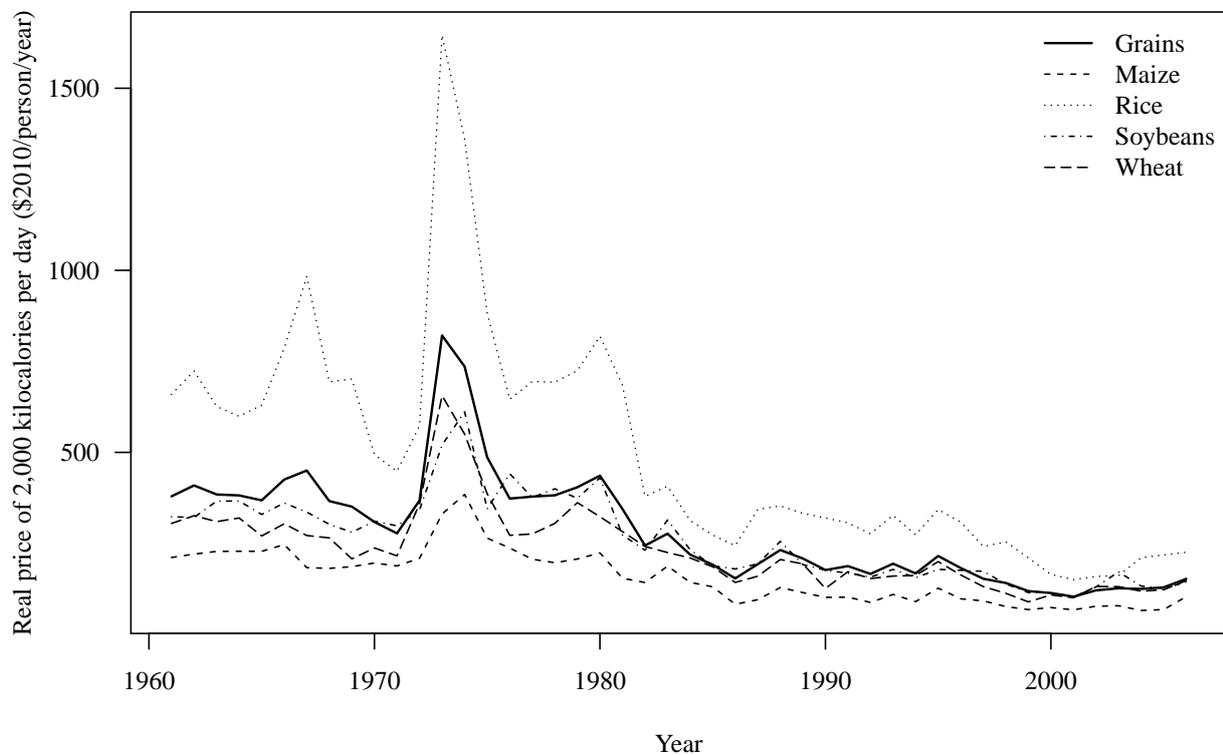


Figure 4.2. Real caloric prices over time. The y-axis is the annual cost of 2,000 kilocalories per day. The price series are taken from the World Bank pink sheets.

4.2.2 DESCRIPTIVE STATISTICS

Next, we present some descriptive statistics for the detrended data and discuss their implications for the estimation of the storage model.

The high levels of the correlation coefficients (all in excess of .85) between the calculated index of grains calories and the real price of each individual crop (table 4.1) are indicative of the large substitution

³ We select the “Maize (US), no. 2, yellow”, “Rice (Thailand), 5% broken, f.o.b. Bangkok”, “Soybeans (US), c.i.f. Rotterdam”, and “Wheat (US), no. 1, hard red winter” series.

⁴ The knots are located in 1963, 1984, and 2005 as suggested in Roberts and Schlenker (2013, Online appendix).

possibilities between these crops. With the exceptions of soybeans and maize, the crops are correlated more to the aggregate than to any other crop. This supports use of an aggregated caloric indicator as a suitable measure of the state of the world food market. Estimation based on each crop individually would create the risk of mixing own-price and cross-price elasticities.

Table 4.1. Correlation coefficients of detrended real prices data, 1961–2006

Commodity	Grains	Maize	Rice	Soybeans	Wheat
Grains	1.000	0.897	0.972	0.856	0.950
Maize	0.897	1.000	0.795	0.886	0.873
Rice	0.972	0.795	1.000	0.774	0.875
Soybeans	0.856	0.886	0.774	1.000	0.813
Wheat	0.950	0.873	0.875	0.813	1.000

Notes: Prices are detrended using a restricted cubic splines using three knots. “Grains” refers to the caloric aggregate of maize, rice, soybeans, and wheat.

Table 4.2 reports the descriptive statistics of the data used to estimate the model. The first-order autocorrelation of prices is high at 0.615. Higher values of autocorrelation (mostly above 0.8) were observed on a different sample by Deaton and Laroque (1992), which led them to reject the storage model because of its inability to match these high levels. Competitive storage behavior is able to explain positively autocorrelated prices, but not very high levels. Hence, the importance of detrending the prices because the model is able to explain only cyclical fluctuations not long-run trends (Gouel and Legrand, 2016b). Consumption also presents a high serial correlation at 0.73, which is consistent with the fact that, except in the case of structural and measurement shocks, consumption should follow price behavior. The first- and second-order autocorrelations are higher for consumption than for price, likely explained by autocorrelated demand shocks. We do not consider this possibility here, but it would make sense if demand shocks are not idiosyncratic but related to the business cycle. Production presents a small first-order autocorrelation of 0.163. With respect to the storage model, this small autocorrelation indicates that uncorrelated supply shocks are quantitatively more important than endogenous supply reactions. The absence of autocorrelation in production supports the relevance of storage to generate price persistence.

Table 4.2. Autocorrelation and coefficient of variation of detrended caloric data, 1961–2006

Variable	One-year a-c	Two-year a-c	Coefficient of variation
Production	0.163	−0.098	0.021
Consumption	0.730	0.418	0.011
Price	0.615	0.181	0.298

The coefficients of variation of production and consumption are quite low at 2.1% and 1.1% respectively. The fact that production is more volatile than consumption shows the importance of inter-annual storage. Without storage, changes in production levels would have to be matched each year by corresponding changes

in consumption levels. Price is much more volatile than consumption. To reproduce this would require a very inelastic demand curve.

Table 4.3 displays the correlation coefficients of production, consumption, and price. The correlations have the expected signs, with a negative correlation between consumption and price and a positive one between production and consumption. However, production and consumption are not perfectly correlated, which again points to the role of storage. Because of storage, in the model, consumption is not determined by production but by the sum of production and stocks. Therefore, production should affect consumption, but this effect is mitigated by the presence of stocks. The low correlation between consumption and price indicates that a lot of the movements observed for consumption stems not from movements along the demand curve, but from movements in the demand curve itself or from measurement errors. If it was due only to movements along the demand curve the correlation would be close to -1 . This low correlation between consumption and price exemplifies the standard econometric challenge in the estimation of demand elasticities: price variations are caused by supply and demand shocks and movements along the supply and demand curves, with the result that identification of a demand elasticity requires the price variations from exogenous supply shocks to be isolated. Some works have proposed clever empirical strategies aimed at isolating clear exogenous supply shocks (Adjemian and Smith, 2012, Roberts and Schlenker, 2013). In this study, the identification comes from the assumed structural form of the model, which allows to recover the various shocks from the observations.

Table 4.3. Correlation coefficients of detrended caloric data, 1961–2006

Variable	Production	Consumption	Price
Production	1.000	0.390	-0.122
Consumption	0.390	1.000	-0.121
Price	-0.122	-0.121	1.000

4.3 ESTIMATION

In this section, we propose an econometric procedure to estimate the storage model using information on quantities. Thus far, structural estimations of the storage model have been undertaken assuming that: (i) supply is inelastic, (ii) only one shock, a supply shock, is generating prices dynamics, (iii) price is the only observable, and (iv) prices are observed without measurement errors. Under these assumptions, Cafiero et al. (2015) develop a Maximum Likelihood estimator. Starting from the same likelihood function, we gradually relax these four assumptions to provide a more comprehensive picture of how production, consumption and spot prices are connected by storage decisions. In this preliminary version of the work, we maintain assumption (iv) that prices are observed without measurement errors. This assumption allows the likelihood to take an analytic form.

Once evaluated, the likelihood function can either be maximized over a vector of parameters θ following the frequentist approach, or according to Bayes' theorem, can be combined with a prior distribution of the

model parameters to form the posterior distribution of the parameters. The posterior distribution then can be used for inference and model comparison. As is often the case when estimating dynamic models, the storage model likelihood is flat in some areas, and exhibits many local maxima. In this context, it is difficult to find the global maximum of the likelihood. This usually requires global search algorithms which are costly to use when the model to be estimated, such as the storage model, requires a non-trivial length of time for its solution. To avoid these difficulties, we take a Bayesian approach by employing Markov chain Monte Carlo methods for sampling posterior parameters, an approach that has become the norm in macroeconomics for the estimation of DSGE models (Fernández-Villaverde et al., forthcoming).

We maximize the log-posterior function to estimate the mode of the posterior distribution. We use the mode of the posterior as the starting value for a random walk Metropolis-Hastings (RWMH) algorithm, which simulates a Markov chain whose stationary distribution corresponds to the posterior distribution of interest. For the random walk step, the initial variance-covariance matrix of the draws is taken to be the inverse of the outer product of the scores resulting from optimization of the log-posterior function. This matrix is then adjusted during the first 10^5 draws of the chain according to the strategy proposed by Vihola (2012).⁵ A sample of 10^7 draws from the posterior distribution is created from the RWMH algorithm, from which we discard the first half of the chain as a burn-in and retain 1 every 1,000 draws to thin the chain before testing for convergence. Convergence of the Markov chain is assessed graphically and using the convergence diagnostics of Geweke (1992). Both approaches confirm that the simulated chain is long enough to ensure convergence to the stationary distribution of the posterior and to deliver reliable moments estimates of the parameters.

4.3.1 THE LIKELIHOOD FUNCTION

GENERIC EXPRESSION

A variety of competing model specifications are estimated depending on assumptions about whether supply responds to prices variations, what variables are observable, and the number of structural shocks. For each assumption, different sets of parameters θ can be recovered from the data. Estimating several model specifications allows us to make the link with previous estimations of the storage model, to ease comparability of our results by progressively relaxing assumptions (*i*) to (*iii*), and to identify the contribution of each observable to the parameter estimations, given that supply and demand data do not deliver the same kind of information. In all the specifications, there are exactly as many shocks as there are observables to avoid stochastic singularity while maintaining a closed-form solution for the likelihood function.

Given the Markov structure of our model, a set of model parameters θ and a sample of observed variables of length T stacked in $Y_{1:T}^{\text{obs}} \equiv \{Y_1^{\text{obs}}, \dots, Y_T^{\text{obs}}\}$, the likelihood function can be expressed as

$$L(Y_{1:T}^{\text{obs}}|\theta) = \prod_{t=1}^T p(Y_t^{\text{obs}}|Y_{t-1}^{\text{obs}}; \theta). \quad (4.22)$$

⁵ This adjustment phase aims at reaching an acceptance rate closes to the optimal value of 23.4% (Robert and Casella, 2004). In all of our estimations the final acceptance rates lie in the interval 18.3–23.3%.

BAYESIAN ESTIMATION OF THE STORAGE MODEL USING INFORMATION ON QUANTITIES⁹

Assumptions about structural measurement error shocks are made such that there are as many shocks as there are observables and such that the method of variable transformation can be applied. In this case, the conditional density of Y_t^{obs} can be written as

$$p(Y_t^{\text{obs}}|Y_{t-1}^{\text{obs}}; \theta) = p(V_t) |J_t|, \quad (4.23)$$

where V_t is a vector of the error terms which include structural and measurement error shocks, and $|J_t|$ is the determinant of the Jacobian of the mapping of $Y_t^{\text{obs}} \mapsto V_t$.

Under the assumption of centered normally distributed shocks, $p(V_t)$ is the density of a multivariate normal and the likelihood function of the state-space model takes the following general form:

$$L(Y_{1:T}^{\text{obs}}|\theta) = (2\pi)^{-\frac{nT}{2}} \prod_{t=1}^T |\Sigma|^{-1/2} \exp\left(-\frac{V_t' \Sigma^{-1} V_t}{2}\right) |J_t|, \quad (4.24)$$

where n is the number of observed variables stacked in Y^{obs} and Σ is the variance-covariance matrix of V .

A specific model is defined by its vector of error terms V_t which in turn, determines Σ and J_t . Given these three elements we can define the likelihood function.

MODEL-SPECIFIC LIKELIHOOD FUNCTION

In the remainder of the chapter, a model is denoted by letters and numbers respectively indicating the observables and the number of assumed structural shocks. For instance for the model PQ1, the observables are price and production, and there is one structural shock, a supply shock. For PDQ2, the observables are price, consumption, and production, and there are two structural shocks, supply and demand shocks.

For brevity, we demonstrate how to evaluate the likelihood function only for the two most comprehensive specifications with elastic supply and for which the vector of observed variables $Y^{\text{obs}} = (P^{\text{obs}}, D^{\text{obs}}, Q^{\text{obs}})'$ includes price, consumption, and production. These specifications nest the others.⁶

MODEL PDQ1 Let consider that prices fluctuations are driven solely by unexpected supply disturbances η^Q (i.e., $\eta^D = 0$). In contrast to consumption and production, prices are assumed to be observed without noise. So the vector of errors is $V_t = (\eta_t^Q, \varepsilon_t^D, \varepsilon_t^Q)'$, where ε^D and ε^Q are measurement errors on consumption and production. Following Cafiero et al. (2015), a production shock can be recovered from observation of two consecutive prices using equation (4.10). So the various elements of V_t are defined by

$$\eta_t^Q = \mathcal{P}^{-1}(P_t^{\text{obs}}) - \frac{\mathcal{S}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}}))}{1+g} - \mathcal{Q}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}})), \quad (4.25)$$

$$\varepsilon_t^D = D_t^{\text{obs}} - D(P_t^{\text{obs}}), \quad (4.26)$$

$$\varepsilon_t^Q = Q_t^{\text{obs}} - \mathcal{Q}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}})) - \eta_t^Q = Q_t^{\text{obs}} - \mathcal{P}^{-1}(P_t^{\text{obs}}) + \frac{\mathcal{S}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}}))}{1+g}. \quad (4.27)$$

⁶ The other set-up are available upon request.

The Jacobian J_t of V_t with respect to Y_t^{obs} is

$$J_t = \begin{pmatrix} \mathcal{P}^{-1'}(P_t^{\text{obs}}) & 0 & 0 \\ -D'(P_t^{\text{obs}}) & 1 & 0 \\ -\mathcal{P}^{-1'}(P_t^{\text{obs}}) & 0 & 1 \end{pmatrix}. \quad (4.28)$$

The determinant of J_t is equal to $|\mathcal{P}^{-1'}(P_t^{\text{obs}})|$.

We allow the measurement errors ε^D and ε^Q on the consumption and production observations to be correlated with the coefficient ρ^{DQ} , and we denote their standard deviation by σ_{ε^D} and σ_{ε^Q} . This leads to the following variance-covariance matrix of the vector of errors V

$$\Sigma = \begin{pmatrix} \sigma_{\eta^Q}^2 & 0 & 0 \\ 0 & \sigma_{\varepsilon^D}^2 & \rho^{DQ} \sigma_{\varepsilon^D} \sigma_{\varepsilon^Q} \\ 0 & \rho^{DQ} \sigma_{\varepsilon^D} \sigma_{\varepsilon^Q} & \sigma_{\varepsilon^Q}^2 \end{pmatrix}. \quad (4.29)$$

Assuming that only price is observable and that supply is inelastic (so $\mathcal{Q}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}})) = \bar{D}$) leads to the same likelihood function as Cafiero et al. (2015).

MODEL PDQ2 Alternatively, let us consider now that price changes might result also from unexpected shifts in consumption. This augments the number of structural shocks to two. Since having a closed-form likelihood function requires as many shocks as observables, we have to remove one measurement error shock. So we assume that consumption is observed perfectly (i.e., $\varepsilon_t^D = 0$). This leads to the vector of errors $V_t = (\eta_t^Q, \eta_t^D, \varepsilon_t^Q)'$ with elements:

$$\eta_t^Q = \mathcal{P}^{-1}(P_t^{\text{obs}}) - \frac{\mathcal{S}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}}))}{1+g} - \mathcal{Q}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}})) + \eta_t^D, \quad (4.30)$$

$$= \mathcal{P}^{-1}(P_t^{\text{obs}}) - \frac{\mathcal{S}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}}))}{1+g} - \mathcal{Q}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}})) + D_t^{\text{obs}} - D(P_t^{\text{obs}}), \quad (4.31)$$

$$\eta_t^D = D_t^{\text{obs}} - D(P_t^{\text{obs}}), \quad (4.32)$$

$$\varepsilon_t^Q = Q_t^{\text{obs}} - \mathcal{P}^{-1}(P_t^{\text{obs}}) + \frac{\mathcal{S}(\mathcal{P}^{-1}(P_{t-1}^{\text{obs}}))}{1+g} - D_t^{\text{obs}} + D(P_t^{\text{obs}}). \quad (4.33)$$

and the Jacobian is:

$$J_t = \begin{pmatrix} \mathcal{P}^{-1'}(P_t^{\text{obs}}) - D'(P_t^{\text{obs}}) & 1 & 0 \\ -D'(P_t^{\text{obs}}) & 1 & 0 \\ D'(P_t^{\text{obs}}) - \mathcal{P}^{-1'}(P_t^{\text{obs}}) & -1 & 1 \end{pmatrix}. \quad (4.34)$$

As before, the determinant of J_t is equal to $|\mathcal{P}^{-1'}(P_t^{\text{obs}})|$.

Since the structural supply and demand shocks are assumed to be uncorrelated, the variance-covariance

matrix of the vector of errors V is given by

$$\Sigma = \begin{pmatrix} \sigma_{\eta^c}^2 & 0 & 0 \\ 0 & \sigma_{\eta^p}^2 & 0 \\ 0 & 0 & \sigma_{\varepsilon^c}^2 \end{pmatrix}. \quad (4.35)$$

4.3.2 PRIOR DISTRIBUTION OF THE PARAMETERS

The model parameters are gathered into the vector $\theta \equiv (r, g, \rho^{DQ}, \sigma_{\varepsilon^p}, \sigma_{\varepsilon^c}, \sigma_{\eta^p}, \sigma_{\eta^c}, k, \bar{D}, \bar{P}, \alpha^D, \alpha^S)$. Before the estimation, two parameters are fixed: the real interest rate and the rate of growth of consumption and production. The real interest rate is always fixed in estimations of the storage model, since it would be very difficult to estimate it based only on observation of commodity prices. In the literature, it is fixed at either 2% or 5% (Deaton and Laroque, 1992, 1996, Cafiero et al., 2011b, 2015). Given that our sample covers the period 1961 to 2006, it seems appropriate to fix the annual real interest rate at 2%. According to the assessment in Barro and Sala-i Martin (1990), for nine OECD countries for which historical data are available the mean short-term interest rate was 1.87% over the period 1959–1989. Since the sharp rise to rates of about 5% in the 1980s, the world real interest rate started declining to reach an average yearly level of about 2% in the mid 2000s (International Monetary Fund, 2014, Chapter 3). The annual rate of growth of consumption and production is fixed at 2.6%, a value estimated by regressing the log of consumption and production on a time trend.

Apart from these calibrated parameters which will not be updated during the estimation procedure, the prior distributions for the other parameters are shown in table 4.4. For the standard errors of the shocks, we follow the usual practice in the estimation of DSGE models of using an inverse-gamma distribution which insures positive support, and without information on their size we use loose priors with mean and standard deviations equal to 0.05 for all. The correlation between measurement errors on consumption and production is assumed to be uniformly distributed from -1 to 1 . Data are detrended and centered on 1. Since the model is nonlinear, the steady state is different from the mean, but the location of the mean around 1 is nonetheless an indication that the steady state will be in this region. So the steady-state values of consumption and production are assumed to follow a gamma distribution with mean 1 and standard deviation of 0.32, high enough to cover a reasonable range of parameter values. The storage cost is assumed to follow a Gamma distribution with mean 0.25 and standard deviation 0.18 so that the prior extends from very low to prohibitive costs, covering World Bank and FAO (2012, Figure 2-4) values around 10%–15% of the price for wheat. For the elasticities, the abundant literature presents very diverse results with demand elasticities ranging from -0.03 (Roberts and Schlenker, 2013) to -1 (Adjemian and Smith, 2012), and similarly for supply elasticities. In light of this, elasticities are assumed to follow rather loose Gamma distributions with mean 0.5 and standard deviation 0.35, so that their domain covers all previous estimates.

Table 4.4. Marginal prior distribution for each model parameter

Parameter	Domain	Density	Hyperparameter (1)	Hyperparameter (2)
ρ^{DQ}	$(-1, 1)$	Uniform	-1	1
σ_{ε^D}	\mathbb{R}^+	Inverse Gamma	0.05	0.05
σ_{ε^Q}	\mathbb{R}^+	Inverse Gamma	0.05	0.05
σ_{η^D}	\mathbb{R}^+	Inverse Gamma	0.05	0.05
σ_{η^Q}	\mathbb{R}^+	Inverse Gamma	0.05	0.05
\bar{D}	\mathbb{R}^+	Gamma	10	0.1
\bar{P}	\mathbb{R}^+	Gamma	10	0.1
k	\mathbb{R}^+	Gamma	2	0.125
α^D	\mathbb{R}^-	Gamma (with transformation to have negative support)	2	0.25
α^S	\mathbb{R}^+	Gamma	2	0.25

Notes: Hyperparameter (1) and Hyperparameter (2) list the upper and lower bounds of the support for the Uniform distribution; the mean and the standard deviation for the Inverse Gamma distribution; and a and b for the Gamma distribution, where $p_G(x|a, b) \propto x^{a-1} \exp(-x/b)$.

4.3.3 POSTERIOR ESTIMATES OF THE PARAMETERS

To maintain a continuum and ease comparability with past empirical storage model studies, we estimate several versions of the storage model from Deaton and Laroque's simple model with inelastic supply where only prices are observed, to more complete specifications with supply reactions and inferences involving consumption and production data in addition to prices.

INELASTIC SUPPLY

Here we fix the supply elasticity α^S to zero before estimation. The number of observed variables varies between the model specifications enabling analysis of what can be learned from the production and consumption observations, and eventually, which aspects of the global grains market dynamics can be captured by the model. For each model, the estimated mean and standard deviation of the parameter posterior distributions when supply is assumed inelastic are reported in table 4.5.⁷

The first column, model P1, corresponds to the simplest specification and is the link with existing empirical storage model studies in which inference is made on prices data. In this case, the model is the same as in Deaton and Laroque (1992, 1996) and the likelihood function is the same as in Cafiero et al. (2015). In addition to assuming that supply is inelastic, inference resting on prices alone requires more parameters to be fixed before the estimation to allow the other parameters to be identified. Deaton and Laroque (1996, Proposition 1) show that when only prices are observed it is not possible to identify the demand function separately from the supply shocks. So we fix the steady-state value of quantities \bar{D} at unity, and the standard deviation of the supply innovation σ_{η^Q} at 0.0214, the standard deviation of the detrended production which amounts to assuming that all observed variations in production are explained by structural shocks. The

⁷ Results based on the median, and the 5th and 95th percentiles of the posterior distribution are similar.

Table 4.5. Bayesian estimates with inelastic supply

Parameter	P1	PD1	PQ1	PDQ1	PD2	PDQ2
ρ^{DQ}	0	0	0	0.6358 (0.1059)	0	0
$\sigma_{\varepsilon Q}$	0	0	0.0210 (0.0023)	0.0231 (0.0027)	0	0.0186 (0.0020)
$\sigma_{\varepsilon D}$	0	0.0143 (0.0016)	0	0.0147 (0.0016)	0	0
$\sigma_{\eta Q}$	0.0214	0.0264 (0.0095)	0.0179 (0.0028)	0.0189 (0.0029)	0.0333 (0.0100)	0.0219 (0.0027)
$\sigma_{\eta D}$	0	0	0	0	0.0151 (0.0018)	0.0153 (0.0018)
\bar{D}	1	0.9959 (0.0030)	1.0017 (0.0036)	0.9956 (0.0031)	0.9942 (0.0034)	0.9943 (0.0027)
\bar{P}	1.1483 (0.0980)	1.1274 (0.1598)	1.0905 (0.1073)	1.1196 (0.1129)	1.2066 (0.1648)	1.2087 (0.1136)
k	0.0595 (0.0208)	0.0373 (0.0148)	0.0518 (0.0198)	0.0508 (0.0183)	0.0453 (0.0196)	0.0698 (0.0228)
α^D	-0.0297 (0.0085)	-0.0160 (0.0043)	-0.0202 (0.0062)	-0.0197 (0.0052)	-0.0263 (0.0093)	-0.0297 (0.0072)
α^S	0	0	0	0	0	0
P^*	1.3953	2.0281	1.4264	1.5228	1.8866	1.4662
# Stockouts	5	2	3	2	2	3

Notes: The table shows the mean and in parenthesis the standard deviation of the posterior distribution. P^* and the number of stockouts are calculated for the parameters at the mean of the posterior distribution.

storage cost k is found to be equal to 5.2% of the steady-state price, a value much higher than the estimations in Cafiero et al. (2011b, 2015) but close to those found by Gouel and Legrand (2016b). The posterior mean of the demand elasticity, α^D , is -0.0296 . This is a very low demand elasticity but is in line with Roberts and Schlenker’s (2013) estimates which are in the range of -0.014 to -0.066 for the same index of grains calories. Furthermore, it is consistent also with the fact that once aggregated, these staple products have very few, if any, substitution possibilities. Finally, the market is estimated to enter the stockout regime five times over the sample length of 46 years. This is in line with the intuition that stockouts are rare events corresponding to periods when prices spike. In our sample, the stockouts correspond (from the highest to the lowest detrended prices) to the peaks in grains prices in 1973 and 1974, to the price increase at the end of the sample in 2006, to 1980 and 1975.

In the second column, the model PD1 includes consumption as an observable. This allows the parameters of the supply process to be identified separately from those of the demand function, meaning that the parameters \bar{D} and $\sigma_{\eta Q}$ are now allowed to be estimated. \bar{D} is precisely estimated at close to 1, which is consistent with the fact that in this storage model the steady-state consumption should be close to the asymptotic mean consumption. The standard deviation of the structural supply shock is slightly above the volatility of production observed in the data (table 4.2). Compared to the specification P1, the demand

function has a much steeper slope at -0.016 . Combined with a lower storage cost estimated at 3.31% of the steady-state price, the inferred cutoff price P^* over which inventories are sold out is 45% higher, which decreases the estimated number of stockouts now limited to 1973 and 1974. The standard deviation of the measurement error shock on consumption is of the same size as the volatility of consumption observed in the data, so the storage model explains little of the variation in consumption. This is expected given the low correlation observed between consumption and price.

In the specification PQ1, we use production as the observable rather than consumption, and assume only one structural shock. Compared to the specification PD1, it leads to a lower standard deviation of the posterior for σ_{η^Q} , consistent with the fact that production is more directly informative than consumption about the production shock. Compare to PD1, demand is slightly more elastic to price, and storage is more costly (4.7% of the estimated steady-state price) but the differences are mostly all within the ranges of the standard deviations of the estimates, except for σ_{η^Q} . Nonetheless, these differences lead to a lower cutoff price P^* implying the occurrence of a third stockout in 2006.

The specification PDQ1 includes all available observables. It leads to estimates that are close to the specifications PD1 and PQ1. This specification confirms that half of observed production fluctuations can be explained by structural shocks with the other half accounted for by measurement errors. As for PD1, the measurement error on consumption is substantial and would account for almost all observed consumption changes. There is a significant correlation coefficient of the measurement error on consumption and production: $\rho^{DQ} = 0.64$. This is consistent with the way these data are collected, with reasonably thorough surveys of production, and estimates for consumption that partly depend on production estimates.

We turn next to specifications PD2 and PDQ2 which feature two structural shocks: one on consumption and one on production. In these cases, a closed-form likelihood function with measurement errors on consumption is not possible. We assume that consumption is perfectly observed, and is the sum of a deterministic demand function and a structural shock. If we compare the specifications PD2 and PD1, what is captured in PD1 in the measurement error on consumption is accounted for now by the structural shock. Surprisingly, this leads also to a much larger structural production shock with a posterior mean for σ_{η^Q} of 0.0333, an estimate which far exceeds the observed volatility in production. The estimation of σ_{η^Q} is lower under the specification PDQ2 which uses production as an observable. Overall, the specifications allowing for two structural shocks lead to estimated net supply shocks ($\eta^Q - \eta^D$) larger in size than their counterparts with one shock (PD1 and PDQ1) which implies a more elastic demand function, closer to Roberts and Schlenker's estimates.

ELASTIC SUPPLY

So far the literature on estimation of storage models has focused on models with inelastic supply because prices were the only observables; this does not permit estimation of demand and supply elasticities. By using consumption and production as additional observables we can estimate models with elastic supply.⁸

⁸ The sole observation of consumption is not informative enough to deliver sound estimates when the model has elastic supply. Hence, the PD1 and PD2 specifications are no longer considered in the subsequent estimations.

BAYESIAN ESTIMATION OF THE STORAGE MODEL USING INFORMATION ON QUANTITIES⁸⁵

Theoretically, speculative storage and elastic production show interesting interactions.⁹ In the absence of storage, the model collapses to Muth's (1961) model where planned production is constant and equal to its steady-state value because the expected price is constant. As soon as speculative storage operates, the expected price and planned production varies. A high stock level weights on the expected prices, and by extension, on the expected profits from production, along with the level of effort invested in new production. Conversely, low stock levels lead to high expected prices and high levels of planned production, with an upper limit attained when stocks are null. Because production adjusts to the expected price and helps alleviate future scarcities, stock levels are less responsive to current availability. For various calibrations, Wright and Williams (1982) show that a model with elastic supply leads to lower price volatility than the same model with inelastic supply. This means that with elastic supply, lower stock levels will be required to fit the same price volatility in the data. This translates to the estimation (see table 4.6) of higher storage costs and lower cutoff prices than for the corresponding inelastic specifications. For the PDQ1 and PDQ2 specifications this leads to five stockouts, in 1973–5, 1980, and 2006, while in the PQ1 specification there is a sixth stockout in 1979.

Table 4.6. Bayesian estimates with elastic supply

Parameter	PQ1	PDQ1	PDQ2
ρ^{DQ}	0	0.6192 (0.1115)	0
$\sigma_{\varepsilon Q}$	0.0209 (0.0023)	0.0231 (0.0028)	0.0189 (0.0020)
$\sigma_{\varepsilon D}$	0	0.0145 (0.0016)	0
$\sigma_{\eta Q}$	0.0189 (0.0029)	0.0194 (0.0029)	0.0224 (0.0029)
$\sigma_{\eta D}$	0	0	0.0150 (0.0017)
\bar{D}	0.9978 (0.0038)	0.9921 (0.0032)	0.9903 (0.0029)
\bar{P}	1.3616 (0.1356)	1.4016 (0.1381)	1.4301 (0.1404)
k	0.2045 (0.0887)	0.1918 (0.0824)	0.1943 (0.0823)
α^D	-0.0218 (0.0065)	-0.0198 (0.0055)	-0.0300 (0.0077)
α^S	0.0560 (0.0290)	0.0507 (0.0270)	0.0492 (0.0285)
P^*	1.2811	1.3804	1.3713
# Stockouts	6	5	5

Notes: The table shows the mean and in parenthesis the standard deviation of the posterior distribution. P^* and the number of stockouts are calculated for the parameters at the mean of the posterior distribution.

⁹ See Wright and Williams (1982) for a thorough description of the effects of modeling supply responsiveness in the dynamics implied by the model.

For the same specifications, the estimations with elastic supply are similar to the estimations with inelastic supply for almost all parameters except the steady-state price and the storage cost; both of which increase significantly. Expressed as a percentage of the steady-state price, storage costs are of the order of 14%, a value consistent with the World Bank and FAO (2012). Supply elasticities are estimated to be around 0.05, so supply is twice as elastic as demand. These supply elasticities are in the lower range of the values in the literature. Compared to Roberts and Schlenker (2013), they are twice as low. Roberts and Schlenker (2013) estimate the supply elasticity as being between 0.085 and 0.116.

While most parameters are precisely estimated, the storage cost and supply elasticity are estimated with limited precision. The standard deviations of the posterior distribution of storage cost and supply elasticities are close to 43% and 53% of their respective means. Storage cost is the least precisely estimated parameter in the inelastic case, which can be explained by the fact that beyond very small values the likelihood function is quite flat with respect to storage cost. However, the standard deviation of k is much higher in the elastic case. This likely stems from the fact that storage and elastic production are substitutes for explaining price volatility. The observation of production should help choose between the two processes but given the size of the measurement error on production, its informativeness is probably limited which explains the lack of precision of the estimates.

Figure 4.3 summarizes the estimation results visually by plotting the prior distribution, and the posterior distributions of the inelastic and elastic PDQ2 models. It confirms that the posterior distributions are the same in the inelastic and elastic cases, except for \bar{P} and k . All parameters are estimated to be significantly different from zero. Except for the storage cost in the elastic case, the posterior distributions are different from the prior distributions. The similarity of the prior and posterior for storage cost if the model features elastic supply confirms a potential problem of identification.

4.4 CONCLUSION

This chapter proposed a new estimation strategy for the rational expectations storage model. In addition to prices, it adds to the observable variables consumption and production. This allows the identification of parameters not recoverable if the inference rests on prices alone, and enables estimation of a richer storage model with elastic supply and two structural shocks. The estimation method takes its inspiration from recent developments in the estimation of DSGE models. It uses Bayesian econometric methods which are more suited to these types of dynamic models than frequentist methods, which are more likely to experience difficulty to find a global maximum. To ease comparability with the results in the literature, we started the estimations with a specification close to Cafiero et al. (2015), with inelastic supply and prices as the only observables. We introduced more observables gradually, and relaxed the assumption of inelastic supply. The variety of model specifications estimated allowed us to identify the contribution of each set of observables to the results. In order to have a benchmark against which to compare our results, the model was estimated on the same set of data as in Roberts and Schlenker (2013): the market for the caloric aggregate of maize, rice, soybeans, and wheat from 1961 to 2006.

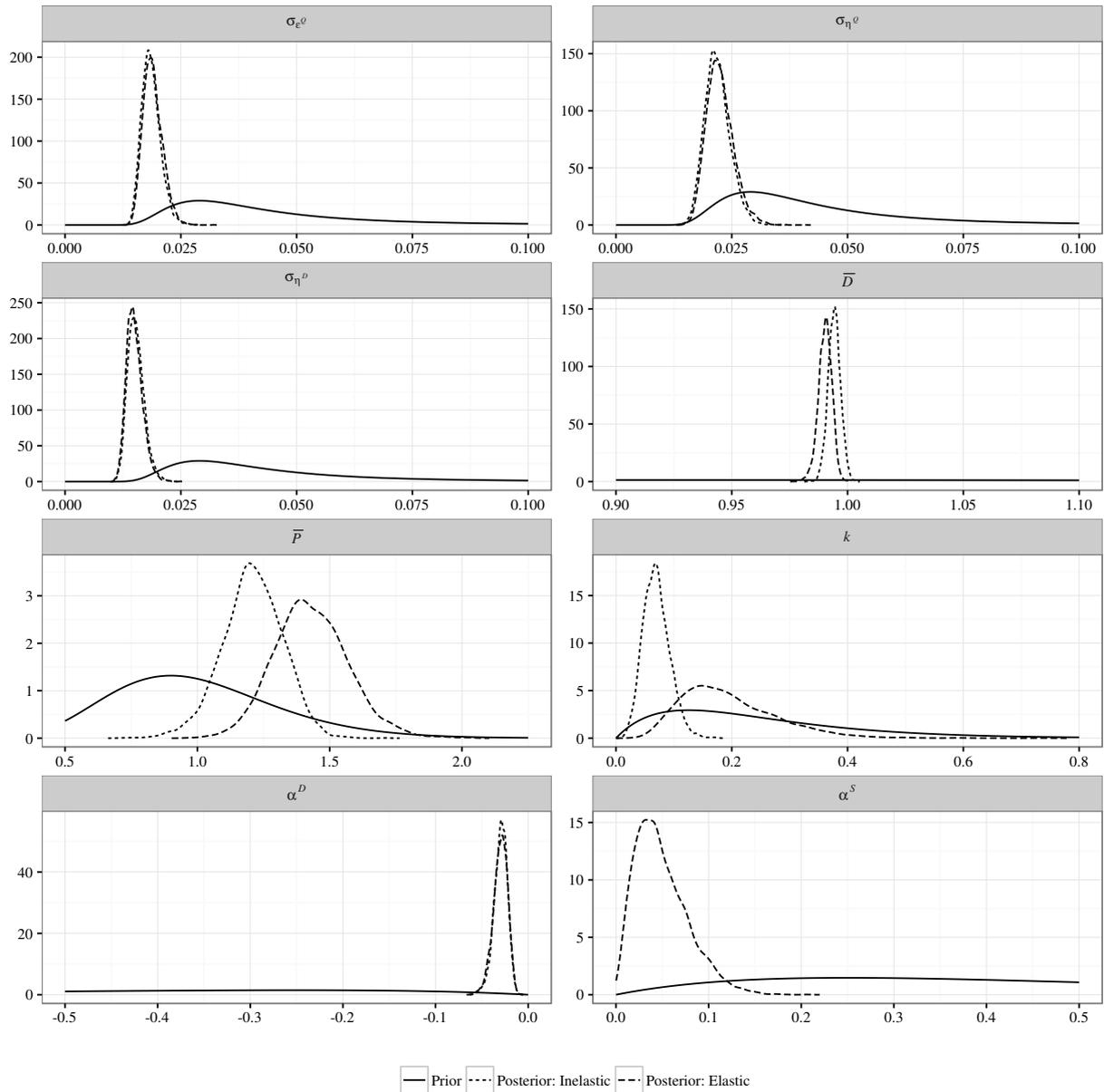


Figure 4.3. Estimated parameter distribution for the specification PDQ2

In our estimations, elasticities are in the lower range in the literature: -0.02 to -0.03 for the demand elasticity and 0.05 for the supply elasticity. These estimates are slightly lower than but consistent with Roberts and Schlenker’s estimates, and other estimates based on the storage model (e.g., Gouel and Legrand, 2016b, Guerra et al., 2015). These low values were expected given the low volatility of observed consumption and production. Storage costs are estimated to be between 4% and 14% of the steady-state price. Storage was shown to be more costly when supply is elastic, because elastic supply and speculative storage have similar effects on price dynamics. The importance of storage decreases when supply is allowed to be elastic and the

number of stockouts increases. These preliminary results tend to confirm that our Bayesian approach is a reliable econometric method for structural estimations of the storage model.

In this preliminary version of the work we made assumptions to permit the likelihood function of the storage model to take an analytic form. This involves severe restrictions: unlike quantities prices were assumed to be observed without noise, and it was not always possible to estimate measurement errors and structural shocks jointly. These restrictions will be lifted in the final version of the study which will present estimations with more general specifications.

The new estimation methods for the storage model proposed in this chapter constitute an important innovation; however one of their main benefits may be the new perspectives they open for this model. Deaton and Laroque (1992, 1996) rejected the storage model for its inability to fit the serial correlation in prices. This problem has been solved in recent works but with an estimation method which allows us to use all observables to fit the model, it is likely that the storage model's ability to fit the behavior of the observables will decrease with the number of observables. The dimensions where the model fails will open the way to new theoretical developments to improve the model fit. We have seen similar developments in the econometrics of DSGE models where extra elements have been added to the basic RBC model to improve its fit (Fernández-Villaverde, 2010). In the case of our estimations, the standard deviations of the measurement errors on consumption and production are large and could explain most the observed variations. So the current specification of the storage model is not able to account well for the dynamics of quantities, and should be extended with this shortcoming in mind.

CHAPTER 5

THE CROWDING-OUT EFFECT OF STORAGE ON INVESTMENT: EVIDENCE FROM THE CRUDE OIL SECTOR

PREAMBLE:
ROLLER COASTER IN THE OIL INDUSTRY

5.1 PREAMBLE

UNPREDICTABLE BY NATURE

It is fair to say that guessing what would be the oil price no further than a couple of months ahead is a perilous if not impossible exercise. At best, one can come up with a rather loose 95% confidence interval. Hamilton (2009) would not disagree with me on this when he shows that neither the U.S. nominal interest rates nor the U.S. GDP growth rates are significantly helpful when it comes to forecast the quarterly real oil price change over the 1970-2008 period. Trying to predict the level instead of the change in prices is of no use since both the Dickey-Fuller and KPSS tests fail to reject the unit root hypothesis at the 5% level of significance. In the end he concludes that crude oil prices follow a random walk with drift. From a statistical standpoint it just means that for a given standard deviation σ of the price change over the whole sample length, the logarithm of the real oil price $p = \log(P)$ in n quarters into the future is expected to fall within the 95% lower and upper bounds defined as $[p \pm 1.96\sigma\sqrt{n}]$. Given a price at \$115 a barrel as of the first quarter of 2008—e.g., the last data point of the sample he used—that leaves somebody trying to guess the price value in the next quarter with a range as large as \$85 to \$115 per barrel. The author could not have put it better when extending the forecast until 2012:Q1 he ends up saying that the price per barrel can well be as low as \$34 or as high as \$391.

In the first quarter of 2012, the real oil price was in the \$85-90 region. At that time, very few people would have bet that four years later (e.g., in 2016:Q1) the WTI crude oil price would lie below the \$30 a barrel barrier. However, such an erratic behavior in the price of crude oil does not mean variations are completely irrational. Instead, a thorough understanding of price dynamics of commodities such as oil relies on a close look to the market fundamentals of supply, demand and storage which eventually are governing the global price formation. With this in mind, I will turn now to try to explain why, after having posted records upon records during more than a decade, crude prices collapsing to the bottom values ranging from \$25 to

\$30 a barrel reached at the beginning of 2016 is not too big a surprise. Similarly, a crude price well above \$100 a barrel as of 2020 seems quite plausible.

A RESILIENT SUPPLY

As in many industries involving substantial upstream investment costs, a large proportion of them could even be described as sunk costs, the oil production has trouble to adjust so as to track closely the corresponding demand. Indeed, in the short run it is almost impossible to satisfy a sudden increase in the oil consumption apart from any excess production capacity and inventories of limited availability. Inversely, the same is true also when it comes to balance a drop in demand. Such a low supply reaction has to do with (i) the long lead times it takes for oil from a new field discovery to be extracted and actually come online,¹ (ii) the hysteresis effects stemming from both the significant capital and exploration expenditures at stake, (iii) the strategic behavior of suppliers willing to stay competitive in this hostile environment. There is an element of truth to all of them so let us illustrate with concrete examples those explanations which have been studied at length in the theoretical as well as the empirical economic literature as will be seen further in the chapter.

IRREDUCIBLE DELAYS

Supply dynamics in the oil sector are deeply constrained by capital and exploration (capex) costs considerations. First, oil companies have to spend billion of dollars in the search for new oil deposits both located in on-and offshore areas. Once discovered comes the exploitation phase which then again requires a significant amount of time and investment. Indeed, before starting to drill, operators have to deal with administrative procedures to get the operating license along with the credit lines from financial institutions given the size of the sums involved. To get a general picture, since the early seventies no less than \$172 billions of dollars a year on average have been invested in capex activities in the oil sector alone as reported by the Rystad Energy company. All of these risky ventures whose outcomes are very uncertain have to be supported by high spot price levels and expected lasting for a while.

In addition, not only the upstream investments are significant but most of them are almost irreversible since, once drilled, a well cannot be resold or at least at an extremely discounted price. It turns that it is optimal for operators to wait for stable and optimistic future economic conditions before committing into the development of new oil fields.²

In sum, the combination of hardly compressible lengths related to the diverse exploration and drilling processes with the long periods of inaction caused by the real options mechanism primarily explain why fresh oil discoveries cannot be expected to be delivered before at least 3 to 5 years according to the most optimistic figures given by the oil industry experts. As a result, the supply falls short of demand leading prices to settle at a higher level as long as a new stream of production flows and balances the market back. Nevertheless,

¹ It is fair to say that these delays are widely reduced in the shale industry.

² The theoretical foundations have been laid out in the real options literature (Pindyck, 1991, Dixit, 1992) and an empirical illustration is provided in Kellogg (2014).

there exist also factors preventing output from decreasing in response to a lower demand adding to the overall lack of supply flexibility, a point to which we will turn now.

STICKY PRODUCTION

Once the newly installed capital becomes productive and start flowing into the market, although technically feasible a downward adjustment of production in response to an oil consumption slowdown is far from being immediate too. Nonetheless, the reasons for such a stickiness in the decline of oil supply are of a very different nature. First, oil producers, often heavily indebted, are desperate for cash flow needed to meet their financial obligations and avoid bankruptcy. Then, they want to lose neither the benefit of their licenses and leases, nor the products from wells which once completed and fractured cannot be capped and tapped later. They also keep pumping to offset the inevitable depletion from old wells. These decisions are supported further by the fact that operating costs are really tiny compared to those already devoted initially in the capex development phases. Finally and rarely mentioned, chances are high that a large share of the upcoming production has been hedged against a fall in prices sometimes for several years ahead using the variety of financial instruments available from the forwards markets. This is why even if the spot price is falling below the breakeven production costs of some oil reserves, the latter can remain profitable to the operators concerned.³

Hence, between 2014 and the beginning of 2016 and despite high production costs and the sharp drop of the crude market price, oil production from North America kept rising to the great displeasure of Saudi Arabia whose supremacy has been challenged by the shale boom and which has seriously underestimated the resilience of the North American oil industry. This leads us to explore the final force leaning against a quick supply response to price variations, namely the market competition.

STRATEGIC BEHAVIORS

Competition in the oil industry is particularly fierce and have even been exacerbated over the past ten years by the U.S. “shale” revolution. To some extent and at some points in the seventies and early eighties the Organization Petroleum Exporting Countries (OPEC) might have been effective at controlling the supply and thereby the price level worldwide.⁴ Since that time, however, evidences have tended to show that it is no longer the case. The broad part of the explanation are of two types.

The first is internal to the cartel and rests on the existing difference between individual and collective marginal profit. In short, to decide on a price target and exercise its market power the OPEC has to fix the total production level implying a zero marginal profit for the group before agreeing to share the corresponding quota between each of the members. The point is that each member has an incentive “to cheat”—e.g., to produce more than its assigned level—breaking the initial agreement thus becoming irrelevant as illustrated in

³ As the very last futures contracts will expire this year, the “hedging effect” comes to an end bringing producers back to the market reality while the U.S. production begins to reverse.

⁴ It has to be noted that OPEC succeeded to the “seven sisters” which is the name given to the seven big oil companies which colluded on prices and dominated the market during the first half of the twentieth century.

Hamilton (2009), and elsewhere in the literature pointing to the overall lack of empirical evidences supporting a significant “cartel effect” on the crude price (Alhajji and Huettner, 2000, Smith, 2005). Things are not expected to change anytime soon as now we are closer to an explosion of the OPEC than a strengthened cooperation, and despite the last estimation of the International Energy Agency (IEA) indicating that OPEC’s share of the oil market has reached 34 percent, a level not seen since 1975. Indeed, the historical religious tensions between Saudi Arabia and Iran is complemented by an economic rivalry since the latter is determined to take advantage of the recent lifting of international sanctions by ramping up production to make up for the lost market shares.⁵

Apart from the apparent failure of the OPEC members to agree on a production quota, the former role of “swing producer” Saudi Arabia used to play is threatened by the emergence of new big entrants, namely Russia, Canada and the U.S., which are not part of the OPEC nor willing to agree on prices. It results in a radical change in the landscape of world oil supply with heightened competition between smaller producers fighting for market shares, reluctant to cut production whenever demand is softening and with no alternative but to commit into a race to efficiency gains to stay competitive. For instance in the U.S. shale oil industry the depletion rate of wells along with the marginal production costs have been almost halved since 2012 contributing to the outstanding resilience of shale oil producers.

Overall, the combination of lumpy and irreversible spending in the capex development stages with a rigid supply and financially constrained operators struggling to hold on their market share and stay in business, can turn even the slightest slowdown in the growth of oil consumption into a real glut exactly like the one experienced since 2014.

AN OPAQUE DEMAND

If the dynamics of production in the oil sector is fairly well featured it is far from being the case concerning the demand side of the picture. All one can say is that it is almost as inelastic as the supply in the short-run and that the economic literature used to draw a distinction between speculative demand and demand for immediate consumption.

VARIABLE ELASTICITIES

Whether directly or indirectly used, oil is an input for all sectors of the economy so that to assess and predict the oil consumption the IEA has no choice but relying on some key macroeconomic variables governing the final demand and the corresponding elasticities.⁶ Demography and economic activity are among the prominent drivers. Indeed, if the data show anything, it is that the consumption of oil in a given country closely tracks the prevailing growth in income per capita. As the living standard are improving, people can afford motorized transportation, buy more consumer electronics and other household appliances while both public and private infrastructures keep pace with the economic growth. All of these elements fuel the final

⁵ Additional tensions do exist between Saudi Arabia and other member states such as Venezuela which really suffer from the current levels of crude price.

⁶ Here, the elasticity has to be interpreted as the variation of quantity demanded following a change in the variable in question.

growth in petroleum consumption. Unsurprisingly, China alone accounts for the lion share in the dramatic rise of oil consumption observed since the early nineties, passing from a low 3.8% to 12.8% of the oil demand worldwide which soared approximately from 21 to 28 billion of barrels between 1990 and 2013.⁷ And now that China's economy is facing serious headwinds, all eyes are turning to India which is expected to take over with its 1.2 billion of inhabitants and its steady double digit rate of growth in Gross Domestic Product (GDP). It is also worth mentioning that, as the yearly per-capita oil consumption in China or India is five times lower than in Germany and even ten times than in the U.S., chances are high that the last IEA's yearly global growth rate figure of 1.6 billion/day can climb to much higher levels in the coming years. Still, China and possibly even more India will be the main growth engines in global oil demand for at least the next decade.

However, the more challenging in the demand assessment process is to estimate the elasticities. Indeed, they are many forces behind the quantity consumed and it is hard to disentangle their respective contribution and even more so since elasticities are varying both over time and across countries depending on the level of economic developments.⁸ Actually the reported estimates are often a mix between the true elasticity of demand for immediate consumption with the speculative one for storage, the second central pillar of oil demand which must not be overlooked.

SPECULATIVE DEMAND

If the storage mechanism and its effects in the price dynamics are straightforward to understand and well documented, the fact remains that measuring with accuracy the levels of stocks is almost impossible. Indeed, abstracting from the underground inventories commonly categorized as "proven reserves", the global stocks held above ground should include (i) the industrial quantity stockpiled by refiners, (ii) those hold by states and (iii) the too often neglected "floating storage" (e.g., on tankers). Let us examine each in turn the motivations driving the accumulation of inventories.

In the same way as for producers hedging against a fall in prices, refiners and more broadly industrial consumers tend to protect their future supplies and avoid costly disruptions in the transformation process of crude oil. That, in turn, lead them to buy and store output in advance whenever the expected rise in the price is sufficient to cover the physical and interest costs incurred. Although it is the most visible and known component of storage demand, that its key determinants are well established and theoretically grounded, wild variations of large magnitudes still happen. The latest case can be found in China where following a legislation change dating back from July 2015, the private refineries known as "teapots" have been allowed to operate directly and independently in the international market, which translated into Chinese record high numbers of crude imports reaching about 125 million tons in the first four months of 2016, up 12% from the same period a year ago and of which teapots alone account for 15%.⁹ Such additional demand had a considerable impact in preventing the spot crude price from tumbling even further, even participating into its last spring rebound.

⁷ The figures are available from the IEA's databases <https://www.iea.org/statistics/statisticsearch/>.

⁸ A summary of demand and income elasticity values in both the short and long-run is provided in Hamilton (2009).

⁹ The figures are taken from the Wall Street Journal.

Onshore tanks are not the only place where commodities can be piled up especially when, as is occurring now, continental storage capacities are stretched to the limits. The amounts involved with the storage at sea, albeit smaller by an order of magnitude, can play a major role in the price behavior and should not be relegated as a simple back-up solution. Indeed, unlike refiners most of the market practitioners are traders who actually do not take on deliveries, acting instead as pure speculators by closing or rolling over time their positions before the contract expiration. To benefit at full from the positive gap between futures and spot price—known as a contango situation—traders do not hesitate to play with the sailing speed waiting for a tightening in the market conditions leading to a price bounce, a strategy which has long been part of their toolkit. If the volume of purchases is large enough it might widen artificially the contango by pushing up the futures prices before the true supply and demand fundamentals finally take over.¹⁰

Lastly, much more important in size but far less transparent are the inventories run by the states themselves. It is no exaggeration to say that having access to a secure supply of oil is absolutely vital for a modern economy since oil shortages can trigger riots or even revolution and wars as has been the case more than once in history. Though oil issues have always been high on the political agenda it seems that we have entered a new era. Indeed, fears from the looming peak oil associated with an ever-increasing world price sparked a race to the energy self-sufficiency. If the U.S. government primarily bet on its own huge non-conventional oil reserves, China actually follows an alternative strategy of buying petroleum output in advance to capitalize on the current crude weakness. Therefore, in addition of buying as much oil assets as they can all through the world (e.g., platform, fields, companies,...), of signing a deal with Hugo Chavez granting them a priority access to the Venezuelan oil in exchange for massive investments into the country's infrastructure, China is building tremendous stocks. By 2020, the official target alone is to hold 90 days of supply (e.g., about 1.5 billion of barrels) within the Strategic Petroleum Reserves (SPR). One never knows with China but the fact that its crude imports grew at a record pace over the first half of 2016 indicates that the country is likely hoarding crude (nearly 95 million of barrels in the first quarter according to Bloomberg). Adding to this the fact that India which imports 75% of the petroleum it consumes is following the same strategy and one ends up with substantial physical quantities removed from the market and carried over to meet further needs, thus impacting both the short and long-run price dynamics. Put it another way, the public storage demand even though out of sight must not be out of mind.

A BRIGHT OR BLEAK OUTLOOK?

In essence, the oil market is characterized by a sluggish supply and a multifaceted demand really hard to square. In addition, both of them are very inelastic, in the short-term at least. Bringing into the overall picture the occurrence of shocks affecting both the supply and the demand sides of the global oil market and the resulting final cocktail can do nothing but induce steep and large price swings in the short to medium-run. Finding your way in these successions of booms and bust episodes is a tricky task, to put it mildly. As I

¹⁰ Critics of the “financialization” of commodity markets often blamed speculators for their destabilizing effect on prices. The scientific community is deeply torn apart by this issue between the empirical studies showing the significant role speculation is playing in the volatility of commodity prices (Singleton, 2014, Basak and Pavlova, 2016) and, inversely, those arguing that it has no or very little impact (Kilian and Murphy, 2014, Knittel and Pindyck, 2016).

have tried to show so far the better and wiser perhaps is to stick to the market fundamentals which ultimately dictate the prices in the longer term. So, let us do it now in an attempt to answer the question of where the oil price is heading to?

On the bearish camp, the arguments rest on *(i)* the record high-levels of inventories likely to cap any crude price upticks for several months into the future, *(ii)* the fast rise in the Iranian production coupled with more and more efficient U.S. shale oil producers ready to restart drilling as soon as the price is crossing the \$50/barrel barrier, as suggested by the modest increases in the U.S. rigs count in the last few weeks, *(iii)* the stance in the U.S. monetary policy toward a normalization of interest rates and post-Brexit uncertainties which both in strengthening the dollar value are weighing on the dollar denominated oil and *(iv)* the pessimistic view regarding the global economic growth following the “great stagnation” theory of Tyler Cowen. It turns that the market is still widely oversupplied and the last four-month price recovery is nothing but a fortunate conjunction of circumstances mainly caused by the temporary supply outages which occurred in Canada (wildfires), Nigeria (Avengers attacks), Venezuela (near bankruptcy) and Libya (political instabilities).

To support their view, the bullish advocates point to *(i)* the huge slashes in capex investment expected to exceed 1 trillion and even more depending on the length of the current supply glut, *(ii)* the no fewer than 350,000 workers which have been fired in the oil sector across the world since 2014, most of whom will not come back as they have moved on to other industries, *(iii)* all the equipment idled and scrapped during long periods of time which need extensive repairs before becoming productive anew, and *(iv)* the lenders scalded by the heavy losses incurred so far and now more than ever reluctant to open new credit lines. The combination of massive layoffs, severe cancellation or postponing of new development projects and a drying-up of credit, will trim for a while the production capacities even if there is a spectacular price rebound. In other words, by leaving the oil sector with loans, labor and equipment shortages, the last crude crash have sowed the seeds for a sharp rally in prices as soon as 2020, given the strains on supply imposed by the emerging economies, China and India ahead.

All in all, if the mainstream view among investors is a crude price fluctuating between \$40 to \$60/barrel before climbing up again around \$100 by 2020, the current market fundamentals do not look crystal clear to everyone. Indeed, the most bearish forecasts stand to a crude price sliding to as low a level as \$10 to \$20 per barrel by the fall of this year while, inversely, the most optimistic predictions expect the spot price reaching the \$80/barrel mark as early as 2017. These upper and lower bounds on prices define an amazingly similar interval as the aforementioned 95% confidence interval when the price was assumed to follow a random walk. Sharp booms and busts cycles are definitely inherent to commodity markets and oil is no exception. Concerning the latter, the only thing that can be expected is a shortening of the price cycles due to the recent U.S. shale revolution. That is why, rather than trying in vain to predict the unpredictable, theoretical and empirical economic research must keep on building models, whether purely statistical or theoretical, with or without microeconomics foundations, which are internally consistent and able to deliver insightful explanation with respect to the behavior of prices on both the spot and forward markets.

5.2 INTRODUCTION

The preamble could not better illustrate the fact that navigating the extremely volatile commodity markets cannot but rely on relevant dynamic models resting on sound microeconomic foundations. Specifically, these frameworks must featured the decisions of individual agents made over time in reaction to unexpected shifts in the supply and demand fundamentals. In commodity markets, the crucial trade-offs faced by the various actors have to do with investment and storage. It is no surprise then if, to assess the supply and demand balance of crude oil, the practitioners look closely at the inventory levels and rig counts, a metric often used to proxy the level of capital expenditure. Lastly, these are forward-looking decisions which often involve substantial amounts of money and sunk costs. This mainly explains why, over the past few decades, storable commodity markets have seen tremendous growth in the type, scope, and maturity of tradeable forward contracts, which typically offer an appreciated price insurance to all the market participants in such an uncertain economic environment. Hence, the interaction between the physical market and the future market warrants a theoretical framework able to represent with accuracy a consistent relationship between market fundamentals and their corresponding spot and futures prices.

Models of firm investment in the macroeconomic literature have been used to study the implications of firm level nonconvexities for aggregate investment dynamics. Along the same lines, real option theory has been applied to investment models with nonconvex adjustment costs as developed in Dixit and Pindyck (1994) but the link between the physical market and the corresponding spot and futures prices has not been studied explicitly. On the other hand, competitive storage models, and in general term structure models of commodity markets, have addressed the link between market fundamentals and prices, yet mostly abstracting from the firm's investment decision. Additionally, empirical validation of the underlying theories has begun at a time when most forward markets were still in their infancy and therefore widely overlooked. In light of the ever-increasing prominence of financial markets, it is fair to say that valuable insights can be gained also from the finance literature which focuses on the links between physical and financial markets, namely the relationships between the market fundamentals and the return on different commodity futures contracts. The idea being that futures markets provide a suitable data laboratory for real time testing of the dynamics implied by such a forward-looking model.

This chapter aims at connecting and building upon three strands of the finance and economics literature so as to feature the essential structural forces driving the commodity price in the world market. In particular it hones in on the interaction between storage and investment by showing that the presence of storage brings forth features in the investment and commodity price dynamics that cannot be accounted for when focusing only on investment. Even more noticeable, exploiting the positive relationship between the levels of inventories and the forward price volatility, we find that storage has a crowding-out effect on investment.¹¹ The crude oil market will be used as a guideline illustration since it embodies, fairly well, this crowding-out phenomenon as well as the occurrence of booms and busts cycles characterizing the prices behavior of most commodities.

¹¹ This positive correlation has even been empirically validated in Fama and French (1988) and Ng and Pirrong (1994).

The results shed light on (i) the importance of introducing storage in an irreversible investment model to generate the price and investment patterns observed in the data, (ii) the key role of the storage arbitrage condition in dictating the impact of the irreversibility constraint on the timing of investment, while causing a crowding-out effect of storage on investment, and (iii) the close relationship between the market fundamentals and the term structure of forward curves given that the behavior of investment and storage are better reflected in the slope of the forward curve rather than in the levels of spot and futures prices which are mainly governed by global business cycles. Nonetheless, if our theoretical framework captures well the core forces governing the observed dynamics in the crude oil market it is unable to generate sufficiently persistent volatility in the futures prices, a common issue of this type of dynamic commodity market models.

The core logic of the present study is straightforward. First, we look at the supply and study to what extent the investment and its associated constraints (e.g., irreversibility and adjustment costs) can generate dynamics in prices similar to those observed on the global commodity markets. Then, turning to the demand side one cannot ignore the large body of literature dedicated to the competitive commodity storage model showing the key role of the speculative demand for inventories in the price discovery (Wright and Williams, 1982, Deaton and Laroque, 1992, 1996). So far both literature on investment and competitive storage have been developed quite independently of one another and we believe that bringing storage into the mechanics of the mere capital accumulation model might help to come up with a consistent story about the functioning of global commodity markets. The intuitive gist behind is that storage, by inducing conditional heteroskedasticity in prices, is an endogenous source of time-varying uncertainty affecting the timing of investment decisions. The impact of time-varying volatility on investment has been studied using real options pricing techniques, elaborated in Dixit and Pindyck (1994).¹² However, in this vein of the literature, heteroskedasticity in the price is often imposed through an exogenous stochastic process.

We start by an extensive literature review, not only to get an overview of the existing structural dynamic models aimed at understanding the behavior of commodity prices, but also to highlight the strong complementarities between them, which have yet to be taken into account. The effects of uncertainty, irreversibility and capital adjustment costs have long been explored by the investment literature but rarely have they exploited the capacity of inventory building to explain the dynamics of investment. For its part, the canonical commodity storage model in the tradition of Gustafson (1958), often contends with either an inelastic supply subject to random shocks (Deaton and Laroque, 1992, 1996, Cafiero et al., 2011b, 2015) or a rather crude modeling of the supply response silent about the underlying capital accumulation mechanism (Wright and Williams, 1982) and Gouel and Legrand (2016a); this is not surprising given that it has been primarily used for analyzing the price behavior of agricultural products.

In both types of models, the agents have rational expectations, thereby taking forward-looking decisions mirrored in the forward markets. This is precisely where the finance literature related to the hedging strategies, in particular literature on normal backwardation and hedging pressure (both based on the market fundamentals), comes to square the circle. In the descriptive analysis which follows we turn to the crude

¹² See for instance Kellogg (2014) who exactly follows this approach in his empirical testing of the options value theory in the oil industry.

oil data and show to what extent investment and storage are complementary, but also and more broadly we explore the interactions between the main variables involved at different time horizons. All of these relationships portray a fairly consistent picture of the endogenous dynamics of the world oil market and thus call for connecting investment and storage models while exploring the consequences on the term structure of forward curves. Next, in an attempt to keep the essential features of each modeling strategy, we lay out the general framework and derive the theoretical insights associated with the variety of economic restrictions, namely the crucial non-negativity constraints on both the investment and storage. Lastly, relying on two different capital accumulation models with irreversible investment depending on whether a speculative storage demand is introduced, a series of simulations is provided to support the relevance of considering the effects of storage on investment and to investigate in which dimensions the model does not work well.

The chapter falls as follows. Section 5.3 summarizes the three streams of literature along with the underlying theories from which are derived most empirical models of commodity markets. Section 5.4 combines theories and data so as to paint a consistent picture of crude market dynamics. The general framework with its associated theoretical insights are outlined in Section 5.5. Section 5.6 follows with simulations and discusses the results. Section 5.7 concludes.

5.3 COMPLEMENTARY THEORIES: A LITERATURE REVIEW

In the economics and finance literature, the majority of dynamic equilibrium models explaining the commodity price formation from market fundamentals rest on the investment and storage theories which provide the microeconomic foundations behind the agents' behavior. In addition, the forward-looking decisions made by market participants are translated into the term structure of commodity futures prices, which in turn affects the current actions. All these effects running both ways call for looking also under the hood of futures pricing and forward market dynamics mostly studied in the finance literature. Highlighting synergies and drawing insights from these theoretical developments is the purpose of this section.

5.3.1 INVESTMENT DYNAMICS AND CONSTRAINTS

Investment projects are more often than not met with large sunk costs, which make them partially if not mostly irreversible. The cost of adjusting the capital stock has drawn much attention in the investment literature. Evidence on the presence of nonconvex firm-level capital adjustment costs and investment irreversibilities is extensive. Standard models of investment, such as q-theoretic models, generally assume that firms can smoothly and continuously adjust their capital. Besides being more tractable, a model with convex adjustment cost render investment less reactive to shocks and introduce serial correlation to its dynamics. This is indeed an attractive feature in the model as it can deliver the persistence observed in the aggregate investment data.

However, when it comes to describing firm-level behavior, models with convex adjustment costs perform poorly. Underlying the representative firm model of investment with quadratic costs is the assumption that, while the individual firm might face non-convex adjustment costs resulting in lumpy firm-level investment patterns, irregularities are smoothed out through aggregation. Since firms adjust their capital stocks

asynchronously, at the aggregate level lumpiness disappears and the capital stock adjustments can be well described by convex adjustment costs. This reasoning provides the justification for the use of a representative firm facing quadratic capital adjustment costs.

To assess the soundness of this short cut, models on aggregate investment turned to study microeconomic investment decisions. Doms and Dunne (1998) cast doubt on the smoothness of capital adjustment at the firm level using micro-data on firm investment distributions. Subsequently, Abel and Eberly (1994), Caballero and Engel (1999) and Cooper and Haltiwanger (2006) as well as references therein, investigate the relevance of different adjustment costs for both firm-level and aggregate investment dynamics. They show that firm-level investment is indeed lumpy as they would like to adjust more when there is a capital shortage and less when they have access to capital. These features of investment point to microeconomic nonlinearities, i.e. both non-convex adjustment functions and investment irreversibility. Nevertheless, lumpiness of investment at the firm-level has been found to disappear at the aggregate level. Thomas (2002) demonstrates how general equilibrium price effects wash out firm-level investment lumpiness and thus pegs nonconvexities in capital adjustment costs as inconsequential for business cycle analysis. More recently, Bachmann et al. (2013) and Bachmann and Ma (2016) nuance the debate on the relevance of micro-economic lumpiness for macroeconomics by pointing out that what can settle the issue is the relevant strengths of price and adjustment cost responses. The difference between firm-level models of aggregate investment and those of the “representative” firm is that the former are able to generate nonlinear aggregate investment. The presence of a hazard rate of adjustment that depends on the gap between the firm’s level of capital and the desired one is the key to matching higher moments of aggregate investment. Therefore as in Caballero (1999), these microeconomic non-convexities generate an important “time-varying/history-dependent aggregate elasticity” of investment to shocks by allowing changes in the synchronization of firms’ capital adjustments. Cooper and Haltiwanger (2006) investigate the relevance of different adjustment cost specification for investment at the firm, sector and aggregate levels. They found that investment whether at the firm or sector level is best described by a model which includes non-convex capital adjustment costs as in Abel and Eberly (1994) and Caballero and Engel (1999).

However, a more complete examination of the commodity markets dynamics requires looking at the second pillar of the supply and demand fundamentals, namely the demand side in which storage is central.

5.3.2 THE COMPETITIVE STORAGE MODEL

A no less lengthy literature focuses on the effect of storage in the formation of commodity prices. The competitive storage model with rational expectations and a non-negativity constraint on inventories in the tradition of Gustafson (1958) has been the workhorse of neoclassical studies in the literature of commodity price volatility. Deaton and Laroque (1992, 1996) pioneered its empirical validation by developing techniques to confront the observed price data with a version of the model with inelastic supply modeled by either i.i.d. or autocorrelated random shocks. Eventually they draw mixed conclusions. On one hand, it proves useful in reproducing most of the prominent features observed in commodity prices (persistence, nonlinearity, positive skewness and excess kurtosis) in particular as a result of the key non-negativity constraint on storage which

brings forth two different price regimes. On the other hand, it is unable to match the very high levels of serial correlations observed in commodity prices even after allowing for persistence in the supply disturbances. Most of the critiques have been addressed through several recent improvements on both the numerical (Cafiero et al., 2011b) and empirical fronts (Cafiero et al., 2015, Guerra et al., 2015).¹³

However, so far existing econometrics studies conducted on the storage model, in relying on information taken from spot prices alone, have been limited to its starkest specification, that is without allowing for neither structural demand shifts nor a supply reaction to prices although versions of the model with elastic supply have existed for a long time.¹⁴ Indeed, Wright and Williams (1982) demonstrate the implications of supply responsiveness in terms of the price behavior generated by the model. Interestingly, they show that storage has a destabilizing effect on the expected price and in turn on the planned production, but also that it is unclear whether planned production and storage act as substitutes or complements since the mean level of storage is left virtually unchanged. Therefore, from an investment standpoint accounting for storage should make it more volatile as its expected return is less certain. Put it another way, it is not so much the long-run average of investment but its dynamics and timing which might be primarily impacted by the introduction of storage into the framework.

Lastly, if most empirical studies of the storage model have been implemented on agricultural commodities and using annual data due to the seasonality, the issues related to the interactions between investment and storage might be more relevant for commodities such as petroleum or metals whose production often requires costly and long investment lead times.¹⁵ Indeed, as stated by Gilbert (1995), these supply constraints should translate into long periods of prices lying below the long-run average of production costs.

In this spirit and still in an effort of extending the fitting possibilities of the storage model, Dvir and Rogoff (2014) build a version for the oil market embedding both elastic and inelastic supply regimes along with persistent demand shocks. Specifically, their modeling accounts for a single trend in both demand and production so that prices are left stationary. The model is then stationarized by scaling all quantity variables by the aggregate income, measured by a global economic activity measure, assumed to be the major driver of the growth in consumption. This set-up, with a rich structure of shocks, allow them to highlight the strong cointegrating links between the prices and the market fundamentals of supply, demand and inventories as predicted by the canonical storage model but also exhibited by the true data. Even more importantly perhaps, they demonstrate that the correlation between prices and inventories can run in both directions depending on whether or not supply is flexible enough to keep pace with the rising trend in demand. In the latter case, price and inventories tend to move in the same direction.

Lastly, as briefly evoked in Chapter 2, given the forward-looking nature of both types of models, chances are high that investment, storage and their subsequent interactions eventually are mirrored in the term structure of commodity forward prices; a point the financial economists have long been recognized.

¹³ See chapter 2 for more on these recent developments.

¹⁴ The lack of reliability and availability of data on quantities mostly explain why they have been overlooked until now. Taking to the data on prices and quantities richer model specifications is precisely the topic of Chapter 3.

¹⁵ From a strict statistical view point, another advantage is the possibility to work with monthly data given that, unlike the agricultural products, this type of commodities are less subjected to the seasonality constraints.

5.3.3 THE DETERMINANTS OF FUTURES PRICING

Although usually designed to model the risk premium of commodity futures contracts and assess the performance of trading strategies, valuable insights can be gained from the literature on commodity futures pricing which provide theoretical foundations to the behavior of prices on the futures market. Indeed, theories of the determinants of speculators' profit might help better understand the information which can be extracted from futures prices and more broadly from the term structure of the futures market. Among them, only those related to the fundamentals of supply, demand, and inventories, will be covered.

The first strand of the literature rests upon the theory of storage in the tradition of Kaldor (1939), Working (1949) and Brennan (1958) which delivers a standard expression for the link between forward and spot prices given by the following storage arbitrage equation:

$$F_t(T) = S_t(1 + R_t(T)) + C_t(T), \quad (5.1)$$

where $F_t(T)$ stands for the forward price as of time t for delivery at time T , S_t is the spot price, R_t is the interest cost of storage and C_t is the total net of interest cost of carry.¹⁶ Telser (1958) is among the first to propose an empirical validation of this theory by documenting the close relationship between the inventory levels and the basis (also called roll-yield) written as the spread between the spot and the nearest to maturity future contract. More precisely, abundant stocks is regarded as a fair signal of a contango regime that is a negative spread or an upward sloping forward curve. Also relying on the storage theory, Fama and French (1988) complement the Samuelson hypothesis according to which (i) the volatility of forward prices has to decline with the contract horizon and (ii) forward prices in contango are always less volatile than those backwarddated. Working with a set of metals and using the sign of the interest-adjusted basis as a proxy for the levels of inventories (e.g., $F_t - (1 + r)S_t$), they demonstrate that whenever the levels of stocks is running high (positive adjusted-interest basis), the spot and futures prices are as volatile. Part of the explanation has to do with the lockstep variations of both current and expected spot prices linked by the storage arbitrage equation (5.1).¹⁷ If inventories are running low, supply and/or demand shocks cannot be buffered by a release of stocks which lead to variations of current spot prices to be greater than those of the futures prices for which the market anticipates supply and demand responses. That is why Fama and French show that the spot price of metals is more volatile around the business cycle peaks when demand is high and is satisfied by a draw down of inventories.

Another stream of literature revolves around the Keynes-Hicks theory of normal backwardation stating that, since hedgers are usually net short in the futures market (e.g., the number of selling positions exceeds the buying one in the forward market), the future price deviations from the expected spot price can be attributed to a risk premium rewarding the traders willing to hold the long positions. Nevertheless, the lack of empirical

¹⁶ $C_t(T) = Wf_t(T) + Rp_t(T) - Cy_t(T)$. $C_t(T)$, total net of interest cost of carry, which can possibly include transportation and warehousing fees Wf_t , risk premia Rp_t and convenience yield Cy_t . Following the literature of commodity storage model, we will assume zero convenience yield and that agents are risk neutral and thus risk premia are zero.

¹⁷ In the basic storage model without convenience yield, whenever storage is positive, the adjusted-interest basis equals the physical storage cost.

evidence led to refinements allowing the hedgers to be either net-long or net-short in aggregate (Cootner, 1960).¹⁸ In the latter case, forward prices are below the spot price in a similar manner to the hypothesis of normal backwardation. Inversely, when the number of hedging positions is net-long the forward curves increase with time to maturity and the market is in contango providing the speculators an incentive to take the opposite short positions. Hence, according to the hedging pressure hypothesis both backwardation and contango are rational states of the futures market from the speculators standpoint. Using proprietary data Dewally et al. (2013) give an illustration for crude oil, gasoline and heating oil. Specifically, they find a systematic positive gain whenever a given trader is taking the opposite position in sign of the net hedger's one. Gorton et al. (2012) provides an optimization-based approach to endogenously model the basis along with the risk premium. Integrating within the same two-periods framework both the theories of storage and normal backwardation they empirically explore the connections between the inventory levels, the basis and the risk premium. Running a series of regression on monthly futures and inventories data of 31 commodities, they demonstrate that, as dictated by the storage theory, the relationship between the levels of stocks and the futures basis is negative and convex. In addition they also show the predictive power along with the negative correlation between the amount in store and the risk premium as posited by the theory of normal backwardation, but do not find significant evidence in favor of the hedging pressure hypothesis.

Overall, future modeling insights can be gained from these results which point to (i) not favor one state (backwardation/contango) over another but instead looking at the net positions of hedgers, (ii) interpret the Samuelson hypothesis as a function of the inventory levels which might be violated whenever commodity is abundant enough so that stocks are high, and (iii) consider storage at the core of the modeling given the strong links between the physical market fundamentals and the term structure of commodity prices.

However, models based on competitive storage cannot account for the longer term dynamics of the term structure since inventories only affect the short end of the forward curve. It turns out that the long term behavior of the term structure might be governed by elements such as the structure of production, new discoveries, investment dynamics, and prices of substitutes. Two avenues have emerged to address this shortcoming. One the one hand, reduced form models of futures prices as in Brennan and Schwartz (1985), Schwartz (1997), and Schwartz and Smith (2000), take spot prices and other factors which can influence futures prices as exogenous stochastic processes. On the other hand, Litzenberger and Rabinowitz (1995), Carlson et al. (2007) and Kogan et al. (2009), use a production economy with adjustment costs, to endogenously determine both the spot and futures prices. A common assumption in these models is the irreversibility of the investment or extraction decision. The presence of a nonconvex adjustment cost aligns this vein of the literature with the investment literature discussed above. The study of the impact of investment dynamics on prices builds the link between the literature related to investment project valuation and prices and the one focusing on investment dynamics at the different firm, sector and aggregate levels.

From an empirical perspective, the term structure of commodity futures prices displays patterns that set commodities apart from other assets. In Litzenberger and Rabinowitz (1995), Carlson et al. (2007) and

¹⁸ Hedging pressure is defined as the difference between long and short positions taken by the hedgers divided by the total open interest positions. The required data on trading positions is available from the Commodity Futures Trading Commission (CFTC)'s website where the hedging positions fall into the class of "commercial traders".

Kogan et al. (2009) it is noted that commodity futures curves are often backwardated, implying that the spot price of a commodity enjoys a premium over the futures prices.¹⁹ Litzenger and Rabinowitz (1995) cast their analysis in an optimal exhaustible resource extraction framework using option pricing techniques which places the exhaustibility of the resource at the center of the analysis. The option value of waiting associated with the depletion of a finite resource in a stochastic environments necessitates, at least, that the spot price of the commodity exceeds the present value of the future price in order to produce. Carlson et al. (2007) and Kogan et al. (2009) take up a similar approach but instead of accounting for the non-renewability of the commodity, they exploit the irreversibility of investment along with potential adjustment costs in the production of oil. Put differently, as in Bertola and Caballero (1994) and Caballero and Engel (1999) these investment constraints are instrumental for the empirical success of sector-level investment models. This latter strategy allows not only to explain the occurrence of both backwardation and contango in commodity markets, but also to generate time-varying volatility of commodity spot and futures prices, with price volatility increasing in the degree of backwardation or contango. The volatility of the forward prices is decreasing in the time to delivery as predicted by the “Samuelson effect”. Part of the explanation has to do with the fact that the mean reverting spot and futures prices give way to a decline in uncertainty as the contract horizon lengthens. In the short-run, demand or supply shocks result in large fluctuations of the spot and short-maturity futures prices because current supply is rather inelastic. At intermediate horizons, the effect of the shocks are dampened by producer’s supply responses. Regarding the longer contract maturities, whether supply and demand shocks or inventory levels, have little effect over the long-run equilibrium price which is governed instead by dynamics in investment, commodity production, fresh discoveries, and other longer run factors.

Nevertheless, there can be instances when the volatility at shorter contract horizons is increasing and eventually dies down as the contract horizon goes farther into the future. The nonmonotonicity of volatility along the forward curve is due to the impact of high inventory levels on short contract horizons. Routledge et al. (2000) explains that very high inventory levels in the current period lower the probability of stockouts for the next few periods confirming the conclusions of Fama and French (1988). Therefore, it is possible, when inventories are high, for the volatility of near term contracts to be lower than the volatility for the subsequent contracts, thereby violating the “Samuelson effect”.

Furthermore, the level of volatility varies with the degree of backwardation or contango. Routledge et al. (2000) with storage but also Carlson et al. (2007) and Kogan et al. (2009) through a model with investment constraints, examine the relation between volatility and the slope of the forward curve. Volatility is higher when there are no inventories to smooth fluctuations in supply. This is the case of a backwardated forward curve. In contango, when the future price is higher than the spot price, inventory levels are positive and therefore can buffer the impact of shocks. Nonetheless, as posited in Fama and French (1988) and Routledge et al. (2000) when the inventories reach a certain level, spot and forward prices tied through the storage arbitrage equation (5.1) exhibit lockstep fluctuations so that the volatility of futures prices starts rising again. Interestingly, Kogan et al. (2009) stress that the observed V-shape of the volatility of futures prices can be

¹⁹ In fact this result really depends on the sample period covered as this higher frequency of backwardation holds only until the late 1990’s after which the market has been found to be in contango much more often.

obtained either through an irreversible investment model with capacity constraints as is the case in their paper, or through a storage model provided that storage capacities have both lower and upper bounds.²⁰ They close their article stating that if storage should be more relevant to explain the fluctuations of the short-end of the forward curve only the investment and capital dynamics are likely to deal with the back-end movements.

All in all, to some rare exceptions the modeling of commodity market fundamentals takes roots either in the storage theory or in the literature related to the irreversibility of investment and capital adjustment costs. However, along with the developments of futures market, there has been a growing interest in attempting to account also for the term structure of forward prices in which are reflected the forward-looking decisions of the market's participants. Despite this common goal and apparent complementarities, both modeling approaches have been developed quite independently of one another.

With this in mind, we use Cooper and Haltiwanger (2006)'s work as a point of departure for our study to model the commodity supplier's capital dynamics. By working within this framework we believe not only to stick to the current trend in the literature on firm(sector)-level investment, but also to echo Kogan et al. (2009)'s motivation for emphasizing the importance of the supply side of the commodity market in order to reproduce the most prominent features of commodity price. The key assumption in their model is that the representative commodity producer cannot resell his already installed capital leading to a time-varying elasticity of supply with respect to shocks. While Kogan et al. (2009) abstract from the storage dimension in the commodity market, we want to bring together the price smoothing features of storage and capital adjustment rigidities in the same framework, so as to shed light on the inner working of commodity markets and the accompanying price dynamics. Additionally, we build upon the recent developments in the literature of the storage model through a more complex specification of supply responsiveness and persistence in the shock processes while taking a close look to the implied variations of quantities and prices both on the spot and forward markets.

5.4 THEORY AND FACTS

In this section, bringing altogether the above three investment, storage and futures pricing streams of literature, we will try to sketch out a narrative for commodity booms and busts cycles. Then, we turn to the global oil market data to check for relevance and adequacy with the theory, thereby motivating and guiding the final modeling approach.

5.4.1 A TALE OF INVESTMENT AND STORAGE

In capital intensive industries, production often requires substantial fix capital investments. In this respect and according to the classic hedging theories, at the time of investment risk-averse producers will use the futures market to lock in future selling prices by taking short positions in futures (e.g., selling futures contracts) pushing the market in backwardation until the installed capital becomes productive and eventually the output

²⁰ The upper-bound on inventories is even not necessary if you recall the Fama and French (1988) and Routledge et al. (2000)'s explanation for the observed increase in futures price volatility with the degree of contango.

comes online. Once the supply starts flowing on to the physical market, the spot price falls so that now it is the turn of industrial consumers willing to secure their future purchasing prices to hold long positions in the forward market driving upward the prices of futures contracts sending the market in contango. If, say, in response to an adverse economic shock the demand for consumption turns out to be lower than expected when the investment decisions have been made, production capacities outsize the optimal level required to satisfy the actual demand. The thing is that, since operating costs for maintenance and pumping are tiny as compared to upstream investments, producers, fighting for market shares, keep on pumping the oil to maintain a certain flow of cash. As a result, it becomes more profitable to build inventories and to postpone investment. As the capital stock is gradually decaying, the production capacity along with the supply shrink slowly absorbing the relative surplus and restoring the balance. Hence, the tightening market gradually moves back from contango to backwardation, inventories are drawing down and the resulting environment of higher prices stimulates investment again.

To summarize and combine these facts with the underlying theories mentioned above, at full carry, the forward market is in contango, spot and futures prices are moving one for one because they are tied down by the storage arbitrage equation. This future volatility translates into a rise in uncertainty, which destabilizes the investment while creating speculative opportunities supportive of storage. In contrast, when the market is in backwardation the spot price is high and the volatility of futures prices declines with the time to delivery in line with the Samuelson effect so that it is less profitable to store but the investment conditions improve.

All these characteristics are well epitomized by the global oil industry whose data are also available and relatively reliable, thus offering a perfect field of experiment.

5.4.2 THE DATA

The data are monthly and span from January 1986 to December 2014.²¹

QUANTITIES: The global production and inventory levels data, noted Q and S respectively, are taken from the Energy International Administration (EIA).²² To remove the trend, they are normalized by dividing the levels to the previous twelve months moving average as in Gorton et al. (2012).

PRICES Monthly futures prices are constructed using the daily observations of the New York Mercantile Exchange (NYMEX) light sweet crude oil contracts.²³ The monthly futures price is equated to the last daily price of a given month. Since futures contracts are traded everyday, prices update accordingly. Consequently, the last day of the month price reflects all the information available that month. Several contracts are traded on each day in our data. To categorize each contract according to the number of months to its maturity, we

²¹ The starting date is dictated both by the availability of the monthly spot price data given by the Energy International Administration (EIA) and the CFTC data related to the traders' positions in the forward market. Although longer monthly series of oil spot prices are available, for instance from the World Bank pinksheet or the International Monetary Fund (IMF), starting in 1986 is not too big a deal since the oil futures market has been first traded in 1983 and was at the beginning not sufficiently liquid to be really relevant.

²² <https://www.eia.gov/petroleum/>.

²³ <https://www.quandl.com/collections/futures/cme-wti-crude-oil-futures>.

identify the maturity date for each contract according to its month of delivery; the date of expiry for each contract is preset. Following Kogan et al. (2009), we sort each contract according to months to delivery. We divide the number of days it has left to maturity by 30 and round off the result. For contracts with less than 15 days to maturity, we add a month. The selected contracts are those maturing in the next 1, 6, 12, and 18 months (hereafter denoted F_1 , F_6 , F_{12} and F_{18}). While this market is liquid, especially for the short term maturity contracts, there are still missing values for daily prices. To address the sparsity of the data, we use the spread between two consecutive contracts to fill in the missing daily price.²⁴ The spot price P is the West Texas Intermediate (WTI) crude price taken from the EIA. Spot and futures prices are deflated by the US CPI following the common practice in the literature (Kilian, 2009, Hamilton, 2009, Knittel and Pindyck, 2016, Baumeister and Kilian, 2016) and expressed in deviation from the same log-linear time trend.

THE SLOPE OF THE TERM STRUCTURE (SL): it is obtained by taking the logarithm of the ratio between the first and the twelfth months forward contracts ($SL = \log(F_{12}/F_1)$). A negative (positive) value of the demeaned slope $SL = \tilde{S}L - \bar{S}L$ is indicative of a backwardated (contango) market.

GLOBAL REAL ECONOMIC ACTIVITY INDEX (GRA): The real economic activity is measured by the Dry Cargo Bulk Freight Rates as constructed in Kilian (2009) and available from the author's personal website.²⁵ The author also opts for a log-linear trend modeling to focus on the cyclical fluctuations solely. Though not free from drawbacks we prefer this measure to the less specific world GDP growth, such as the OECD +6 monthly GDP data used in Dvir and Rogoff (2014), to assess the global demand pressure for industrial commodities often cited as one of the primary driver of prices.

INVESTMENT RATE (I): the real capital and exploration expenditures in the oil sector are only available at an annual frequency from the IMF.²⁶ However, the oil services company Baker Hughes publicly publishes the world number of oil rigs on a monthly and even weekly basis.²⁷ Thus, we build a monthly series of investment rate, denoted I , by first regressing the yearly growth rate of capital expenditures on the one of annual rigs. We use the estimated relationship in combination with the monthly growth rate of rigs to recover the corresponding growth rate of investment at the desired monthly frequency, which thus can be either positive or negative.²⁸

²⁴ The spread between two consecutive months, $\Delta_{1,2} = F_1 - F_2$, is constructed using daily prices. Then for all the days where the spread is missing, we fill it out with the closest available spread. If, for a given day, F_1 is missing, we fill it in using $F_2 + \Delta_{1,2}$. Once we obtained the constructed daily prices, we use the last price as the monthly price. If this price is still missing, we interpolate between the two closest available prices to construct the monthly price; i.e. $F_{1,t} = \frac{F_{1,t-1} + F_{1,t+1}}{2}$.

²⁵ <http://www-personal.umich.edu/~lkilian/paperlinks.html>.

²⁶ <https://www.imf.org/external/np/res/commod/pdf/WEOSpecialAPR15.pdf> who used the proprietary database Rystad Energy UCUBE. Investment is deflated using a price index for private fixed investment in mining and oil field machinery in the United States available from the Bureau of Economic Analysis' website.

²⁷ <http://phx.corporate-ir.net/phoenix.zhtml?c=79687&p=irol-rigcountsintl>.

²⁸ For the sake of comparison with the empirical studies of Cooper and Haltiwanger (2006) and Kogan et al. (2009), in an abuse of language we will use the term "investment rate" instead of "investment growth rate" in the rest of the analysis.

HEDGING PRESSURE (H): Following Gorton et al. (2012) we obtain the historical positions of traders from the “Commitments of Traders Reports” published on the CFTC’s website.²⁹ Assuming that hedgers belong to the group of “commercial traders”, the hedging pressure variable is defined as the difference between the long and short positions held by the hedgers expressed in percentage of the total open interest positions.

We will now take look at the big picture these data portrayed and try to emphasize some of the key features.

5.4.3 EMPIRICAL FEATURES

Let us start with some descriptive statistics about the variables in consideration. The main moments are documented in table 5.1. First, as can be seen, the less persistent variable is by far the investment rate,

Table 5.1. Descriptive statistics of the monthly detrended observables (1986:M1-2014:M12)

Variables	First-Order AC	2nd-Order AC	Coeff. of Variation	Skewness	Excess Kurtosis
Normalized inventory	0.86	0.71	0.02	0.09	0.11
Investment rate	0.18	0.03	0.05	0.13	8.91
Normalized production	0.98	0.97	0.06	-0.70	-0.32
Slope of the term structure	0.64	0.42	0.09	-0.14	0.56
Hedging pressure	0.79	0.66	0.09	-0.07	-0.05
Global real economic activity index	0.96	0.89	0.25	0.53	-0.16
Spot price	0.94	0.87	0.31	0.59	0.64
Front-month futures price	0.92	0.84	0.31	0.66	0.94
6th-month futures price	0.95	0.89	0.31	0.46	0.14
12th-month futures price	0.93	0.89	0.32	0.46	0.24
18th-month futures price	0.96	0.92	0.32	0.39	-0.09

Notes: The index of global real, the Spot and futures prices are log-linearly detrended.

I, with the two first-order correlation coefficients of 0.18 and 0.02 respectively as compared to the others all in excess of 0.6. In addition, the strong persistence of storage, S, and even more the production, Q, match well with the supply constraints inherent to the oil industry previously underlined. Adding to this the high levels of serial correlation displayed by the real economic activity, it comes as no surprise that the first and second-order autocorrelation coefficients of prices, respectively, lie well above 0.9 and 0.8 at all the contract horizons. Regarding the slope of the term structure, $\tilde{S}L$, it is interesting to see that it is much less autocorrelated than the forward prices themselves (e.g., a cut by about one-third) reflecting quite frequent changes in the practitioners’ expectations about the long-run supply and demand fundamentals. These changes in expectations affect the back end of the forward curve—e.g., within a year—and lead to a market balancing between both the backwardation and contango regimes. This is also confirmed by the lower autocorrelation coefficients of the positions of traders measured by the hedging pressure variable H.

²⁹ <http://www.cftc.gov/files/dea/history/>. The CFTC contract code of the NYMEX light sweet crude oil product is 67651.

Then, turning to the values of the coefficient of variation, the volatility of the investment rate is in between that of storage and production, which is consistent with the fact that production is also subjected to random disturbances such as the disruptions related to climatic or geopolitical reasons. Furthermore, the much larger fluctuations exhibited by the spot and futures prices suggest very low supply and demand elasticities. Then again, the fact that the GRA index is almost as volatile as prices supports for the view that short-run prices variations are primarily dictated by demand shocks. The absence of any Samuelson effect, namely the decrease in the volatility of futures prices with the contracts horizon must be noted.³⁰ Actually, this is in line with the Fama and French (1988) and Routledge et al. (2000)'s findings, who clearly demonstrate that when the market is in contango (e.g., about half of the time in our sample), inventories are high and may lead to violations of the Samuelson effect which is a phenomenon more significant under the backwardation regime.

Finally, unlike production, prices are positively skewed and, along with the investment rate, exhibit fat right tails as indicated by the positive excess kurtosis coefficients. Together, these asymmetries in the prices distribution illustrate (i) the importance of considering the nonnegativity constraints on both investment and storage and (ii) the prominent roles storage and investment might play in the overall price dynamics, thereby supporting the relevance of studying the synergies among them.

The main key features of oil forward prices for different maturities are exhibited in Figure 5.1. Apart from

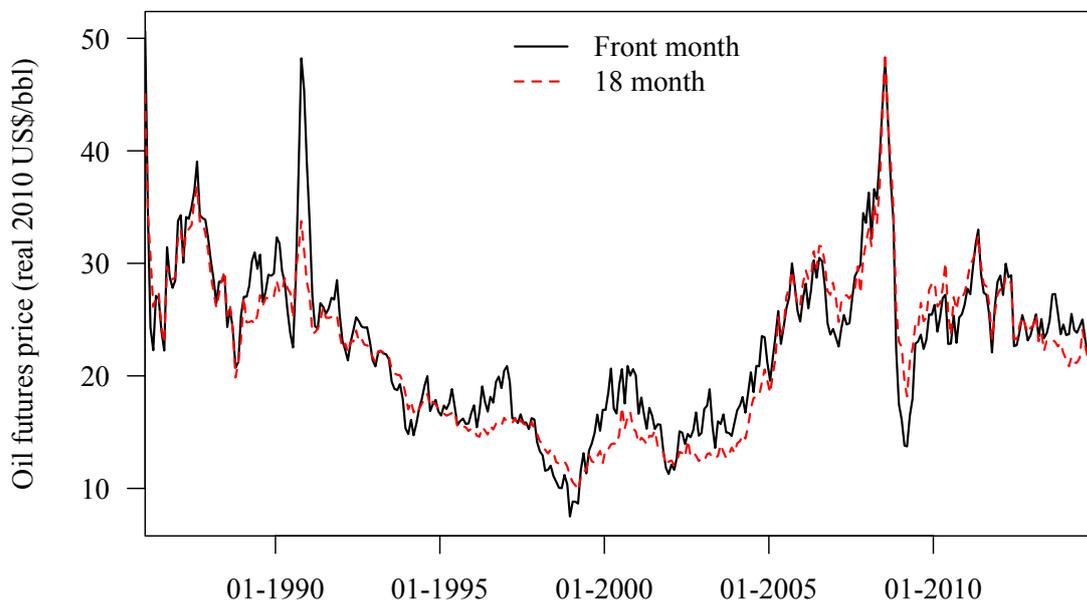


Figure 5.1. NYMEX Front-month and 18-Month Oil Futures Prices (real 2010 US\$). The prices have been deflated by the US CPI before being log-linearly detrended.

the obvious succession of booms and busts episodes along with the clusters of volatility, the mean-reverting tendency and, especially for the nearest to delivery contract, the sharp spikes leading to the noted positively

³⁰ In some way, this is partly due to our expression of volatility measured by the coefficient of variation.

skewed distribution, two points deserve particular emphasis. First, the 18-month-ahead price seems to be less volatile when the market is in backwardation—e.g., when it lies below the front-month future price—confirming the fact that the Samuelson effect should be more pronounced when prices are backwardated. Second is to note that, although over the whole sample length the market is nearly as often in contango as in backwardation, both states are quite long-lasting. For instance between the mid 1990's to the early 2000's the market was in backwardation almost all the time before reverting into a sustained contango since 2005. This further supports the resilient supply hypothesis and the irreversible nature of investment inherent to capital intensive industries such as the oil sector, where excess capacities of production take long to be absorbed and thus result in a persistent glut with ballooned inventories, a depressed spot price and an upward-sloping forward curve. Applying the opposite reasoning when the supply falls short of the demand and the outcome is empty inventories, a rocketing spot price sending the market in backwardation for a while until a series of investment in new production capacities eventually lead fresh output to come online and restore the equilibrium.

Before delving into the inner-working of the world market of oil through the study of the raw correlations across the whole set of variables, additional insightful remarks can also be drawn from a closer inspection of the investment dynamics within the oil sector, represented here by the investment rate variable I . Translated into a theoretical language, both the lumpiness and intermittent behavior of investment within a firm or a given industrial sector are microeconomic features which have long been documented (Caballero and Engel, 1999, Cooper and Haltiwanger, 2006). In particular they fit well with the nature of investments in capital intensive sector like the oil industry, which is known to involve large sunk costs (Kellogg, 2014). For the sake of comparison with the investment rate at the manufacturing plant-level as described in Cooper and Haltiwanger (2006) (table 1), we report the same key features of the distribution of our investment rate variable in table 5.2.

Table 5.2. Summary comparative statistics of the monthly investment rate

Variables	Cooper and Haltiwanger	Oil Sector (1986:M1-2014:M12)
Average Investment Rate	0.12	0.04
Inaction Rate	0.08	0.11
Fraction of Negative Investment Rate	0.10	0.09
Positive Spike Rate	0.19	0.15
Negative Spike Rate	0.02	0.01

Notes: Cooper and Haltiwanger results are based on US firm-level observations obtained from the Longitudinal Research Database (LRD) that were continually in operation from 1972 to 1988. The spikes consist of investment rates greater than 20% (e.g., about twice the mean) in absolute value in Cooper and Haltiwanger reduced to 8% in our case so as to stay comparable.

Thus defined, our investment rate variable I , seems to capture fairly well the main microeconomic patterns of investment at the firm-level. Indeed, periods of inaction—e.g., I lower than 1% in absolute value—are interspersed by positive spikes of investment. In addition, the asymmetry of the investment rate behavior where episodes of intense capital expenditures exceeding 8%—e.g., about twice the mean—hardly exist in the negative territory (less than 1% of the time), corroborates the irreversible nature of investment in the oil sector. As explained in Kellogg (2014), on the ground of investors, pull back investment and wait to

exercise the option to invest whenever they face higher uncertainty. Finally, as in Cooper and Haltiwanger (2006), the investment rate exhibits a slightly positive first-order serial correlation suggesting an imperfect synchronization of investment within the oil sector partly due to heterogeneous production costs along with very long-lasting demand shocks and possible capital adjustment costs.

On the whole, these results tend to indicate that investment decisions are fairly well synchronized across the producing oil companies so that the problem can be simply recasted into a single-agent dynamic investment problem affected by random shocks without being too concerned about aggregation issues. Furthermore, and as suggested earlier, by the positively skewed and leptokurtic distribution displayed in table 5.1, the modeling should consider investment as fully irreversible by setting a zero lower bound on I as is the case in Kogan et al. (2009).

An illustration of the destabilizing effect of storage on investment is provided in Figure 5.2. It clearly

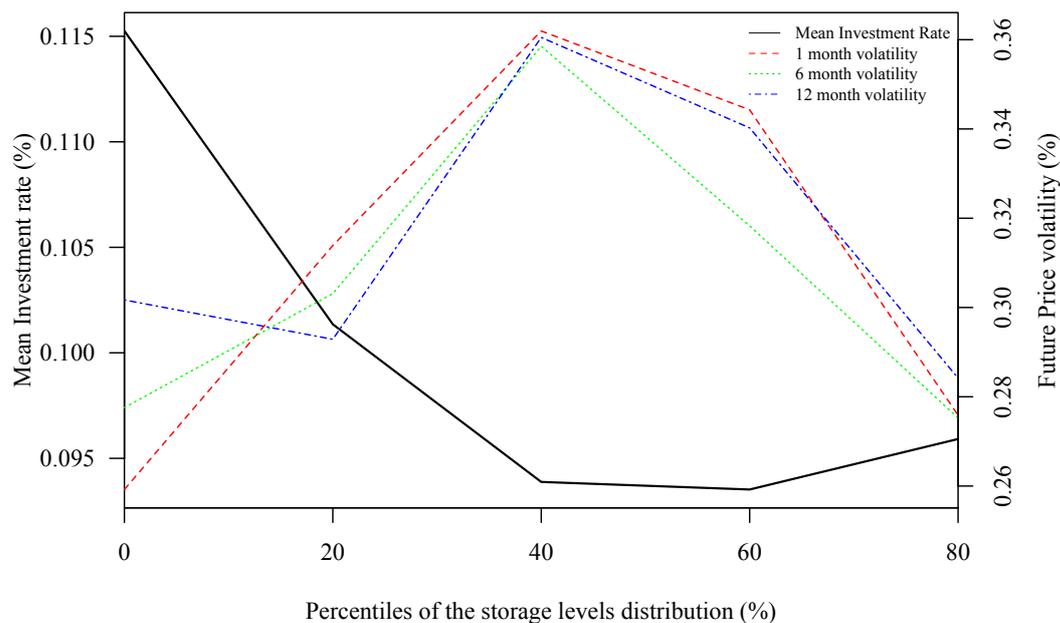


Figure 5.2. NYMEX Front-month volatility and Investment Rate with respect to the 20th percentiles of the inventory levels distribution

Notes: The left and right vertical axes respectively stand for the mean investment rate and the coefficient of variation of the forward contracts at the first, sixth and twelfth months to delivery. They are computed for each 20th percentile of the storage level distribution.

shows the effects of storage on the volatility of futures prices and, in turn, on the investment decision. Put simply, speculation through storage is associated with a rise in the expected price volatility, thereby causing an increase in the waiting value and thus a deferral of investment according. However, the relationship between stockpiling and the increase in uncertainty is broken when stocks reach a certain level (around the 60th percentile of the distribution). Everything goes as if above this threshold the market is so oversupplied that the cushion effect of inventories on price volatility outweighs the speculative destabilization. This is

further confirmed by the greater smoothing effect storage has on intermediate maturities (e.g., 6-months) as compared to the longer term (12 month).

The empirical analysis is completed by the computation of pairwise correlation coefficients displayed in table 5.3 and which appears quite consistent with the oil industry narrative delivered in subsection 5.4.1.³¹

Table 5.3. Correlation coefficients of the monthly detrended observables (1986:M1-2014:M12)

Variables	<i>S</i>	<i>I</i>	<i>Q</i>	$\tilde{S}L$	<i>H</i>	GRA	<i>P</i>	F_1	F_6	F_{12}	F_{18}
<i>S</i>	–	–0.17	–	0.27	0.16	–	–	–	–	–	–
<i>I</i>	–0.17	–	0.09	–	–	0.10	–	–	–	–	–0.09
<i>Q</i>	–	0.09	–	–	–0.23	0.27	–0.47	–0.46	–0.43	–0.43	–0.43
$\tilde{S}L$	0.27	–	–	–	–	–	–	–	0.13	0.21	0.24
<i>H</i>	0.16	–	–0.23	–	–	–	–	–	–	–	–
GRA	–	0.10	0.27	–	–	–	0.27	0.26	0.28	0.27	0.26
<i>P</i>	–	–	–0.47	–	–	0.27	–	0.98	0.96	0.94	0.92
F_1	–	–	–0.46	–	–	0.26	0.98	–	0.98	0.96	0.94
F_6	–	–	–0.43	0.13	–	0.28	0.96	0.98	–	0.99	0.98
F_{12}	–	–	–0.43	0.21	–	0.27	0.94	0.96	0.99	–	0.99
F_{18}	–	–0.09	–0.43	0.24	–	0.26	0.92	0.94	0.98	0.99	–

Notes: All the coefficients are significant at 10% and in boldface are those significant at 5%.

First, storage is negatively correlated with investment but positively correlated with both the slope of the forward curve and the traders' positions. In other words, storage increases when the market is in contango; i.e. when the slope of the forward curve rises with the contract horizon ($SL > 0$). This is the outcome of an abundant availability combined with a low spot price and long hedging positions in the futures markets ($H > 0$). Likewise, it should come as no surprise that bursts of investment are more likely to happen around the business cycle peaks when the oil consumption is stronger thereby tightening the supply and demand balance on the market. And besides, consistent with the hypothesis that investment more likely affects the back-end of the forward curve, is the significant negative correlation between *I* and F_{18} since fresh production is expected to come online.

Regarding the spot and forward prices, although slightly decaying over time, the correlations across the whole set of times to delivery remain very elevated showing actually that a great deal of the relevant information relating futures prices with the market fundamentals is embedded into the shape of the forward curve. The closeness in the behavior of both the spot and front-month futures prices illustrates the expected convergence phenomenon occurring between physical and forward markets as the delivery date is approaching. Interestingly, the level but not the shape of the term structure seems to be in part driven by the global economic activity in light of the relatively high and positive correlation coefficients between the GRA index and the prices at all maturities. Put crudely, a strengthening industrial demand is associated with an upward shift of the whole forward curve regardless of the contracts horizons. This sizable correlation justifies the introduction

³¹ Only the correlation coefficients significant at the 10% percent level are given while in boldface are those significant at the 5% level.

of a persistent demand factor as in Routledge et al. (2000) to account for such an underlying consumption growth engine which puts pressure on the supply side.

Nevertheless, further points deserve some comments, as one might be puzzled in view of the absence of significant relationships found in the true data such as those between storage and prices at all times to maturity. A possible explanation is that WTI futures contracts exchanged on the NYMEX better reflect the contemporaneous supply and demand conditions in the US than elsewhere in the world.³² Another reason has to do with the typical lack of reliability of data on quantities in general and on inventories in particular. Hidden strategic state-owned stocks added to substantial floating storage are among the factors prone to make difficult the precise assessment of inventory levels at the global scale. Having said this, the significant contemporaneous correlations between the production and futures prices qualify somewhat the disappointing weak correlations results as production is known to be much more precisely estimated than storage. Some authors like Gorton et al. (2012) decide to lag the data to account for some possible reporting time. Because of the lack of true theoretical justification for introducing such lags in the variables, and given the strong and consistent contemporaneous correlations observed between production and prices as well as between the slope of the term structure with storage,³³ we instead prefer not to try adding some hypothetical lags in the variables and to be content with the overall coherent, albeit imperfect, picture delivered by the correlations table.

In light of these results, the subsequent modeling must be able to generate endogenously and alternatively backwardation and contango states. Conjointly, these states must be accompanied by lumpy and intermittent episodes of investment and complement the storage activity, which is no longer profitable whenever production capacities falls short of the industrial demand, especially during economic booms. Indeed the relative abundance in the market goes hand-in-hand with (i) a bearish market poorly encouraging investment but rather much more inclined to support the accumulation of inventories by speculators willing to make the most of the resulting low spot price, (ii) a forward market in contango in response to the net-long positions of refiners hedging their future crude supply by buying forwards contracts, (iii) steeper fluctuations of the futures prices, since linked to the spot price through the arbitrage equation, thus leading to a very uncertain economic environment favorable to speculative storage while increasing the option value to delay investment. To what extent these stylized facts can be reproduced by embedding the speculative storage within the standard capital accumulation model with an irreversible constraint on investment is the topic further studied in the remainder of the chapter.

³² Unsurprisingly if, as in most empirical studies using the crude stocks data, when the more reliable US instead of world levels of inventories are used the correlation between spot prices and stocks is -0.10 and significant at 10%.

³³ These variables are reliable indicators of the state of the market fundamentals.

5.5 MODEL

5.5.1 MODEL'S EQUATIONS

COMMODITY PRODUCTION There is an infinitely-lived representative commodity producer operating a stock of capital goods with a decreasing returns technology, $Q_t = AK_t^{\alpha_Q} \eta_t^Q$, with $\alpha_Q < 1$.³⁴ Production is affected by a multiplicative i.i.d shock η_t^Q . This disturbance can be emanating from supply disruptions such as unfavorable weather variations, labor strikes, or geopolitical events. The producer can invest in new capital goods each period, which are added to the existing productive stock next period. We assume that capital goods require one period for initial installation before they become productive and installation of the newly purchased capital goods is costly. Therefore the total cost of new capital $\Phi(I_t, K_t) = p_K I_t + \phi(I_t, K_t)$ where the latter term of the right hand side is a capital adjustment cost function. Capital depreciates at rate δ_K . There is no secondary market for capital goods: once they are installed, they have no scrap value and thus investment is irreversible. This capital could be considered as industry specific and if there is an unfavorable industry-specific shock, there would be no party willing to purchase it. The irreversibility constraint on investment may lead the investment rate distribution to exhibit the same lumpiness, positive skewness and excess kurtosis as observed in the data.

Total beginning next period capital stock K_{t+1} equals to the undepreciated capital stock from last period plus the newly purchased capital in the previous period such that

$$K_{t+1} = (1 - \delta_K) K_t + I_t. \quad (5.2)$$

The rational commodity producer is risk-neutral, price-taker of the spot price P_t . As of time t , since only $\eta_0^Q, \dots, \eta_t^Q$ have been observed, P_t will be independent of future realizations of the shock. Therefore, when at t the producer decides how much capital to purchase, he takes the current capital stock, K_t , current availability X_t , the current and future expected realizations of the demand shocks $\{Y_s\}_{s=0}^{\infty}$ so as to maximize his present value expected net profit

$$E_t \sum_{k=0}^{\infty} \beta^k \left\{ P_{t+k} AK_{t+k}^{\alpha_Q} \eta_{t+k}^Q - p_K I_{t+k} - \phi(I_{t+k}, K_{t+k}) \right\}, \quad (5.3)$$

subject to

³⁴ It is widely documented that the rate of extraction of a given well is decreasing with the pressure function of the oil level remaining. As a result, it requires an ever-increasing amount of effort to keep production from declining. According to Hamilton (2009), over the decade from 1970 to 1980 the US tripled the number of wells without preventing the oil production from falling. Furthermore, if it is true that the recent emergence of new extraction techniques such as the horizontal drilling allowed for significant productivity gains and reductions in the production costs, it has to be noted that the lifetime of fracking wells is even shorter than the conventional ones so that the only way to keep the oil supply steady is to drill at a growing pace. Put it another way, an increasing amount of resources devoted to production can only offset the supply depletion from old wells. Finally, it is also hard to deny that, as oil will become scarcer, deeper wells located into always more remote areas or even offshore in deep water places will be needed so as to satisfy the raising global demand in the years to come. Together, these results lead us to prefer a production function with diminishing returns to scale.

$$\begin{aligned} K_{t+1} &= (1 - \delta_K) K_t + I_t. \\ I_t &\geq 0. \end{aligned} \quad (5.4)$$

THE STORAGE DEMAND In addition to producers and consumers, the commodity market comprises storers also assumed rational, risk-neutral and price-takers. Through the storage technology, the commodity is transferred from one period to another at a constant marginal cost k . Storers maximize the expected net profit from purchasing S_t of the commodity and selling it next period,

$$\max_{S_t \geq 0} [(1 - \delta_S) \beta E_t P_{t+1} - P_t - k] S_t, \quad (5.5)$$

with δ_S the decay rate of inventories. The total availability of the commodity X_t is determined by the sum of the current supply of the commodity, Q_t , and the inventories inherited from the previous period net of the share lost due to decay, that is

$$X_t = Q_t + (1 - \delta_S) S_{t-1}. \quad (5.6)$$

MARKET CLEARING The market demand for the commodity constitutes the consumption demand $D(P_t)$ and the speculative demand for storage S_t . In each period, the market clears for a spot price P_t when the availability equals total demand according to the equilibrium condition

$$X_t = D(P_t) + S_t, \quad (5.7)$$

with the linear demand function $D(P_t)$, assumed downward-sloping in P_t and subject to a multiplicative stochastic disturbance Y_t described by an autoregressive process.³⁵ Hence, the linear demand function takes the following form:

$$D(P_t) = \bar{D} \left(1 + \frac{\alpha_D}{\bar{P}} (P_t - \bar{P}) \right) Y_t, \quad (5.8)$$

where \bar{D} and \bar{P} represent the steady-state values of final demand and the spot price respectively and α_D is the elasticity of demand.

5.5.2 THE COMPETITIVE EQUILIBRIUM

Definition 1. A rational competitive equilibrium is given by the path of capital investment $\{I_t\}_{s=0}^{\infty}$, storage $\{S_t\}_{s=0}^{\infty}$ and prices $\{P_t\}_{s=0}^{\infty}$ such that: (i) the representative producer maximizes the present value of his expected net profits subject to the sequence of capital accumulation constraints in (5.4); (ii) storers maximize the present value of their net profits subject to the nonnegativity constraint on storage; and (iii) the market clears in every period.

³⁵ The demand shock is an AR(1) process: $Y_t = \rho Y_{t-1} + \eta_t^D$. The demand uncertainty is modeled as a persistent stochastic process akin to the cyclical fluctuations of the international business cycle.

Before deriving the model's first order conditions another assumption will be made regarding the convex adjustment costs Φ . Even though the observed investment rate exhibits a slightly positive serial correlation which might call for some kind of convex adjustment costs, we believe they matter less than the irreversibility constraint on I and so can be overlooked without changing neither the internal relationships among the variables nor the qualitative nature of the dynamics implied by the model.³⁶ Hence, for the sake of simplification, $\phi(I_t, K_t)$ in equation (5.3) is set to zero in the rest of the chapter. Taking the price of capital p_K as a constant and fixed at 1, it turns out that the producer's maximization problem given by the equations (5.3) and (5.4) delivers the following Euler equation:

$$\beta E_t \left\{ P_{t+1} \alpha_Q \left(A K_{t+1}^{\alpha_Q - 1} \eta_{t+1}^Q \right) + (1 - \delta_K) \right\} \leq 1, \quad = 1 \text{ if } I_t > 0. \quad (5.9)$$

The investment decision rests on the present value of the expected marginal return on capital, the left hand side of equation (5.9) being equal to its marginal cost. Should the right hand exceed the left, there is a large enough opportunity cost of investing today which makes the investment in the current period non-viable.

Likewise, regarding the speculative demand for storage, differentiating (5.5) with respect to $S_t \geq 0$ yields the following storer's optimality condition:

$$\beta (1 - \delta_S) E_t P_{t+1} - P_t - k \leq 0, \quad = 0 \text{ if } S_t > 0. \quad (5.10)$$

The storage decision hinges on whether the commodity price (net of the carrying costs) grows at the rate of interest. It is profitable to store only if the price growth rate equals the interest rate. Therefore, a market in contango is one in which the expected price would rise at the decay adjusted interest rate. Finally, as a result of the rational expectations assumption, both the investment and storage are forward-looking decisions resting on the expectations agents form regarding the sole next-period price F_1 without any consideration for F_2 and the subsequent forward prices.

5.5.3 NUMERICAL SOLUTION

The nonlinear nature of the decisions rules warrants the use of global numerical solution methods. We choose to employ a projection method to approximate the solution of our model. There are two endogenous state variables K_t, X_t , and one stochastic state variable Y_t . The decision variables are S_t and I_t , while P_t falls from the market clearing condition. P is regarded as an additional control variable and so are the futures prices. To solve the model, the state space is discretized and the bounds are defined around the steady state values of the state variables. It thus consists in $[\underline{X}, \bar{X}] \times [\underline{K}, \bar{K}] \times [\underline{Y}, \bar{Y}]$. The solution to the time iteration problem delivers three time-invariant policy functions $P = \mathcal{P}(X, K, Y)$, $I = \mathcal{I}(X, K, Y)$, $S = \mathcal{S}(X, K, Y)$. These policy functions solve the constrained system of equations (5.7) and (5.9)-(5.10), using the transition

³⁶ The presence of convex adjustment costs will result in a zero-lower bound less often binding thereby leading to a smoother, more persistent and symmetric distribution rate of investment.

equations in (5.4) and (5.6) to bring the model forward.³⁷ The model solution yields nonlinear decision rules that are governed by endogenous thresholds, which in turn depend on the state variables. In order to assess the extent to which storage interacts with the irreversibility constraint on investment, we proceed by studying two models, identically calibrated and which differ only by whether there is the possibility for storage.

5.6 SIMULATION RESULTS

In this section, we will discuss simulation results of two models: a baseline irreversible investment model and the same basic set-up but augmented with storage capacity. The former is no different from the model set out in the previous section except that we remove the possibility of stockpiling.

5.6.1 CALIBRATION

In calibrating the models, if the choices have been largely guided by the above empirical analysis, a particular attention has been also paid to their internal consistency as it is a connection between two strands of literature mostly developed independently of one another. The calibrated parameter values are reported in table 5.4 and are selected so as to follow the standard calibration and, when available, estimation results found in the investment and storage literature. The share of capital α^K is set to 0.33 which is equivalent to a long-run supply elasticity of $\alpha^K / (1 - \alpha^K) \approx 0.5$. Since no distinction is drawn between short and long-run demand elasticities, α^D is set to -0.1 , a value in the range of estimates provided in Dahl (1993) and Cooper (2003) and also reflecting the lack of substitutes for such a basic product. It has to be said that these low values of supply and demand responsiveness have been further suggested by the substantial gap in volatility between the prices and quantities noted in Table 5.1. The depreciation rate of capital δ_K is set to 10% which is intermediate in the typical range of 8 and 12% used in the related literature (Kogan et al., 2009, Kung and Schmid, 2015). Likewise, the decay rate on storage δ_S is fixed at 5% to be consistent with the 3% used in Routledge et al. (2000). We decided to also account for a physical storage cost, $k = 5\%$, unlike most of the empirical studies of the storage model, which specify either a proportional cost as in Deaton and Laroque (1996) or a constant marginal storage cost following Cafiero et al. (2011b). The relatively low selected value—e.g., 1% of the long-run average price—reflects this modeling choice, as we want to avoid precluding storage with too high a total cost of carry. Regarding the demand shock Y , its role in the model's internal mechanics is very close in nature to the one played by the income shock variable embedded in the storage framework developed in Dvir and Rogoff (2009, 2014). Hence, for the persistence value of the demand shock ρ , we borrow the value they used which is equal to 0.5. Lastly, the volatilities of supply and demand shocks are chosen so as to match the observed coefficient of variation of production (table 5.1).³⁸ Before running

³⁷ The model is solved by implementing policy function iteration using cubic spline function approximation through "Rational Expectations Complementarity Solver" (RECS) developed by Gouel (2013b) and available from the following website <http://www.recs-solver.org/>.

³⁸ As the consumption simply equals the difference between the production and the stock variation, its descriptive statistics have not been documented in table 5.1. Still, the coefficient of variation of the normalized demand, equals to 0.0632, is really similar to the production's one and thus to the selected value of 0.05.

Table 5.4. Model Parameters

Parameter	Description	Value
α^K	Capital share	0.33
δ_K	Capital depreciation rate	0.1
p_k	Purchase price of capital	1
α^D	Demand elasticity	-0.1
k	Physical storage cost	0.05
δ_S	Storage decay rate	0.05
β	Discount factor	0.95
A	Scale parameter	β^{-1}
\bar{D}	Long-run average demand	1
\bar{P}	Long-run average price	5.07
ρ	Persistence of demand shocks	0.5
σ_{η^D}	Standard deviation of supply shocks	0.05
σ_{η^Q}	Standard deviation of demand shocks	0.05

Notes: The table describes all the annualized parameter values characterizing the model and used in the simulations.

simulations, it is yet interesting to highlight the key theoretical implications which can be drawn from the set of restrictions introduced in the modeling.

5.6.2 THEORETICAL INSIGHTS

STATES VARIABLES AND REGIMES THRESHOLDS: The nonnegativity constraints give way to nonlinear decision rules for storage and investment, which are governed by trigger levels for availability and capital, respectively. These thresholds, are functions of the other state variables and can be written as $X_t^* = X^*(K_t, Y_t)$ and $K_t^* = K^*(X_t, Y_t)$. K_t^* represents the capital stock above which it is optimal to delay investment and let the capital stock depreciate. For different levels of X_t , it is determined from the optimality condition (5.9) of the producer's problem when investment is null and the equality holds. When capital is abundant (e.g., above K_t^*) the marginal product of capital is too low to make investment profitable. At the same time X_t^* is the availability level under which the spot price is too high compared to the expected price to justify holding any positive inventories. When the availability of the commodity in the market is large, the target level of capital is lower. This is mainly driven by the lower prices resulting from the large amount of commodity in the market. Similarly, a large capital stock entails that the price at which storage becomes profitable is lower leading in a higher availability threshold than when the capital stock is smaller. Given the properties of the expected price and spot price functions, the relationships between K_t^* with X_t and Y_t as well as between X_t^* with K_t and Y_t are summarized in the two observations below.

Observation 1. X_t^* is a nondecreasing function of K_t .

Observation 2. The desired level of capital K_t^* is

1. strictly decreasing in X_t and strictly increasing in Y_t when $S_t > 0$;

2. increasing with Y_t and invariant to X_t when $S_t = 0$.

First, looking at the impact of capital on the availability threshold X^* under which stocks are empty, observation 1 simply shows that a greater capital level is associated with a higher expected supply weighing on any increase of the expected price.

Then, switching to the effects of availability on the target capital level K^* , two distinct regimes must be explored. With this in mind, the first statement in observation 2 corresponds to the case when inventory building is profitable, that is $S_t > 0$. The interpretation is straightforward recalling from the arbitrage equation (5.10) that $E_t P_{t+1} = \beta (1 - \delta_S)^{-1} (\mathcal{P}(X_t, K_t, Y_t) + k)$, which implies that variations in spot and expected prices are coupled. Hence, since the expected price is a decreasing function of the availability in the market, when the commodity is abundant and storage is positive the expected price is low. This in turn reduces the net marginal benefit from investment and in the end lowers the desired level of capital. The result points to the first source of divergence between the two models with and without storage. Put simply, storage increases the value of postponing investment by lowering the cut off value above which it is optimal to delay capital expenditures. In addition, and perhaps even more importantly, by inducing conditional heteroskedasticity in prices the storage mechanism implies a higher uncertainty around the expected price which both supports speculation and heightens the option value of deferring investment. Through these two channels, the presence of storage has a crowding out effect on investment. The outcome is a gradual shrinkage of the productive capacity accompanied by withdrawals of inventories eventually making the occurrence of a stockout more and more likely.

Finally, once the supply falls short of the demand, stocks are sold out—e.g., $S_t = 0$ —and from (5.10) $E_t P_{t+1} = E_t [D^{-1}(Q_{t+1}, Y_{t+1})]$. In other words, the expected price is no longer a function of the spot price. The stockout regime reverts to the model of irreversible investment without inventory building capacity, in which the desired capital level is a function of the realized supply-side shock, the steady state values of the price and consumption demand of the commodity. The realized shock Y_t raises the trigger value of capital. To borrow the terminology from the option pricing literature, the value of waiting to invest is lower when the realized value of the disturbance is high. Indeed, given the assumed persistence of shocks to the consumption demand for the commodity, the whole conditional distribution $F(Y_{t+1}|Y_t)$ shifts to the right giving greater probability to larger Y_{t+1} values, thereby rendering the opportunity to invest and to terminate the option more attractive than waiting. Then again, this investment incentive is further strengthened by what can be called the “uncertainty effect”. The reason is that, if the high spot price deters inventory speculation, it also provides a much kinder environment for investing since the expected price, now decoupled from the very volatile spot price, is more stable and even smoothed out according to the Samuelson effect. The volatility of the expected price is now constant since the expected price itself is a function the capital stock and the expected demand shock.³⁹

All in all, the combination of persistent demand shocks and time-variations in both the desired level of capital and uncertainty of future price are the key reasons behind the certain substitutability, albeit imperfect, between storage and investment.

³⁹ The constant volatility of the expected price in a stockout regime is discussed in Deaton and Laroque (1992, 1996).

Together, both zero-lower bounds on storage and investment split the state space into four regions demarcated by the capital and availability thresholds determined by the current supply and demand conditions. They are described in the following observation:

Observation 3. The competitive equilibrium can be characterized by four regimes:

1. $I_t = 0, S_t = 0$, if $K_t \geq K_t^*$ and $X_t \leq X_t^*$;
2. $I_t = 0, S_t > 0$, if $K_t \geq K_t^*$ and $X_t > X_t^*$;
3. $I_t > 0, S_t = 0$, if $K_t < K_t^*$ and $X_t \leq X_t^*$;
4. $I_t > 0, S_t > 0$, if $K_t < K_t^*$ and $X_t > X_t^*$.

If both $I = 0$ and $S = 0$, the expected price is only a function of expected production, which is constant AK_t^α . This is a regime where the economy has overcapacities of production and it is optimal to defer investment. Furthermore, in spite of a relatively low spot price, it is not profitable to store neither because of the large productive capacity. Indeed, as stated in observation 1 the very high capital level weighs on the expected price, preventing the latter from rising sufficiently so as to cover the purchasing and carrying cost of inventories.

If only $I = 0$, there is still an excess of capital but not enough to preclude expected price from increasing so that it becomes profitable to stockpile (e.g., $S > 0$). So long as the expected commodity price grows at a higher rate than the rate of interest (net of decay), it is profitable to store.

If now $S = 0$ but $I > 0$, the market is tight resulting in a high spot price. Futures market is backwardated and selling inventories today is optimal. Although the availability is too scarce to allow storage, the associated environment of high prices encourages investment to reach the optimal level of capital K^* .

Finally, as mentioned previously the investment-storage substitutability is only partial and it might be the case that it is optimal to invest and store jointly so that $I > 0, S > 0$. It has to be noted that, in this regime, both the S and I values are much lower than those reached when one of the constraint is binding. The market equilibrium can enter this regime for instance if, despite a capital level lying below the desired K^* , a high positive value of the supply shock η^Q yields an availability in excess of the threshold X^* . The latter scenario is even more likely if supplemented by a persistent low demand state Y which will lower X^* while raising K^* . The outcome is a relatively slack market in which inventories are used to absorb excess supply. Yet, and contrary to the first regime when $I = 0$ and $S = 0$, here the stock of capital is not large and so (i) is not pressing down the expected price increase needed to cover the carrying cost of inventories, (ii) it is still optimal to invest and bring the capital stock to the target K^* . Moreover, the quantities S at stake being lower than they are when investment is stuck at its zero-lower bound, they have too limited an impact on the expected price volatility to make very attractive the option value of waiting.

Let us move now to the characterization of the policy functions prevailing in the various market regimes.

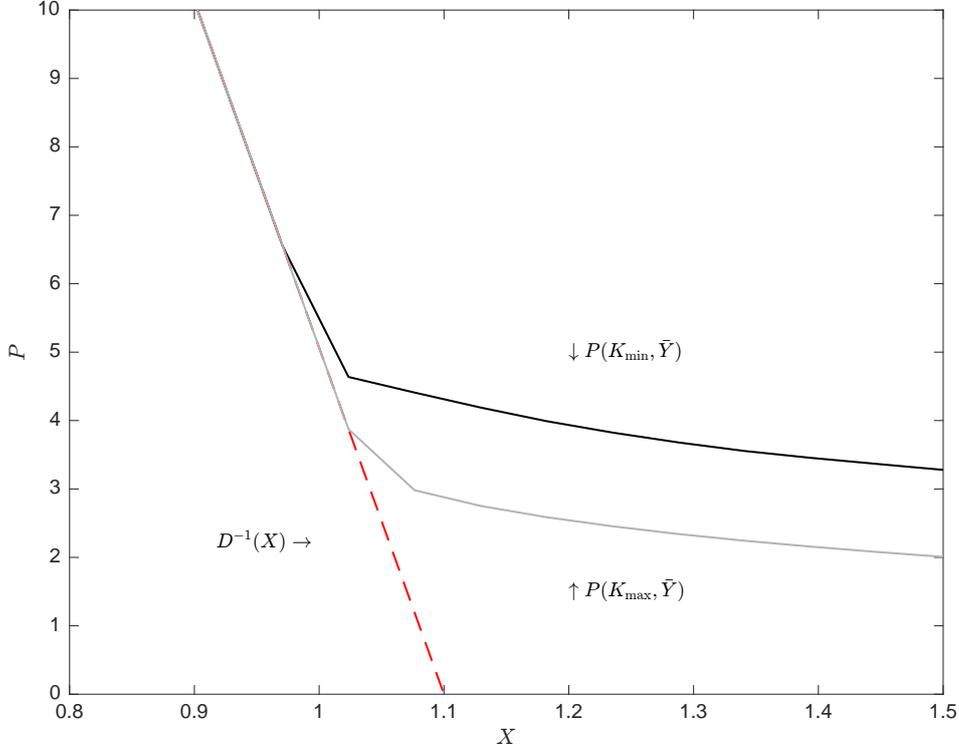


Figure 5.3. Price Function

Notes: Two price functions, obtained for the highest and the lowest capital levels, are plotted against different levels of availability X . Additionally, the inverse demand function that prevails when inventories are null is plotted in the dashed line.

POLICY FUNCTIONS' BEHAVIORS X^* threshold point implies that the price function is nonlinear and follows a two regime equilibrium which, from equation (5.10), can be written as:

$$P_t = \mathcal{P}(X_t, K_t, Y_t) = \begin{cases} \beta(1 - \delta_S) E_t \{P_{t+1}\} - k & \text{if } X_t > X_t^* \\ D^{-1}(X_t) & \text{otherwise.} \end{cases} \quad (5.11)$$

The rule can be summarized in the following functional form:

$$\mathcal{P}(X_t, K_t, Y_t) = \max [\beta(1 - \delta_S) E_t P_{t+1} - k, D^{-1}(X_t)]. \quad (5.12)$$

Figure 5.3 depicts the two regimes of the price policy function with respect to the availability and for two extreme values of K . The abscissa of the kink is X^* below which inventories are zero. As a result, the spot price is only function of the consumption demand assumed linear. In line with observation 1, a high level of capital is associated with a right shift of X^* . Where there is a large productive capacity, the spot price is lower for all levels of availability and storage becomes optimal at a higher availability level. Characterizing $\mathcal{P}(X_t, K_t, Y_t)$ in terms of the quadrants shaped by X_t^* and K_t^* gives:

Observation 4. The equilibrium price function $\mathcal{P}(X_t, K_t, Y_t)$ relates to different levels of capital and availability in the following manner :

1. $\mathcal{P}(X_t, K_t, Y_t)$ is strictly decreasing in X_t ;
2. $\mathcal{P}(X_t, K_t, Y_t)$ is nonincreasing in K_t .

The first part of the observation is obvious and does not deserve additional comments. Regarding the second point, the associated explanation is actually rather intuitive. Knowing that when inventories are carried over, the price function is linked to the behavior of the expected price along the capital stock dimension. Since the equilibrium of the model is described in terms of a desired level of capital K^* , the expected price is also a function of this threshold. Specifically, when the capital stock lies below K^* , investment is positive and brings back the next period capital stock to its optimal level. In this regime, the expected price is disconnected from the level of capital and so is the current spot price.

On the other hand, when the capital stock is above K^* , there is no investment and the next period capital stock equals the current capital stock less depreciation. Since a high level of capital entails a high expected supply, it turns out that the expected price and the spot price are decreasing in the capital stock whenever its current value exceeds K^* . Consequently, whether K is below or above K^* , the spot price is either independent or a decreasing function of the capital stock.

The same characterization can be derived for the other two investment and storage policy functions.

Observation 5. The equilibrium investment and storage functions, $I_t = \mathcal{I}(X_t, K_t, Y_t)$ and $S_t = \mathcal{S}(X_t, K_t, Y_t)$, relate to availability, capital and demand shock in the following manner :

1. $\mathcal{I}(X_t, K_t, Y_t)$ is nonincreasing in X_t and K_t and increasing in Y_t ;
2. $\mathcal{S}(X_t, K_t, Y_t)$ is nondecreasing in X_t , nonincreasing in K_t , and decreasing in Y_t .

The observation is further illustrated in Figure 5.4 exhibiting the investment and storage functions as they relate to the state variables, X , K , and Y . The substitutability between investment and storage as well as the nonlinearities embedded in this model are well represented by these functions and the different kinks at the thresholds, X^* and K^* , can be identified.

As can be seen on the left panel, when $X < X^*$, I is constant with respect to availability and decreasing with K . The reason is that the investment decision is driven by the expected price. Below X^* , the relationship between the expected and spot price is severed. In a stockout market, the expected price only depends on the next period stock of capital along with the expected state of the demand governed by the autocorrelated shock Y . Investment follows suit: for a given fixed capital stock lying below K^* , optimal investment is constant and equals the gap between K and its target K^* so as to restore the optimality. Therefore, the higher K the lower I . In sum, whether K exceeds its target, I is either null or decreasing in K .

On the other hand, when the commodity is abundant in the market so that X lies above X^* , I is decreasing in X . In this regime, as the storage arbitrage condition holds, the expected price is indeed a function of the spot price which is decreasing with the availability. Moreover, given that each period the market availability

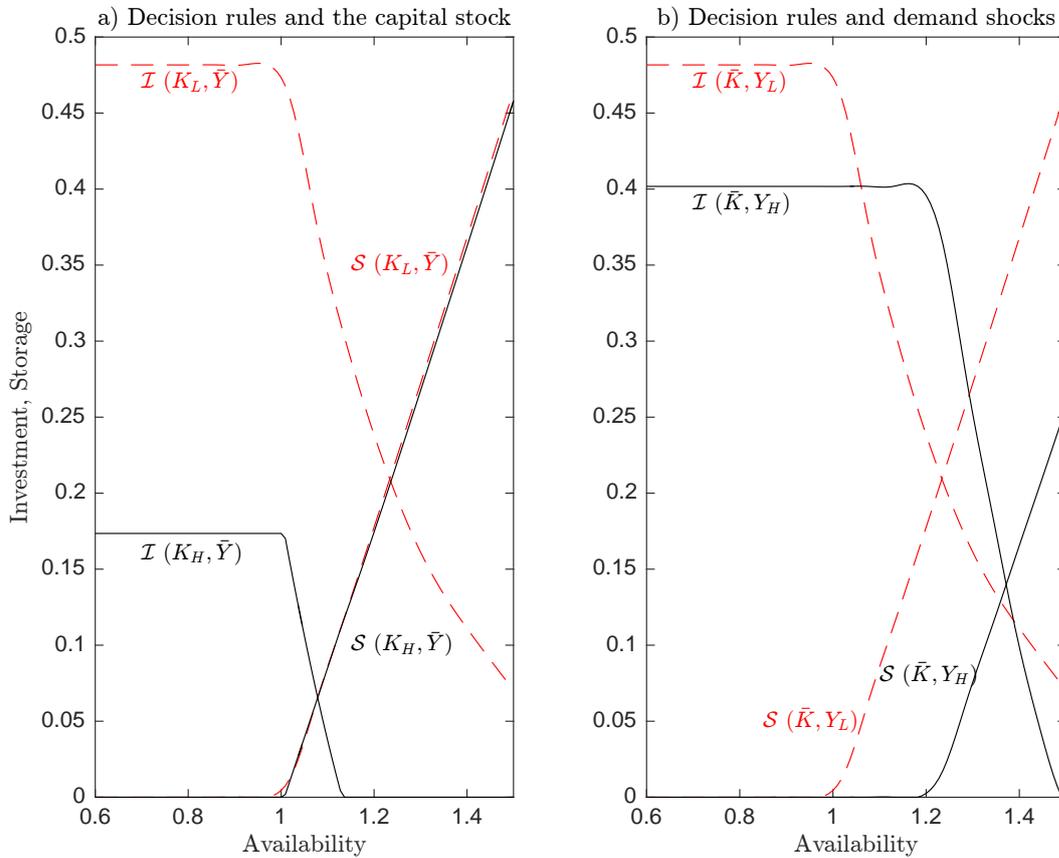


Figure 5.4. Investment and Storage Functions

Notes: The investment and storage functions for the highest and lowest value of capital and demand shock are plotted against different levels of volatility. Panel a) represents the two nonlinear functions in terms of the two extreme values of capital. Panel b) represents the functions for the two extreme realizations of the demand shock.

equals the sum of past inventories with the realized production, an increase in the productive capacity is sluggish whenever stockpiling is optimal. It must be added that the rise in the option value of waiting stems from the higher uncertainty inherent in the transmission of spot price volatility to the expected price. It turns out that the bigger the quantity in store, the greater the crowding-out effect on investment which, consequently, is a nonincreasing function of availability for any given level of capital.

For its part, storage is nondecreasing in X and Y . Storage is profitable only when the commodity is sufficiently abundant in the market so as to depress the spot price. Investment and storage are negatively correlated, with inventories standing high when the market is flooded. Since excess supply is persistent, as the constant gradual shrinkage of the capital stock is slow, storage becomes more important as an adjustment channel while the productive capacity adjusts. Therefore, storage does not vary much with the capital stock.

As already mentioned and illustrated in the panel b) of figure 5.4, investment and, interestingly storage too, are really reactive to demand shocks. Investment response is of the same order of magnitude. All that

means is that the persistent demand shock entails shifts in the whole demand curve affecting the expected price level and, in turn, the equilibrium investment and storage schedules. As a result, a higher demand pushes upward the expected price and so both the X^* and K^* thresholds.

Finally, the risk-neutrality assumption and constant interest rate allow us to equate the future price to the expected price at n maturity, such that,

$$F_{t,t+n}(X_t, K_t, Y_t) = E_t P_{t+n}. \quad (5.13)$$

Figure 5.5 displays the futures curve for 12 maturities along several dimensions with the zero-maturity price as spot price. The top panels represent the futures curves when the realized demand shock is the highest

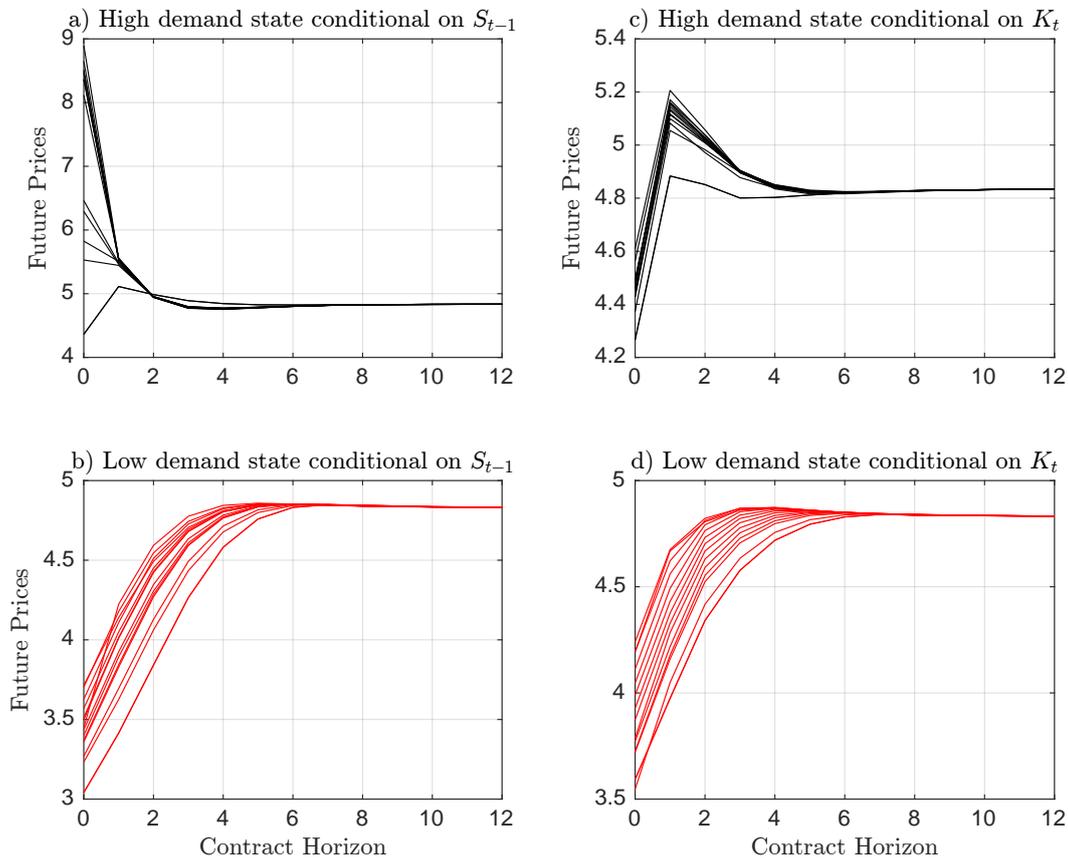


Figure 5.5. Futures Curves

Notes: The futures prices are plotted for each of the 12 contract maturity, with the zero maturity contract as the spot price. Panels a) and b) represent the futures curves for different levels of past inventory at the average capital level, when the demand shock is at its highest and lowest, respectively. Similarly, panels c) and d) show the futures curves for different levels of capital at the average income storage level, when the demand shock is at its highest and lowest, respectively.

while the bottom panels stand for the futures curves when the demand shock is at its lowest. Specifically, the futures price in panels a) and b) are displayed for different levels of incoming inventories keeping the

capital stock at its average level. Panels c) and d) plot futures curves for different capital levels for the mean previous inventory level.

In all states of the world, futures prices converge to a state-invariant long-term equilibrium price, namely the unconditional mean of the spot price. The reversion to the unconditional mean is established in Routledge et al. (2000) and rests on the fact that storage has no impact on the long term price recalling that, in steady state, inventories are zero. Incoming inventories dampen the effect of the positive demand shock on prices, the lowest spot price curve is thus associated with a high level of inherited inventories. Nevertheless futures curves are in backwardation when the demand shock is favorable. The degree of backwardation is highest when the quantities in store are the lowest if not zero.

Most futures curves are monotonous except when inventories are very high. In this case, the front-month price is above the spot price and the subsequent future prices decline. This goes to show that when there is an abundance of the commodity in the market, a favorable demand shock is not enough to alleviate the supply glut. Inventories affect the front-end of the forward curve in line with observations in Kogan et al. (2009). A favorable demand shock, often accompanied by either low or zero outgoing inventories, raises both the spot price and the subsequent forward prices. Given that Y is persistent, the distribution of the shocks shifts rightward and therefore the expected value of Y would be higher. There is a clear ordering of prices along the demand realizations regardless of the other state variables X_t and K_t . On the other hand, a negative demand shock results in an upward sloping futures curve for all possible values of incoming inventories, the lowest futures curve is associated with the highest level of past inventories or equivalently the highest level of availability. The term structure along the capital stock dimension is hump-shaped for the high values of Y . Since the inherited inventories are the same, the difference in the spot price comes from difference in the production capacity at the time the shock hits. In the presence of positive storage, a very favorable demand shock is more often than not associated with stockouts. Therefore next period price rises above the spot price today which is still kept low since there are positive incoming inventories.

All the above observations on the resulting decision rules for I and S and the price function have provided a general picture into the inner workings of an irreversible investment model with storage capacity. To go further in the empirical analysis, we simulate 1,000 sequences of length 500 and discarding the first hundred and fifty of futures prices up to twelve maturities as going beyond does not prove really insightful in light of the very strong similarities between the futures prices series whether simulated or even observed.⁴⁰ As in Kogan et al. (2009) the simulated investment variable has been divided by the stock of capital so as to be directly comparable to the observed investment rate variable I . The slope of the forward curve is defined as

$$SL_t = \log \left(\frac{F_{t,12}}{F_{t,1}} \right). \quad (5.14)$$

As of time t , the forward curve is classified as being in contango (backwardation) when the demeaned slope $\tilde{S}L = SL_t - \bar{S}L$ is positive (negative).

⁴⁰ It has already been shown in the previous section that futures prices tend to converge to a long-run future price. We can thus consider the 12-month contract to be F_∞ as in Routledge et al. (2000).

5.6.3 DISCUSSION

Our starting point is the irreversible investment model with no inventory building capacity. The model solved at first is the standard neoclassical growth model with a nonnegativity constraint on investment in the face of an exogenous consumption demand subjects to a persistent shock. The model equations remain the same with the exception of the first-order condition on storage equation (5.10). In this model, the demand for the commodity is only for consumption purposes and there is no capacity to absorb excess supply through storage. The only room for maneuver to counter supply or demand shocks is through changes in the production capacity. In this model, spot price dynamics are far from the ones which describe commodity prices. The irreversible investment model with no storage delivers a weakly persistent price with a negatively skewed distribution. These results are displayed in Table 5.5.

Table 5.5. Storage Effects on Price and Investment Dynamics

Moments	No Storage		Storage		Observed Data	
	Price	Investment	Price	Investment	p^{obs}	I^{obs}
First-Order Autocorrelation	0.10	-0.18	0.26	-0.03	0.94	0.18
Second-Order Autocorrelation	0.01	-0.14	0.07	-0.16	0.87	0.03
Coefficient of Variation	0.53	0.06	0.31	0.08	0.31	0.05
Skewness	-0.16	0.68	2.04	1.34	0.59	0.13
Excess Kurtosis	0.04	0.15	5.11	2.02	0.64	8.91
Inaction Rate		0.05		0.15		0.11
Positive Spike Rate		0.10		0.15		0.15
Frequency of Backwardation	0.67		0.57		0.49	

Notes: The table shows moments of simulated price and investment time series from a model with no storage and a model with storage.

A model with investment as the sole variable of adjustment to demand and supply fluctuations does not generate the correct price stylized facts. When it comes to modeling commodity prices, it is thus important to allow for inventory building. Fluctuations in commodity prices are mainly driven by this second type of investment; fixed capital investment is not enough. Moreover, investment dynamics are also impacted by the presence of this second channel for transferring the commodity supply intertemporally. Interestingly, fixed capital investment in the presence of storage is more volatile and lumpy. The rate of inaction is higher when storage is possible. This can be explained by the presence of two substitutable ways to meet economic fluctuations.

Storage is used to mitigate the effects of a supply glut on the commodity price and therefore prevents the latter from dropping too quickly. At the same time, while storage is profitable, the production capacity or the targeted level of capital is decreasing in storage. In section 5.6.2, we showed that the storage arbitrage condition creates a tight link between the spot and expected price. An implication of this condition is that storage, which occurs at lower spot prices, ties the next-period price to this low level of price. As a result of the storage arbitrage, the expected price is pinned down to a lower price regime, leading to a lower desired capital stock and ultimately a lower investment rate. Additionally, the speculation through storage renders

the expected price more volatile. Because we are in a world where the decision to invest is impacted by both uncertainty and sunk costs, the presence of storage increases the value of postponing investment and of waiting to receive more information before committing to an investment project of this sort. Thus, in response to the higher uncertainty surrounding the expected price whenever inventories are carried over, producers tend to wait, thereby making investment even more intermittent and pronounced. With storage, the targeted level of capital is lower than without storage. Therefore, upon stockout, the desired stock of capital is at its highest and investment spikes up. In other words, we invest less often but more aggressively. It turns that both the rate of inaction and the positive spike rate are higher when the possibility to store the commodity does exist. Since investment is irreversible, it is more optimal to wait for more information, defer investment, and instead use storage to smooth fluctuations in the commodity market. In this set up, there is an under-investment which is followed by a sharp increase when inventories are run down completely. When outgoing inventories are either running low or empty, the spot price is higher and decoupled from the expected price, and it is no longer optimal to delay investment. Since backwardation (or stockouts) is persistent in the oil market, it is optimal to take advantage of the incidence of both current and future higher prices by investing and selling the commodity.

Figure 5.6 depicts the relationship between the slope of the forward curve, $\tilde{S}L$, and storage. On average, storage is null only when the market is strongly backwardated (i.e. the slope is steeply negative).⁴¹ It also reveals that a highly positive slopes is associated with elevated inventory levels in the commodity market; the storage decision is closely linked to the slope of the term structure. By the same token, the investment rate is also governed by how futures market set prices. From Figure 5.6, the investment rate decreases with $\tilde{S}L$, regardless of the model specification (i.e. whether the model allows for storage capacity). The difference between the two models is the average investment rate conditional on the slope of the forward curve. When the commodity market is weakly backwardated, namely when outgoing inventories are low, the investment rate is lower in a model with stockpiling capacity than in the model without. Since in the latter case fixed capital investment is the only adjustment variable, it is optimal to invest a lot more so that the desired level of capital would be higher than if there were still inventories in store, despite being low. Stocks, though have an asymmetric effect on price, can still mitigate sudden price increases as long as they are positive. The resulting investment rate will be lower in this model precisely because as long as storage remains positive, the storage arbitrage condition ties the expected to the spot price. Given this lockstep variation in prices, outgoing inventories would maintain a lower expected price than otherwise in a model without stockpiling capacity. Given that the investment decision hinges on the expected price, a lower expected price implies a lower investment rate. This is captured in Figure 5.6 when the range of $\tilde{S}L$ is negatively but lower than -0.1 .

The investment rate in periods of stockouts or strong backwardation is however greater in a model with storage capacity. This speaks to the underinvestment or stymied production capacity when the excess supply can be stored. The departure of the no storage model from the storage one is due to the lack of excess capacity. With no capacity to use inventories as a smoothing mechanism, the reversal of the slope of the forward curve

⁴¹ Litzenberger and Rabinowitz (1995) distinguish two types of backwardation: strong backwardation as the case where $F_{t+n} < P_t$ and weak backwardation when $F_{t+n} < (1 + \bar{r})^n P_t$

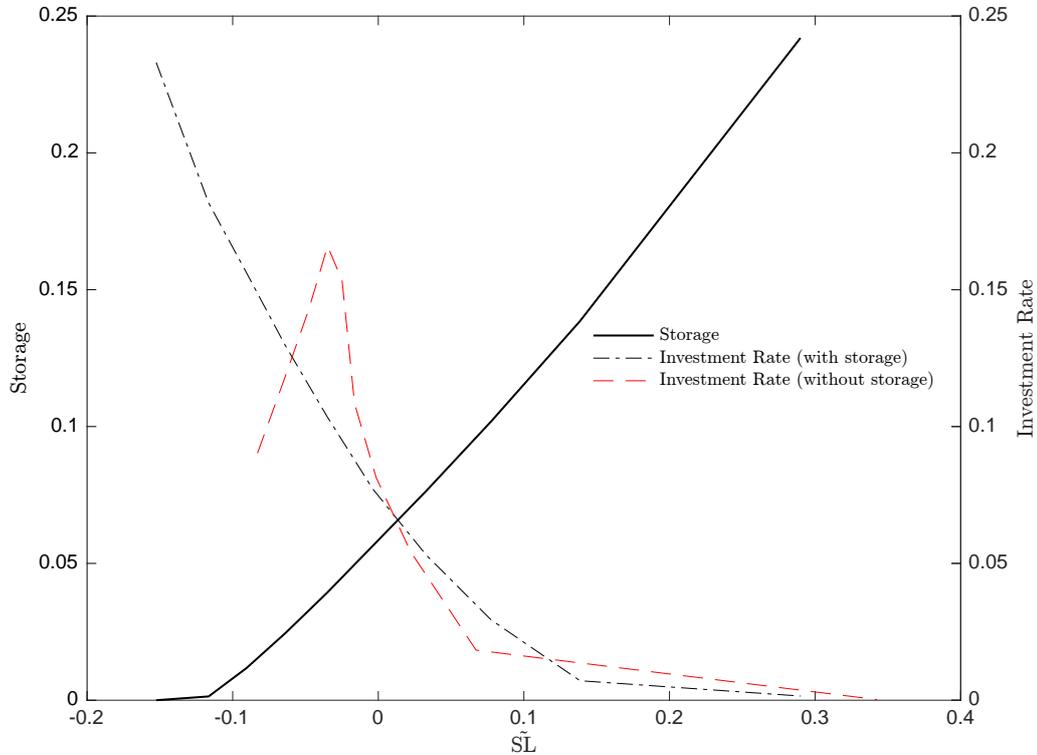


Figure 5.6. Storage, investment rate and the term structure of futures prices

Notes: The average inventory holdings are calculated for each value of the slope to derive a storage as a function of the shape of the term structure.

implies an ensuing supply shortage. In a strongly backwardated market (i.e. stockout), the storage arbitrage no longer holds, which means that the spot price and the expected price are no longer connected to each other. The difference between the investment rate emanating from the two models, in this case, is related (i) to the difference in the existing capital stock at the time of stockout and (ii) to the level of uncertainty in a strongly backwardated market. The first case has already been addressed. It is due to the lower desired capital stocks when storage can act as a substitute to investments and ends up crowding out investment. The latter point will be tackled at length in the upcoming discussion. What we can already conclude at this juncture is that, in a strongly backwardated market, uncertainty in a model with storage capacity is lower than in a model without it. Finally, when the market is in contango, the difference between the two investment rates is not as stark.

Going one step further in comparing the model with storage capacity and the model without, we look to the distribution of the slope that each model delivers. We can already see in Figure 5.6, that the range of $\tilde{S}L$ is different between the two models. While the model with storage capacity delivers a more steeply negatively sloped forward curve than a the model without storage, the latter give a more positively sloped forward curve. Looking at the distribution of $\tilde{S}L$ emerging from the two models, we note that indeed whether we allow for storage capacity produces two very distinct distributions juxtaposed in Figure 5.7.

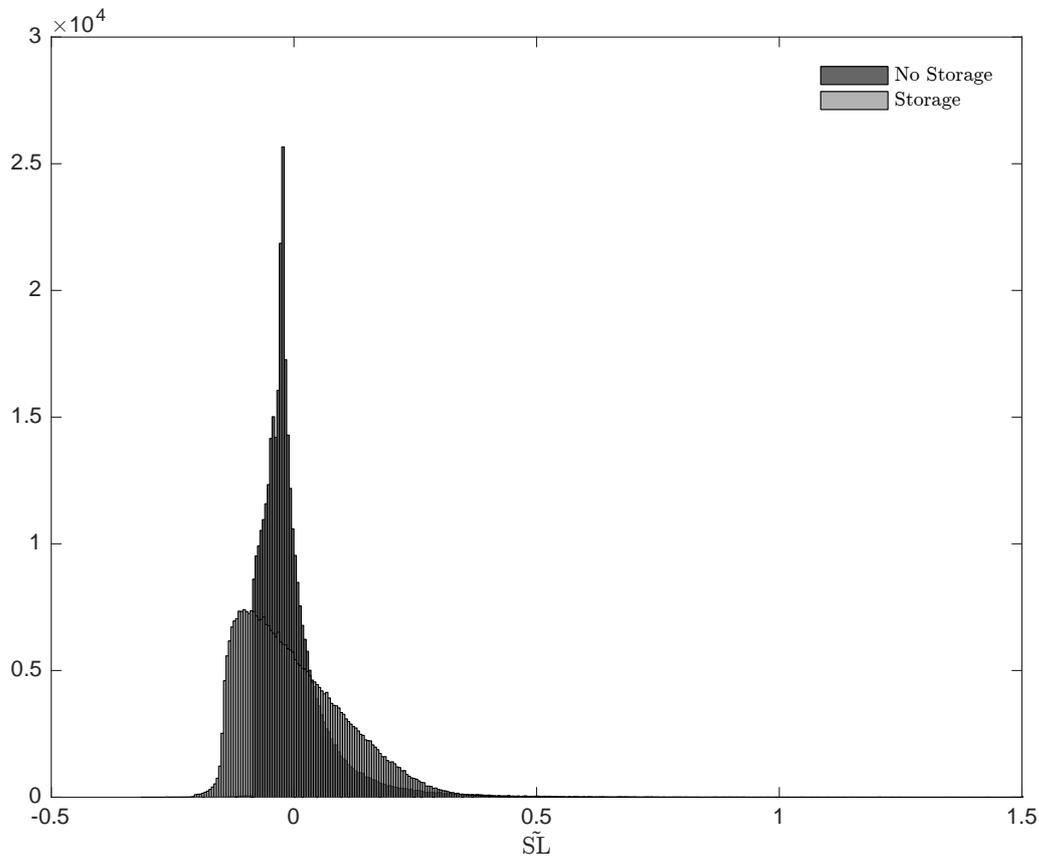


Figure 5.7. Distribution of the term structure of futures prices

Notes: The model with no storage capacity and the model with storage capacity are simulated using parameter values in Table 5.4. Panel a) represents the simulated slope for the model with no storage capacity. Panel b) represents the simulated slope for the model with storage capacity.

In a backwardated market, when stockpiling is not feasible, and thus inventories are not available to absorb excess supply, the slope of the forward curve is much steeper than the case with stocks. As storage mitigates the decrease in the spot price, both the spot and expected prices remain in a lockstep variation mediated by the storage arbitrage condition. Therefore, in a contango market, the forward curve does not slope upward as sharply as the forward curve in a market deprived of storage capacity.

Regarding the backwardation state, although it is more frequent when there is no capacity for storage due to the absence of incoming inventories to cushion the effects of a positive demand shock on the spot price, it is not as pronounced as when storage is possible. Since stockpiling depresses the production capacity in the short-run, it might be the case that upon a very positive demand shock, quantities in store are not enough to mitigate this effect. Newly invested capital comes online with a lag which means that the production capacity cannot be instantaneously adjusted to meet the boost in demand for consumption. In such a state, the spot price would rise a lot more than in a regime with only fixed capital investment particularly because

storage delays investment. The effect of storage can thus be captured in a higher degree of backwardation due precisely to the crowding-out effect of storage on investment and the resulting lower production capacity.

As mentioned earlier, the degree of uncertainty is intimately linked to this crowding-out effect. The storage arbitrage condition, locks both the expected to the spot price thereby transferring the volatility of the spot price into the future. This very condition results in an increased uncertainty around the expected price. When uncertainty about the expected price rises, the probability of hitting the lower bound on investment, or in other words having too much capital, increases as well. As a result, the producer prefers to invest less or nothing as to avoid being constrained in the future.

While the presence of storage has a strong smoothing effect on the spot price of the commodity, it is destabilizing for both investment and the expected price. Figure 5.8 illustrates the conditional volatilities of investment, the spot price and the expected price for both models on the slope of the forward curve. Introducing storage to an irreversible investment model almost halves the standard deviation of the spot price (see Table 5.5). The standard deviation of the price is decreasing in the slope of the forward curve when we

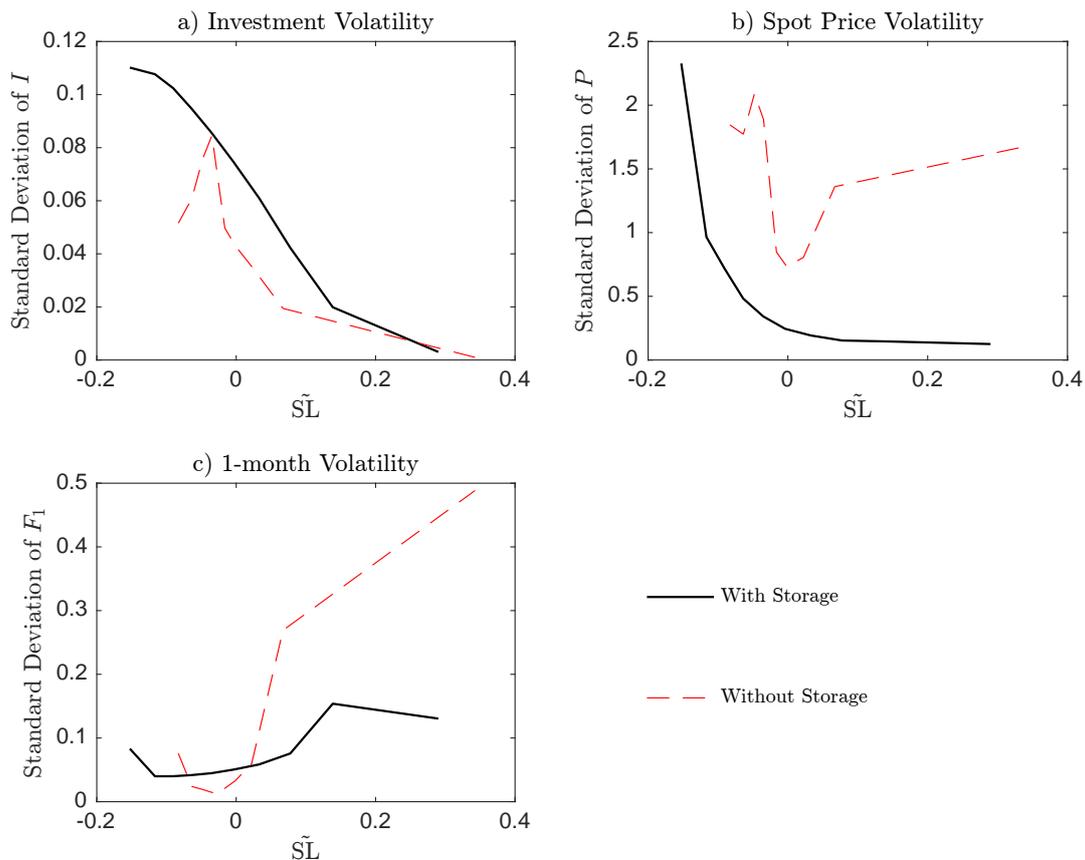


Figure 5.8. Conditional standard deviation for I , P , and F_1

Notes: The standard deviations for I , P , and F_1 from the model without storage and the model with storage, are plotted against the slope of the forward curve, \tilde{S} . These moments are computed for each of the 10th percentiles of the distribution of the simulated time series $\{I_t\}_{t=0}^T$ and $\{P_t\}_{t=0}^T$.

allow for storage. Since the latter is positively correlated with storage, the higher is the slope—e.g., the more inventories there are—the smoother is the spot price. This is not the case for a model without storage. The conditional volatility of the spot price is V-shaped: it is highest when the market is strongly backwardated, indicating a supply shortage, dips when the market is moderately satiated so that the forward and spot prices are closer and spikes again during a supply glut. On the other hand, the volatility of the forward price displays a V-shape for both models, but the extent to which the volatility changes is different between the two models depending on the commodity market tightness.

The volatility of the forward price in Figure 5.8 panel c) is directly mirrored in the average investment rate displayed in Figure 5.6. The investment rate is not only dependent on the expected price but also, given the nonnegativity constraint, hinges on the degree of future uncertainty. If uncertainty is higher, increasing the probability of bad spells, the producers will want to avoid being constrained and thus will invest less today. The presence of storage thus generates higher uncertainty for instances of a weakly backwardated market. Since in this regime the mass of the slope distribution for the model with storage is the biggest, then it is often that we are in this region of high uncertainty, which would be accompanied by lower investment rates. The increased endogenous risk gives way to a more volatile investment rate compared to the stark irreversible investment model. With storage, investment is always more volatile, except in the case of an extreme supply glut. A corollary to this result is that the standard deviation of the front-month price rises more sharply with the slope of the forward curve in a model with no storage capacity. A market in contango, with no inventory building, generates much more uncertainty for the expected price. This result falls from the increased smoothness of the spot price that is transferred to the future price through the storage arbitrage condition. On the other hand, in weak backwardation, the expected price is more volatile when storage is feasible. In this region of weak backwardation and low outgoing inventories, the forward and spot prices are still moving together but the spot price volatility is higher. The low excess capacity starts to translate into higher uncertainty because up until now, the producers have delayed investment more than they would have if they were not able to store. When outgoing inventories are running low, the spot price becomes more affected by both disturbances in supply and the persistent demand shock. Since the production capacity adjusts sluggishly, coupled with low outgoing inventory levels, the expected price will be more volatile than under the stark model. This excess volatility is the primary reason for which investment is lumpier in a model with the crowding-out effect of storage. Uncertainty justifies delaying investment since the value of waiting is higher and dominates the increase in the marginal benefit from investment.

Correspondingly, we can deliver a similar depiction to Figure 5.2 of the relationship between future uncertainty, investment, and storage for our simulated variables in Figure 5.9. The similarities are really striking. Indeed, the investment rate is decreasing in inventories, corroborating the relationship between the investment rate and the slope of the forward curve in Figure 5.6. Furthermore, storage has a destabilizing effect on the forward price.⁴² The elevated levels of uncertainty when the amount in store are high explains also why in this regime the optimal investment rate is lower. As in Figure 5.2, the volatility of the forward

⁴² The volatility of the subsequent forward prices collapses very rapidly an artifact of this class of models. This is noted in Routledge et al. (2000) with no clear solution to remedy such a result. For this reason, the subsequent conditional volatility of the forward price is not plotted in Figure 5.9.

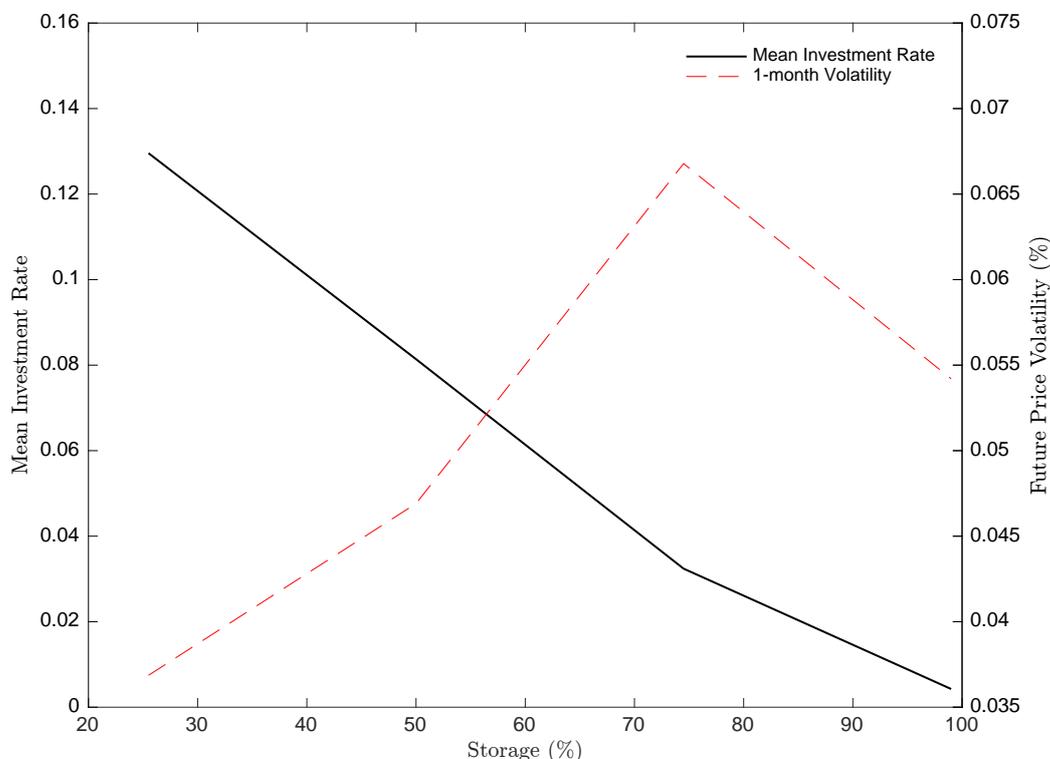


Figure 5.9. Conditional volatility of F_1 and mean investment rate

Notes: The left scale stands for the mean of the simulated investment rate while the right one represents the coefficient of variation of the simulated time series for the front-month price, F_1 . They both are computed for each 10th percentile of the storage levels distribution.

price starts to decrease when the supply glut is at its highest meaning that the storage smoothing effect on the spot price dominates its destabilizing effect.

All in all, uncertainty about the future, when the producer is constrained and cannot resell his capital in bad states of the world, makes him more prudent when deciding to invest. This prudence effect of the nonnegativity constraint on investment is most present when the market is weakly backwardated. The effect of the irreversibility constraint on investment is strengthened when storage is allowed for. This is a novel insight and certainly extends our understanding of a firm's investment decision when it can decide between two type of investment: fixed capital investment and inventory investment. Additionally, the endogenous risk that is brought about by the lockstep variation between the spot and the forward price is key in generating the destabilizing effect of storage on the forward price and the investment rate.

5.7 CONCLUSION

Storage and investment are the two main economic mechanisms serving as the theoretical bedrock of most of the dynamic commodity models. In addition, the recent development of liquid futures market offers a

valuable way to test empirically these forward-looking theories by looking at the market's reaction to various shocks and see if they match the model's predictions. Even from the strict perspective of the operators in the global market of crude oil, the two most scrutinized metrics are the inventory levels and drilling counts publicly published on a weekly basis. They are believed to mirror the prevailing supply and demand balance, where a glut is associated with ballooned inventories and diminishing capital expenditures. This is why we believe that it is worth to study investment and storage decisions jointly to account for fluctuations in prices, a point acknowledged but thus far neither explored in the dynamics of capital accumulation nor competitive storage model literature.

This study aims at filling this gap by building upon three strands of the economics and finance literature (e.g., capital accumulation, storage and futures pricing) to lay out a partial equilibrium-framework placing investment and storage at the forefront of the economic decisions dictating the dynamics of a commodity market. The simulation results obtained on two versions of the model depending whether storage is acknowledged clearly support the importance of considering both economic mechanisms. They demonstrate that, at the margin, investment is less profitable whenever storage is possible. Indeed, not only carrying inventories will weigh on the expected price and in turn the marginal benefit of investing today but also will raise future uncertainty and thus the options value of waiting and postponing investment. Put another way, operators invest less often but more aggressively. The deferred investment translates into lower capital stock and hence a mitigated production capacity. As a result, the commodity becomes scarcer, storing is more costly, thereby leading to an upward turn in the spot price and a tighter market. The supply and demand tension is eventually alleviated with a renewed increase in the production capacity through capital investment. Such a narrative of the cyclical emergence of booms and busts in the oil industry broadly proves to match the data fairly well. The key insight which emerges out of the confluence of inventory and fixed capital investment is the implications of lockstep variations in the spot and forward prices on the investment decision. This tight link between the two prices translates into higher future uncertainty, rendering the nonnegativity constraint even more penalizing. Ultimately, storage reinforces the irreversibility of investment.

In terms of extensions, it might be worthwhile to study the effects of capital adjustment costs of various nature—fix, convex and non-convex—in the tradition of Cooper and Haltiwanger (2006) since they are possibly significant in capital intensive sectors like the oil industry. Among the expected effects of interest are a higher persistence in production translated into the volatility levels of forward prices which are dying-off too quickly in our current modeling as compared to the levels observed, although it is a shared drawback among many dynamic economic models of this kind. Attractive also should be considering the new frictions subsequent to the introduction of a second but not predetermined factor of production (for e.g., labor known to be the very first expendable in times of turmoil in the oil market) and the resulting effects on the dynamics implied by the model. Finally, and perhaps more challenging given the computational issues at stake, it would be to push the empirical analysis even further in estimating the model key parameters in place of the current calibration.

CHAPTER 6

CONCLUSION

“Essentially, all models are wrong, but some are useful.”

Box and Draper (1987, p.424)

6.1 GENERAL CONCLUSION

In economy as in sciences, a model is an abstraction of the reality, a mathematical representation which simplifies a phenomenon to be studied and its associated environment so as to reveal the key mechanisms at stakes, the roles they play and the way they interact with one another. In this regard, the modeling exercise necessarily requires a set of assumptions to simplify things. This is why, as stated by Box and Draper, to ask to a model embodying the whole truth, if any, is somewhat utopian and even not really desirable. All that matters in the end is its usefulness. In economics, a model is useful if it helps to interpret the data, clarify and organize the thinking, replicate key observed phenomena or else implement conditional forecasts to test and compare the impacts of alternative policies. The two main metrics to assess the merit of an economic model are internal and external consistency, the challenge being then to strike the right balance between these two pillars.

In the context of commodity price volatility studies, looking at the fundamentals of supply, demand and inventories is a natural place to start thinking about the price behavior in the dynamic and uncertain world commodity markets. Also natural is to assume that actors in these markets are in competition to smooth their consumption over time, and thus try their best to predict the future price so as to make their decisions accordingly. Put in equations, this roughly yields the skeleton of the canonical competitive storage model along with its associated set of hypotheses. Taking for granted all these theoretical developments and applying the latest statistical tools available in macroeconometrics, the ultimate objective of the thesis is to attempt extending the storage model in order to get a more comprehensive understanding of the key mechanisms governing the booms and busts episodes observed in the global prices of staples goods.

With this in mind, the introducing survey reviews the variety of empirical strategies developed so far to match the storage theory with the observed data. As is often the case in empirical macroeconomics, the variety of techniques employed vary in the amount of theoretical constraints imposed on the data. Regardless

of the ad-hoc or structural approach followed, together the results justify the initial hopes placed in the storage theory in confirming the empirical relevance of the storage model, thereby strengthening its status as a promising device to analyze the price variations of basic products on the quantitative front. That said, the findings also emphasize the numerous pitfalls currently plaguing the storage framework and which, if settled, could help to answer some of the present puzzling phenomena observed in commodity price series, including the excessive co-movements and the high levels of serial correlation. Remembering the aforementioned double criteria of internal and external consistency to deem the performance of a model, the chapter ends by suggesting a research agenda, gradual in the level of time and effort involved, to improve the model's explanatory power and from which originate the three subsequent chapters.

The first contribution is purely empirical. It starts by acknowledging the recent agreement, in the dedicated literature, about the fact that commodity prices are best described by short to medium-run cyclical fluctuations around a long-run trend affected by structural breaks. In view of the absence of satisfying theoretical explanations for these long-term movements a pragmatic empirical strategy has been adopted. More precisely, the idea, borrowed from the DSGE literature (Canova, 2014), consists in coming up with a reduced-form representation for the trend which is then jointly estimated with the structural parameters of the model. With such a statistical repair of the modeling which preserves the internal consistency of the structure, the model's deep parameters are found to be more plausible and eventually lowers the level of persistence in prices to be explained. Put it another way, part of the observed persistence has nothing to do with the storage theory and, instead, should be explained by the trend. If not it is not only the empirical relevance of the storage theory but also the reliability of the estimations which might be reduced.

The second contribution is innovative in many respects and I think quite central for the further econometric work on the storage model, including in the near future. The initial statement is clear: any estimations of richer specification of the storage model is hampered as long as inference relies on prices information alone, as has been the case so far. Put differently, reasoning from a price change is too limited an approach for getting a deeper understanding of the key determinants of the observed dynamics in the commodity markets. Hence, still inspired from the recent developments in the DSGE literature, we provide an econometric procedure to take the storage model to the data on both prices and quantities. The latter bring a complement of information allowing to freely recover additional key parameters among which are the supply elasticity, the volatility of the production as well as demand structural shocks. Furthermore, as there are more parameters to estimate, the classical maximum likelihood approach has been replaced with its Bayesian counterparts, more convenient and widely used to estimate the DSGE model parameters though, as of now, never to infer those of the storage model. Overall, we believe both these novelties will help paving the way for future research. Indeed, any serious expansion of the storage model, on both the theoretical and empirical fronts, require the adoption of a state-space representation of the storage framework as well as the incorporation of data on quantities in the set of observables, while the Bayesian tools seem more appropriate for recovering the greater number of parameters.

The last contribution is more theoretical but no less important regarding the future empirical abilities of the model, at least in the longer-run. Establishing that booms and busts cycles observed in the oil sector are

for the most part a supply and demand story, we think interesting to extend the storage model on the supply side in accounting for the dynamics of capital accumulation. Intuitively, storage is nothing but another kind of investment, and thus both should play central roles in driving the spot and future price dynamics in world commodity markets. This is confirmed by the simulation results obtained with the investment-augmented storage model which are fairly well supported by the crude oil data. The prime finding is certainly the crowding-out effect of storage on investment. The main limit of this work is that the model has now three state variables and thus may be difficult to estimate structurally.

6.2 PERSPECTIVES

Although I hope this dissertation contributed to reinforce the empirical relevance of the competitive storage model, the latter remains undeniably improvable if, in echo to the introductory citation of Box and Draper (1987), it is to become an analytical tool “useful” for organizing our thinking about the commodity price volatility from a quantitative standpoint. In this respect, using a typology similar to the one chosen in the opening survey, I suggest below some avenues of extensions to be considered at different time scales, depending on the amount of research energy to be allocated along with the level of computational techniques required.

NOISY PRICES This is the most natural and straight continuation of the work undertaken in chapter 4. Indeed, to build upon the latest econometric development of Cafiero et al. (2015) and keep an analytic form for the Maximum Likelihood estimator, prices have been assumed observed without noises. The latter assumption is very restrictive in terms of the structural shocks which can be freely identified. Relaxing this hypothesis will constitute a genuine step toward the evaluation of the fitting performance of more general specifications of the storage model. Testing alternatives set-ups against one each other will allow for a comprehensive exploration of the dimensions in which the storage theory does not seem to work well, and thus indicating in which directions model’s extensions are needed. However, this comes at a computational cost since, with measurement errors on prices, the likelihood function is no longer tractable and so has to be simulated using Monte-Carlo approximation techniques. Specifically, the whole estimation procedure rests on the so-called particle filter, recently introduced in the DSGE literature (Fernández-Villaverde and Rubio-Ramírez, 2007) but, as far as I know, never applied to the storage model.

MACROECONOMIC FEEDBACKS Alongside the autocorrelation, another puzzle in the commodity price behavior for which the storage model is unable to account for is the excess of co-movements (Pindyck and Rotemberg, 1990). As discussed in chapter 2, the integration of macroeconomic spillovers through the interest rate channel is worth considering for the storage model to be able to capture this kind of richer movements in and across prices. As is common in empirical macroeconomics, the incorporation of such macroeconomic forces (e.g., exchanges rates) can be first in the form of an ad-hoc repair deprived of microfoundations, before ideally being derived from microeconomic principles with the benefit of theoretical advances. On the

empirical front of this endeavor, the particle filter can well be the powerful tool able to recover, for instance, the deep parameters of the Frankel (1986)'s overshooting model expressed in a state-space form.

Another benefit of thinking about the interest rate variable as a bridge to connect the storage model with the complex macroeconomic environment, is its suitability for including the potential effects of the financial markets. Indeed, the current state of the storage theory and, let alone, the storage model, is almost silent about the interactions between the physical commodity markets and the financial sector. If the links between the real economy and finance have long been studied, the Great Recession triggered a race to the financialization of the macroeconomic models in which the financial industry now plays a key role in driving the business cycles, and the literature of the storage model can well follow suits. Admittedly, to date the storage model is a representative-agents based framework with forward-looking and rational expectations. Still, these are natural and meaningful starting assumptions, not universal rules set in stone.

TWEAKING THE CORE ASSUMPTIONS? It is fair to say that the sharp movements of prices on the world commodity markets witnessed over the past decade are hardly reconcilable with the fundamentals alone. With this in mind, dealing with the growing inflow of financial investors likely to trade with sentiments—the pure “animal spirits”—and thus no real bearing to the fundamentals, and the ultimate consequences on the commodity prices is at least a natural and fertile field of investigation. This is why, I think there is a place, in the literature of commodity price volatility, for the effects of financial linkages to explain specific events such as destabilizing speculative bubbles, episodes of self-fulfilling prophecies, panic and flight to safety, herding behaviors and other irrational moves alike. From this perspective, one can think in particular about heterogeneous agents and learning expectations models. Along these lines, of interest is the concept of rational destabilization developed in De Long et al. (1990) or, close in spirit but more recent, the approach of Singleton (2014) which consists in introducing informational frictions in the modeling by assuming that market practitioners have a different interpretation—e.g. “difference of opinions”—about the same publicly available information related to the economic fundamentals. Conceptually, the traders' behaviors follow a learning mechanism in which price expectations are a mix between market fundamentals along with past and current prices. Together the heterogeneity and learning mechanisms are likely to magnify the up and/or downward swings in prices similar to the booms and bust cycles. Having said this, it should not be forgotten that, sooner or later, prices are deemed to revert back to the level dictated by the prevailing physical supply and demand conditions (Knittel and Pindyck, 2016). As a result, the financial economics literature is torn apart about the real influence speculation actually has on the prices of primary products, driving them away from the market fundamentals. The thing is that the publicly available data is sparse, of poor reliability and so not very insightful for attempting to fix the controversy in quantitative terms. Add to this data problem, both the numerous methodological and computational challenges involved, and there are all the ingredients for making the introduction of finance into the storage theory a very long-winded undertaking.

NO BLACK BOXES As a last remark, to keep working with parsimonious models with crystal clear inner-workings, I do not think reasonable to try adding all these potential extensions in a single framework with the vain hope of matching the whole diversity of patterns observed in the data. More realistic would be to

build and structurally estimate different versions of the storage model, incorporating one or a few of the aforementioned developments, and for eventually being able to deliver reliable answers to questions posed conditional on a given set of circumstances (e.g., normal times vs markets turmoil).

In sum, in spite of all what has already been achieved to rekindle the interest and usefulness of the competitive storage model, there are still many precious insights which are yet to be learned from this tool. For all these reasons future work in this area are part of a very exciting and dynamic research program.

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RÉSUMÉ SUBSTANTIEL

Cette thèse propose une analyse empirique et théorique de la volatilité des prix des matières premières en utilisant le modèle de stockage compétitif à anticipations rationnelles. En substance, la théorie du stockage stipule que les prix des commodités sont susceptibles de s'envoler dès lors que les niveaux de stocks sont bas et donc dans l'incapacité de prémunir le marché contre des chocs exogènes. L'objectif principal poursuivi dans ce travail de recherche est d'utiliser les outils statistiques pour confronter le modèle de stockage aux données afin d'évaluer le bien-fondé empirique de la théorie du stockage, identifier ses potentiels défauts et proposer des solutions possibles afin d'améliorer son pouvoir explicatif. Dans ce contexte, la diversité des approches économétriques employées jusqu'à présent pour tester le modèle et ses prédictions théoriques est passée en revue dans le chapitre introductif (Ch. 2). Dans l'ensemble, malgré son caractère relativement parcimonieux, le modèle de stockage s'avère être en mesure de reproduire de nombreux faits stylisés observés dans les données de prix. Cela étant, il existe toujours des caractéristiques des prix non expliquées, comme les hauts niveaux d'autocorrélations ou les co-variations excessives. Les chapitres suivants explorent trois pistes différentes pour essayer d'augmenter la cohérence empirique du modèle de stockage. Le chapitre 3 repose sur l'idée qu'il existe des mouvements de long-termes dans les prix des matières premières qui n'ont rien à voir avec la théorie du stockage. Ceci tend à être confirmé par les résultats obtenus par la mise en œuvre d'une méthode d'estimation hybride permettant de déterminer conjointement les paramètres fondamentaux du modèle avec ceux caractérisant la tendance. En effet, les estimations des paramètres structurels sont plus plausibles et le modèle s'ajuste mieux aux données. Dans le chapitre 4, la procédure de test de la théorie du stockage est encore approfondie grâce au développement d'une méthode empirique pour estimer le modèle à la fois sur données de prix et de quantités, une première dans la littérature. L'apport d'information supplémentaire permet d'estimer et de comparer des spécifications alternatives et plus riches du modèle, d'inférer des paramètres tels que les élasticités d'offre et de demande, qui ne sont pas identifiables lorsque seuls les prix sont utilisés pour l'estimation. Une autre nouveauté est que des méthodes Bayésiennes sont utilisées pour l'inférence au lieu des approches fréquentistes employées jusqu'à présent. Ces deux innovations devraient permettre d'ouvrir la voie à des recherches futures en permettant l'estimation de modèles aux structures plus complexes. Le dernier chapitre est plus théorique et porte sur l'extension du volet offre du modèle en prenant en compte la dynamique d'accumulation du capital. Sur le plan conceptuel, le stockage n'est autre qu'une seconde forme d'investissement, et par conséquent les deux variables d'investissement et de stockage devraient jouer des rôles primordiaux dans la dynamique des prix spot et futures sur les marchés mondiaux des commodités. Cette intuition est confirmée par les résultats des simulations obtenues avec un modèle de stockage augmenté de l'investissement, qui sont assez bien en adéquation avec les données du pétrole brut. Le résultat principal est l'effet d'éviction qu'a le stockage sur l'investissement.

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Titre : Reconsidérer le modèle de stockage compétitif comme outil d'analyse empirique de la volatilité des prix des matières premières

Mots clés : Inférence Bayésienne, estimation structurelle, volatilité des marchés des matières premières, stockage, tendances, investissement.

Résumé : Cette thèse propose une analyse empirique et théorique de la volatilité des prix des matières premières en utilisant le modèle de stockage compétitif à anticipations rationnelles. En substance, la théorie du stockage stipule que les prix des commodités sont susceptibles de s'envoler dès lors que les niveaux de stocks sont bas et donc dans l'incapacité de prémunir le marché contre des chocs exogènes. L'objectif principal poursuivi dans ce travail de recherche est d'utiliser les outils statistiques pour confronter le modèle de stockage aux données afin d'évaluer le bien-fondé empirique de la théorie du stockage, identifier ses potentiels défauts et proposer des solutions possibles afin d'améliorer son pouvoir explicatif. Dans ce contexte, la diversité des approches économétriques employées jusqu'à présent pour tester le modèle et ses prédictions théoriques est passée en revue dans le chapitre introductif (Ch. 2). Les chapitres suivants explorent trois pistes différentes pour essayer d'augmenter la cohérence empirique du modèle de stockage. Le chapitre 3 repose sur l'idée qu'il existe des mouvements de long- termes dans les prix des

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Title : Revisiting the competitive storage model as a tool for the empirical analysis of commodity price volatility

Keywords : Bayesian inference, non-linear dynamic models, structural estimation, commodity markets volatility, trends, storage, investment.

Abstract : This thesis proposes an empirical and theoretical analysis of commodity price volatility using the competitive storage model with rational expectations. In essence, the underlying storage theory states that commodity prices are likely to spike when inventory levels are low and cannot buffer the market from exogenous shocks. The prime objective pursued in this dissertation is to use statistical tools to confront the storage model with the data in an attempt to gauge the empirical merit of the storage theory, identify its potential flaws and provide possible remedies for improving its explanatory power. In this respect, the variety of econometric strategies employed so far to test the model itself or its theoretical predictions are reviewed in the opening survey (Ch. 2). The subsequent chapters explore three different routes with the aim of increasing the empirical relevance of the storage framework. Chapter 3 rests on the idea that there might exist long-term movements in the raw commodity

price series which have nothing to do with the storage theory. This tends to be confirmed by the results obtained by implementing a hybrid estimation method for recovering jointly the model's deep parameters with those characterizing the trend. In chapter 4 the testing of the storage theory is pushed even further thanks to the development of an empirical strategy to take the storage model to the data on both prices and quantities, for the first time in the literature. Another novelty is that Bayesian methods are used for inference in contrast to the frequentist approaches employed thus far. Hopefully both these innovations should help paving the way for future research in allowing for the estimation of more complex model set-ups. The last chapter is more theoretical as it deals with the storage model extension on the supply side to account for the dynamics of capital accumulation. The key finding is the crowding-out effect of storage on investment.